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Mark Scheme (Results)

January 2007

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GCE

GCE Mathematics

Statistics (6683)

January 2007
6683 Statistics S1
Mark Scheme

Question number	Scheme	Marks
1. (a)	(£) 17 Just **17**	B1 (1)
(b)	$\sum t = 212$ and $\sum m = 61$ (Accept as totals under each column in qu.)	B1, B1
	$S_{tm} = 2485 - \frac{61\times 212}{10}$, = 1191.8 awrt **1190** or 119 (3sf)	M1, A1
	$S_{tt} = 983.6$ (awrt 984) and $S_{mm} = 1728.9$ (awrt 1730) (or 98.4 and 173)	A1, A1 (6)
(c)	$r = \frac{1191.8}{\sqrt{983.6\times 1728.9}}$	M1, A1f.t.
	= 0.913922… awrt **0.914**	A1 (3)
(d)	0.914 (Must be the same as (c) or awrt 0.914)	B1f.t. ($\|r\|$ <1)
	e.g. linear transformation, coding does not affect coefficient (or recalculate)	dB1 (2)
(e)	0.914 suggests longer spent shopping the more spent. (Idea more time, more spent)	B1
	0.178 different amounts spent for same time.	B1 (2)
(f)	e.g. might spend short time buying 1 expensive item OR might spend a long time checking for bargains, talking, buying lots of cheap items.	B1g (1)
		15 marks

(b) M1 for one correct formula seen, f.t. their $\sum t, \sum m$ [Use 1st A1 for 1 correct, 2nd A1 for 2 etc]

(c) M1 for attempt at correct formula, $\frac{2485}{\sqrt{2101\times 5478}}$ scores M1A0A0

A1ft f.t. their values for S_{tt} etc from (b) but don't give for S_{tt} = 5478 etc (see above)

Answer only (awrt 0.914) scores 3/3, 0.913 (i.e. truncation) can score M1A1ft by implication.

(d) 2nd B1 dependent on 1st B1 Accept $\sum m = 261, \sum m^2 = 8541, \sum tm = 6725 \rightarrow 0.914$

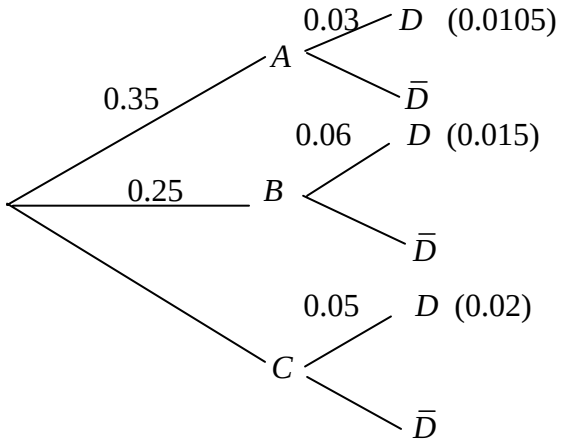
(e) One mark for a sensible comment relating to each coefficient

For 0.178 allow "little or no link between time and amount spent". Must be in context.

Just saying 0.914 is strong +ve correlation between amount spent and time shopping and 0.178 is weak correlation …scores B0B0.

(f) B1g for a sensible, practical suggestion showing that other factors might affect the amount spent.

E.g. different day (weekend vs weekday) or time of day (time spent queuing if busy)

Question number	Scheme		Marks
2. (a)		Correct tree shape *A*, *B* and *C* and 0.35 and 0.25 *D* (x3) and 0.03, 0.06, 0.05 (May be implied by seeing P$(A \cap D)$ etc at the ends)	M1 A1 A1 (3)
(b)(i)	P$(A \cap D) = 0.35 \times 0.03$, = **0.0105** or $\frac{21}{2000}$		M1, A1
		P(*C*) = 0.4 (anywhere)	B1
(ii)	P(*D*) = (i) + 0.25x 0.06 + (0.4x0.05)		M1
	= **0.0455** or $\frac{91}{2000}$		A1 (5)
(c)	P$(C \mid D) = \frac{\text{P}(C \cap D)}{\text{P}(D)}$, = $\frac{0.4 \times 0.05}{\text{(ii)}}$		M1, A1ft
	= 0.43956… or $\frac{40}{91}$	**0.44** or awrt **0.440**	A1 (3)
	[Correct answers only score full marks in each part]		**11 marks**

(a) M1 for tree diagram, 3 branches and then two from each. At least one probability attempted.

(b) 1st M1 for 0.35x0.03. Allow for equivalent from their tree diagram.

B1 for P(*C*) = 0.4, can be in correct place on tree diagram or implied by 0.4x0.05 in P(*D*).

2nd M1 for all 3 cases attempted and some correct probabilities seen, including +. Can ft their tree.

Condone poor use of notation if correct calculations seen. E.g. P$(C \mid D)$ for P$(C \cap D)$.

(c) M1 for attempting correct ratio of probabilities. There must be an attempt to substitute some values in a correct formula. If no correct formula and ration not correct ft score M0.

Writing P(*D*|*C*) and attempting to find this is M0.

Writing P(*D*|*C*) but calculating correct ratio – ignore notation and mark ratios.

A1ft must have their 0.4 x0.05 divided by their (ii).

If ratio is incorrect ft (0/3) unless correct formula seen and part of ratio is correct then M1.

Question number	Scheme	Marks
3. (a)	N.B. Part (a) doesn't have to be in a table, could be a list P(X = 1) = …etc	B1, B1, B1

x	1	2	3	4	5	6
P($X = x$)	$\frac{1}{36}$	$\frac{3}{36}$	$\frac{5}{36}$	$\frac{7}{36}$	$\frac{9}{36}$	$\frac{11}{36}$

0.0278, 0.0833, 0.139, 0.194, 0.25, 0.306 (Accept awrt 3 s.f) (3)

(b) P(3) + P(4) + P(5) =, $\frac{21}{36}$ or $\frac{7}{12}$ or awrt 0.583 M1, A1 (2)

(c) $E(X) = \frac{1}{36} + 2\times\frac{3}{36} + ..., = \frac{161}{36}$ or $4.47\dot{2}$ or $4\frac{17}{36}$ M1, A1 (2)

(d) $E(X^2) = \frac{1}{36} + 2^2\times\frac{3}{36} + ..., = \frac{791}{36}$ or full expression or $21\frac{35}{36}$ or awrt 21.97 M1, A1

Var(X) = $\frac{791}{36} - \left(\frac{161}{36}\right)^2$, = **1.9714… *** M1, A1c.s.o. (4)

(e) Var(2 – 3X) = 9×1.97 or $(-3)^2\times1.97$, = 17.73 awrt **17.7** or $\frac{2555}{144}$ M1, A1 (2)

13 marks

(a) 1st B1 for x = 1, … 6 and at least one correct probability N.B. $\frac{3}{36} = \frac{1}{12}$ and $\frac{9}{36} = \frac{1}{4}$

2nd B1 for at least 3 correct probabilities

3rd B1 for a fully correct probability distribution.

(b) M1 for attempt to add the correct three probabilities, ft their probability distribution

(c) M1 for a correct attempt at E(X). Minimum is as printed. Exact answer only scores M1A1.

[Division by 6 at any point scores M0, no ISW. Non-exact answers with no working score M0.]

(d) 1st M1 for a correct attempt at $E(X^2)$. Minimum as printed. $\frac{791}{36}$ or awrt 21.97 scores M1A1.

2nd M1 for their $E(X^2) - \left(\text{their } E(X)\right)^2$.

2nd A1 cso needs awrt 1.97 and $\frac{791}{36} - \left(\frac{161}{36}\right)^2$ or $\frac{2555}{1296}$ or any fully correct expression seen.

Can accept at least 4 sf for both. i.e. 21.97 for $\frac{791}{36}$, 4.472 for $\frac{161}{36}$, 20.00 for $\left(\frac{161}{36}\right)^2$.

(e) M1 for correct use of Var($aX + b$) formula or a full method.

NB $-3^2\times1.97$ followed by awrt 17.7 scores M1A1 BUT $-3^2\times1.97$ alone, or followed by – 17.7, scores M0A0.

Question number	Scheme	Marks
4. (a)	Positive skew (both bits)	B1 (1)
(b)	$19.5 + \frac{(60-29)}{43}\times 10$, = 26.7093…. awrt **26.7**	M1, A1 (2)
	(N.B. Use of 60.5 gives 26.825… so allow awrt 26.8)	
(c)	$\mu = \frac{3550}{120} = 29.5833...$ or $29\frac{7}{12}$ awrt **29.6**	B1
	$\sigma^2 = \frac{138020}{120} - \mu^2$ or $\sigma = \sqrt{\frac{138020}{120} - \mu^2}$	M1
	$\sigma = 16.5829...$ or ($s = 16.652...$) awrt **16.6** (or s = 16.7)	A1 (3)
(d)	$\frac{3(29.6-26.7)}{16.6}$	M1A1ft
	= 0.52…. awrt **0.520** (or with s awrt 0.518)	A1 (3)
	(N.B. 60.5 in (b) ...awrt 0.499[or with s awrt 0.497])	
(e)	0.520 > 0 correct statement about their (d) being >0 or < 0	B1ft
	So it is consistent with (a) ft their (d)	dB1ft (2)
(f)	Use Median	B1
	Since the data is skewed or less affected by outliers/extreme values	dB1 (2)
(g)	If the data are symmetrical or skewness is zero or normal/uniform distribution	B1 (1)
	("mean =median" or "no outliers" or "evenly distributed" all score B0)	**14 marks**

(b) M1 for (19.5 or 20) + $\frac{(60-29)}{43}\times 10$ or better. Allow 60.5 giving awrt 26.8 for M1A1
Allow their $0.5n$ [or $0.5(n+1)$] instead of 60 [or 60.5] for M1.

(c) M1 for a correct expression for σ, σ^2, s or s^2. NB $\sigma^2 = 274.99$ and $s^2 = 277.30$
Condone poor notation if answer is awrt16.6 (or 16.7 for s)

(d) M1 for attempt to use this formula using their values to any accuracy. Condone missing 3.
1st A1ft for using their values to at least 3sf. Must have the 3.
2nd A1 for using accurate enough values to get awrt 0.520 (or 0.518 if using s)
NB Using only 3 sf gives 0.524 and scores M1A1A0

(e) 1st B1 for saying or implying correct sign for their (d). B1g and B1ft. Ignore "correlation" if seen.
2nd B1 for a comment about consistency with their (d) and (a) being positive skew, ft their (d) only
This is dependent on 1st B1: so if (d)>0, they say yes, if (d)<0 they say no.

(f) 2nd B1 is dependent upon choosing median.

Question number	Scheme	Marks
5. (a)	Time is a <u>continuous</u> variable or data is in a <u>grouped</u> frequency table	B1 (1)
(b)	Area is proportional to frequency or $A \propto f$ or $A = kf$	B1 (1)
(c)	$3.6 \times 2 = 0.8 \times 9$ 1 child represented by 0.8	M1 dM1 A1 cso (3)
(d)	(Total) = $\frac{24}{0.8}$, = **<u>30</u>**	M1, A1 (2)
		7 marks

(b) 1st B1 for one of these correct statements.

"Area proportional to frequency density" or "Area = frequency" is B0

(c) 1st M1 for a correct combination of any 2 of the 4 numbers: 3.6, 2, 0.8 and 9

e.g. 3.6×2 or $\frac{3.6}{0.8}$ or $\frac{0.8}{2}$ etc BUT e.g. $\frac{3.6}{2}$ is M0

2nd M1 dependent on 1st M1 and for a correct combination of 3 numbers leading to 4th.

May be in separate stages but must see all 4 numbers

A1cso for fully correct solution. Both Ms scored, no false working seen and <u>comment required.</u>

(d) M1 for $\frac{24}{0.8}$ seen or implied.

Question number	Scheme	Marks
6. (a)	Used to simplify or represent a real world problem Cheaper or quicker or easier (than the real situation) or more easily modified To improve understanding of the real world problem Used to predict outcomes from a real world problem (idea of predictions)	(any two lines) B1 B1 (2)
(b)	(3 or 4) Model used to make predictions. (Idea of predicted values based on the model) (4 or 3) (Experimental) data collected (7) Model is refined.	B1 B1 B1 (3) **5 marks**

(a) 1st B1 For one line

2nd B1 For a second line

Be generous for 1st B1 but stricter for B1B1

(b) 1st & 2nd B1 These two points can be interchanged.

Idea of values from (experimental) data and predicted values based on the model.

1st B1 for predicted values from model e.g. "model used to gain suitable data"

2nd B1 for data collected. Idea of experimental data but "experiment" needn't be explicitly seen

3rd B1 This should be stage 7. Idea of refinement or revision or adjustment

Question number	Scheme	Marks
7. (a)	$P(X < 91) = P(Z < \frac{91-100}{15})$ Attempt standardisation	M1
	$= P(Z < -0.6)$	A1
	$= 1 - 0.7257$	M1
	$= 0.2743$ awrt **0.274**	A1 (4)
(b)	$1 - 0.2090 = 0.7910$ 0.791	B1
	$P(X > 100+k) = 0.2090$ or $P(X < 100+k) = 0.7910$ (May be implied)	M1
	Use of tables to get $z = 0.81$	B1
	$\frac{100+k-100}{15}$,=0.81 (ft their $z = 0.81$, but must be z not prob.)	M1, A1ft
	***k* = 12**	A1 cao (6)
		10 marks

(a) 1st M1 for attempting standardisation. $\pm\frac{(91-\mu)}{\sigma}$ or σ^2. Can use of 109 instead of 91.Use of 90.5 etc is M0

1st A1 for – 0.6 (or + 0.6 if using 109)

2nd M1 for 1 – probability from tables. Probability should be > 0.5)

(b) 1st B1 for 0.791 seen or implied.

1st M1 for a correct probability statement, but must use *X* or *Z* correctly. Shown on diagram is OK

2nd B1 for awrt 0.81 seen (or implied by correct answer - see below) (Calculator gives 0.80989…)

2nd M1 for attempting to standardise e.g. $\frac{100+k-100}{15}$ or $\frac{k}{15}$

$\frac{X-100}{15}$ scores 2nd M0 until the 100+ *k* is substituted to give *k*, but may imply 1st M1 if *k*= 112.15 seen

1st A1ft for correct equation for *k* (as written or better). Can be implied by *k* = 12.15 (or better)

2nd A1 for *k* = 12 only.

Answers only

k = 112 or 112.15 or better scores 3/6 (on EPEN give first 3 marks)

k = 12.15 or better (calculator gives 12.148438…) scores 5/6 (i.e loses last A1 only)

k = 12 (no incorrect working seen) scores 6/6

NB Using 0.7910 instead of 0.81 gives 11.865 which might be rounded to 12. This should score no more than B1M1B0M1A0A0.