

# Mark Scheme (Results)

## January 2011

GCE

### GCE Core Mathematics C2 (6664) Paper 1

Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers.

Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.

For further information, please call our GCE line on 0844 576 0025, our GCSE team on 0844 576 0027, or visit our website at [www.edexcel.com](http://www.edexcel.com).

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our **Ask The Expert** email service helpful.

Ask The Expert can be accessed online at the following link:

<http://www.edexcel.com/Aboutus/contact-us/>

January 2011

Publications Code US026235

All the material in this publication is copyright  
© Edexcel Ltd 2011

## General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
  - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
  - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
  - **B** marks are unconditional accuracy marks (independent of M marks)
  - Marks should not be subdivided.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol  $\surd$  will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper
- $\square$  The second mark is dependent on gaining the first mark

January 2011  
Core Mathematics C2 6664  
Mark Scheme

Question Number	Scheme	Marks
1.	<p>(a) <math>f(x) = x^4 + x^3 + 2x^2 + ax + b</math></p> <p>Attempting <math>f(1)</math> or <math>f(-1)</math>.  <math>f(1) = 1 + 1 + 2 + a + b = 7</math> or <math>4 + a + b = 7 \Rightarrow a + b = 3</math> (as required) <b>AG</b></p>	M1 A1 * cso (2)
	<p>(b) Attempting <math>f(-2)</math> or <math>f(2)</math>.  <math>f(-2) = \underline{16 - 8 + 8 - 2a + b = -8}</math> <math>\{\Rightarrow -2a + b = -24\}</math>            Solving both equations simultaneously to get as far as <math>a = \dots</math> or <math>b = \dots</math>            Any one of <math>a = 9</math> or <math>b = -6</math>            Both <math>a = 9</math> and <math>b = -6</math></p>	M1 A1 dM1 A1 A1 cso (5) [7]
<b>Notes</b>		
(a)	<p>M1 for attempting either <math>f(1)</math> or <math>f(-1)</math>.            A1 for applying <math>f(1)</math>, setting the result equal to 7, and manipulating this correctly to give the result given on the paper as <math>a + b = 3</math>. Note that the answer is given in part (a).</p>	
(b)	<p>M1: attempting either <math>f(-2)</math> or <math>f(2)</math>.            A1: <u>correct underlined equation</u> in <math>a</math> and <math>b</math>; eg <u><math>16 - 8 + 8 - 2a + b = -8</math></u> or equivalent, eg <math>-2a + b = -24</math>.            dM1: an attempt to eliminate one variable from 2 linear simultaneous equations in <math>a</math> and <math>b</math>. Note that this mark is dependent upon the award of the first method mark.            A1: any one of <math>a = 9</math> or <math>b = -6</math>.            A1: both <math>a = 9</math> and <math>b = -6</math> and a correct solution only.</p>	
<p><b><u>Alternative Method of Long Division:</u></b>            (a) M1 for long division by <math>(x - 1)</math> to give a remainder in <math>a</math> and <math>b</math> which is independent of <math>x</math>.            A1 for {Remainder = } <math>b + a + 4 = 7</math> leading to the correct result of <math>a + b = 3</math> (answer given.)            (b) M1 for long division by <math>(x + 2)</math> to give a remainder in <math>a</math> and <math>b</math> which is independent of <math>x</math>.            A1 for {Remainder = } <u><math>b - 2(a - 8) = -8</math></u> <math>\{\Rightarrow -2a + b = -24\}</math>.            Then dM1A1A1 are applied in the same way as before.</p>		

Question Number	Scheme	Marks
2.	<p>(a) <math>11^2 = 8^2 + 7^2 - (2 \times 8 \times 7 \cos C)</math>  <math>\cos C = \frac{8^2 + 7^2 - 11^2}{2 \times 8 \times 7}</math> (or equivalent)  <math>\{\hat{C} = 1.64228\dots\} \Rightarrow \hat{C} = \text{awrt } 1.64</math></p>	<p>M1 A1 A1 cso (3)</p>
	<p>(b) Use of Area <math>\Delta ABC = \frac{1}{2}ab\sin(\text{their } C)</math>, where <math>a, b</math> are any of 7, 8 or 11.  <math>= \frac{1}{2}(7 \times 8)\sin C</math> using the value of their <math>C</math> from part (a).  <math>\{= 27.92848\dots \text{ or } 27.93297\dots\} = \text{awrt } 27.9</math> (from angle of either <math>1.64^\circ</math> or <math>94.1^\circ</math>)</p>	<p>M1 A1 ft A1 cso (3) <b>[6]</b></p>
<b>Notes</b>		
	<p>(a) M1 is also scored for <math>8^2 = 7^2 + 11^2 - (2 \times 7 \times 11 \cos C)</math> or <math>7^2 = 8^2 + 11^2 - (2 \times 8 \times 11 \cos C)</math>  or <math>\cos C = \frac{7^2 + 11^2 - 8^2}{2 \times 7 \times 11}</math> or <math>\cos C = \frac{8^2 + 11^2 - 7^2}{2 \times 8 \times 11}</math>  1<sup>st</sup> A1: Rearranged correctly to make <math>\cos C = \dots</math> and numerically correct (possibly unsimplified). Award A1 for any of <math>\cos C = \frac{8^2 + 7^2 - 11^2}{2 \times 8 \times 7}</math> or <math>\cos C = \frac{-8}{112}</math> or <math>\cos C = -\frac{1}{14}</math> or <math>\cos C = \text{awrt } -0.071</math>.  SC: Also allow 1<sup>st</sup> A1 for <math>112\cos C = -8</math> or equivalent.  Also note that the 1<sup>st</sup> A1 can be implied for <math>\hat{C} = \text{awrt } 1.64</math> or <math>\hat{C} = \text{awrt } 94.1^\circ</math>.  <b>Special Case:</b> <math>\cos C = \frac{1}{14}</math> or <math>\cos C = \frac{11^2 - 8^2 - 7^2}{2 \times 8 \times 7}</math> scores a SC: M1A0A0.  2<sup>nd</sup> A1: for awrt 1.64 <b>cao</b>  <b>Note that</b> <math>A = 0.6876\dots^\circ</math> (or <math>39.401\dots^\circ</math>), <math>B = 0.8116\dots^\circ</math> (or <math>46.503\dots^\circ</math>)</p>	
	<p>(b) M1: alternative methods must be fully correct to score the M1.  For any (or both) of the M1 or the 1<sup>st</sup> A1; their <math>C</math> can either be in degrees or radians.  Candidates who use <math>\cos C = \frac{1}{14}</math> to give <math>C = 1.499\dots</math>, can achieve the correct answer of awrt 27.9 in part (b). These candidates will score M1A1A0cso, in part (b).  Finding <math>C = 1.499\dots</math> in part (a) and achieving awrt 27.9 with no working scores M1A1A0.  Otherwise with no working in part (b), awrt 27.9 scores M1A1A1.  <b>Special Case: If the candidate gives awrt 27.9 from any of the below then award M1A1A1.</b>  <math>\frac{1}{2}(7 \times 11)\sin(0.8116^\circ \text{ or } 46.503^\circ) = \text{awrt } 27.9</math>, <math>\frac{1}{2}(8 \times 11)\sin(0.6876\dots^\circ \text{ or } 39.401\dots^\circ) = \text{awrt } 27.9</math>.  <b>Alternative: Hero's Formula:</b> <math>A = \sqrt{13(13-11)(13-8)(13-7)} = \text{awrt } 27.9</math>, where M1 is attempt to apply <math>A = \sqrt{s(s-11)(s-8)(s-7)}</math> and the first A1 is for the correct application of the formula.</p>	

Question Number	Scheme	Marks
3. (a)	$ar = 750$ and $ar^4 = -6$ (could be implied from later working in either (a) or (b)). $r^3 = \frac{-6}{750}$ $r = -\frac{1}{5}$	B1 M1 A1 Correct answer from no working, except for special case below gains all three marks. (3)
(b)	$a(-0.2) = 750$ $a \left\{ = \frac{750}{-0.2} \right\} = -3750$	M1 A1 ft (2)
(c)	Applies $\frac{a}{1-r}$ correctly using both their $a$ and their $ r  < 1$ . Eg. $\frac{-3750}{1--0.2}$ So, $S_{\infty} = -3125$	M1 A1 (2) <b>[7]</b>
<b>Notes</b>		
(a)	B1: for both $ar = 750$ and $ar^4 = -6$ (may be implied from later working in either (a) or (b)). M1: <b>for eliminating <math>a</math></b> by either dividing $ar^4 = -6$ by $ar = 750$ or dividing $ar = 750$ by $ar^4 = -6$ , to achieve an equation in $r^3$ or $\frac{1}{r^3}$ . Note that $r^4 - r = -\frac{6}{750}$ is M0. Note also that any of $r^3 = \frac{-6}{750}$ or $r^3 = \frac{750}{-6} \{ = -125 \}$ or $\frac{1}{r^3} = \frac{-6}{750}$ or $\frac{1}{r^3} = \frac{750}{-6} \{ = -125 \}$ are fine for the award of M1. SC: $ar^{\alpha} = 750$ and $ar^{\beta} = -6$ leading to $r^{\delta} = \frac{-6}{750}$ or $r^{\delta} = \frac{750}{-6} \{ = -125 \}$ or $\frac{1}{r^{\delta}} = \frac{-6}{750}$ or $\frac{1}{r^{\delta}} = \frac{750}{-6} \{ = -125 \}$ where $\delta = \beta - \alpha$ and $\delta \geq 2$ are fine for the award of M1. SC: $ar^2 = 750$ and $ar^5 = -6$ leading to $r = -\frac{1}{5}$ scores B0M1A1.	
(b)	M1 for inserting their $r$ into either of their original correct equations of either $ar = 750$ or $\{a = \} \frac{750}{r}$ or $ar^4 = -6$ or $\{a = \} \frac{-6}{r^4}$ – <b>in both <math>a</math> and <math>r</math></b> . No slips allowed here for M1. A1 for either $a = -3750$ or $a$ equal to the correct follow through result expressed either as an exact integer, or a fraction in the form $\frac{c}{d}$ where both $c$ and $d$ are integers, or correct to awrt 1 dp.	
(c)	M1 for applying $\frac{a}{1-r}$ correctly (only a slip in substituting $r$ is allowed) using both their $a$ and their $ r  < 1$ . Eg. $\frac{-3750}{1--0.2}$ . A1 for $-3125$ In parts (a) or (b) or (c), the correct answer with no working scores full marks.	

Question Number	Scheme	Marks
4.	(a) Seeing $-1$ and $5$ . (See note below.)	B1 (1)
(b)	$(x + 1)(x - 5) = \underline{x^2 - 4x - 5}$ or $\underline{x^2 - 5x + x - 5}$ $\int (x^2 - 4x - 5) dx = \frac{x^3}{3} - \frac{4x^2}{2} - 5x \{+ c\}$ $\left[ \frac{x^3}{3} - \frac{4x^2}{2} - 5x \right]_{-1}^5 = (\dots) - (\dots)$ $\left\{ \left( \frac{125}{3} - \frac{100}{2} - 25 \right) - \left( -\frac{1}{3} - 2 + 5 \right) \right\}$ $\left\{ = \left( -\frac{100}{3} \right) - \left( \frac{8}{3} \right) = -36 \right\}$ Hence, Area = 36	B1 M1A1ft A1 dM1 A1 Final answer must be 36, not $-36$ (6) [7]
<b>Notes</b>		
(a)	B1: for $-1$ and $5$ . Note that $(-1, 0)$ and $(5, 0)$ are acceptable for B1. Also allow $(0, -1)$ and $(0, 5)$ generously for B1. Note that if a candidate writes down that $A: (5, 0)$ , $B: (-1, 0)$ , (ie $A$ and $B$ interchanged,) then B0. Also allow values inserted in the correct position on the $x$ -axis of the graph.	
(b)	B1 for $x^2 - 4x - 5$ or $x^2 - 5x + x - 5$ . If you believe that the candidate is applying the Way 2 method then $-x^2 + 4x + 5$ or $-x^2 + 5x - x + 5$ would then be fine for B1. 1 <sup>st</sup> M1 for an attempt to integrate meaning that $x^n \rightarrow x^{n+1}$ for at least one of the terms. Note that $-5 \rightarrow 5x$ is sufficient for M1. 1 <sup>st</sup> A1 at least two out of three terms correctly ft from their multiplied out brackets. 2 <sup>nd</sup> A1 for correct integration only and no follow through. Ignore the use of a '+c'. Allow 2 <sup>nd</sup> A1 also for $\frac{x^3}{3} - \frac{5x^2}{2} + \frac{x^2}{2} - 5x$ . Note that $-\frac{5x^2}{2} + \frac{x^2}{2}$ only counts as one integrated term for the 1 <sup>st</sup> A1 mark. Do not allow any extra terms for the 2 <sup>nd</sup> A1 mark. 2 <sup>nd</sup> M1: Note that this method mark is dependent upon the award of the first M1 mark in part (b). Substitutes $5$ and $-1$ (and not $1$ if the candidate has stated $x = -1$ in part (a).) (or the limits the candidate has found from part(a)) into an "integrated function" and subtracts, either way round. 3 <sup>rd</sup> A1: For a final answer of $36$ , not $-36$ .  <b>Note:</b> An alternative method exists where the candidate states from the outset that Area ( $R$ ) = $-\int_{-1}^5 (x^2 - 4x + 5) dx$ is detailed in the Appendix.	

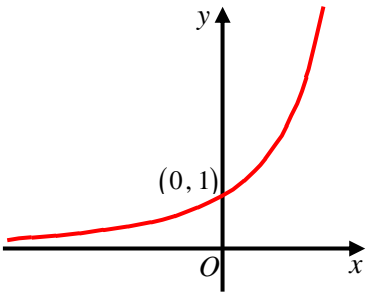
Question Number	Scheme	Marks
5.  (a)	$\binom{40}{4} = \frac{40!}{4!b!}$ ; $(1+x)^n$ coefficients of $x^4$ and $x^5$ are $p$ and $q$ respectively. $b = 36$ Candidates should usually “identify” two terms as their $p$ and $q$ respectively.	B1  (1)
(b)	Term 1: $\binom{40}{4}$ or ${}^{40}C_4$ or $\frac{40!}{4!36!}$ or $\frac{40(39)(38)(37)}{4!}$ or 91390  Term 2: $\binom{40}{5}$ or ${}^{40}C_5$ or $\frac{40!}{5!35!}$ or $\frac{40(39)(38)(37)(36)}{5!}$ or 658008  Hence, $\frac{q}{p} = \frac{658008}{91390} \left\{ = \frac{36}{5} = 7.2 \right\}$	Any one of Term 1 or Term 2 correct. (Ignore the label of $p$ and/or $q$ .) Both of them correct. (Ignore the label of $p$ and/or $q$ .) for $\frac{658008}{91390}$ oe  M1  A1  A1 oe cso  (3) [4]
<b>Notes</b>		
(a)	B1: for only $b = 36$ .	
(b)	The candidate may expand out their binomial series. At this stage no marks should be awarded until they start to identify either one or both of the terms that they want to focus on. Once they identify their terms then if one out of two of them (ignoring which one is $p$ and which one is $q$ ) is correct then award M1. If both of the terms are identified correctly (ignoring which one is $p$ and which one is $q$ ) then award the first A1.  Term 1 = $\binom{40}{4}x^4$ or ${}^{40}C_4(x^4)$ or $\frac{40!}{4!36!}x^4$ or $\frac{40(39)(38)(37)}{4!}x^4$ or $91390x^4$ ,  Term 2 = $\binom{40}{5}x^5$ or ${}^{40}C_5(x^5)$ or $\frac{40!}{5!35!}x^5$ or $\frac{40(39)(38)(37)(36)}{5!}x^5$ or $658008x^5$  are fine for any (or both) of the first two marks in part (b).  2 <sup>nd</sup> A1 for stating $\frac{q}{p}$ as $\frac{658008}{91390}$ or equivalent. Note that $\frac{q}{p}$ must be independent of $x$ .  Also note that $\frac{36}{5}$ or 7.2 or any equivalent fraction is fine for the 2 <sup>nd</sup> A1 mark.  SC: If candidate states $\frac{p}{q} = \frac{5}{36}$ , then award M1A1A0.  Note that either $\frac{4!36!}{5!35!}$ or $\frac{5!35!}{4!36!}$ would be awarded M1A1.	



Question Number	Scheme	Marks
<p>6.</p> <p>(a)</p>	$\begin{array}{c c c c c c} x & 2 & 2.25 & 2.5 & 2.75 & 3 \\ \hline y & 0.5 & 0.38 & 0.298507\dots & 0.241691\dots & 0.2 \end{array}$ <p>At <math>\{x = 2.5,\}</math> <math>y = 0.30</math> (only)</p> <p>At <math>\{x = 2.75,\}</math> <math>y = 0.24</math> (only)</p>	<p>At least one y-ordinate correct. B1</p> <p>Both y-ordinates correct. B1</p> <p>(2)</p>
<p>(b)</p>	$\frac{1}{2} \times 0.25 ; \times \{ 0.5 + 0.2 + 2(0.38 + \text{their } 0.30 + \text{their } 0.24) \}$ $\{ = \frac{1}{8}(2.54) \} = \text{awrt } 0.32$	<p>Outside brackets <math>\frac{1}{2} \times 0.25</math> or <math>\frac{1}{8}</math> B1 aef</p> <p>For structure of <math>\{ \dots \}</math>; M1</p> <p>Correct expression <u>inside brackets</u> which all must be multiplied by their “outside constant”. <math>A1 \sqrt{\quad}</math></p> <p>awrt 0.32 A1</p> <p>(4)</p>
<p>(c)</p>	<p>Area of triangle <math>= \frac{1}{2} \times 1 \times 0.2 = 0.1</math></p> <p>Area(S) = "0.3175" - 0.1</p> <p><math>= 0.2175</math></p>	<p>B1</p> <p>M1</p> <p>A1 ft</p> <p>(3)</p> <p>[9]</p>

Question Number	Scheme	Marks
<b>Notes</b>		
(b)	<p>B1 for using <math>\frac{1}{2} \times 0.25</math> or <math>\frac{1}{8}</math> or equivalent.</p> <p>M1 requires the correct {...} bracket structure. This is for the first bracket to contain first y-ordinate plus last y-ordinate and the second bracket to be the summation of the remaining y-ordinates in the table.</p> <p>No errors (eg. an omission of a y-ordinate or an extra y-ordinate or a repeated y-ordinate) are allowed in the second bracket and the second bracket must be multiplied by 2. Only one copying error is allowed here in the <math>2(0.38 + \text{their } 0.30 + \text{their } 0.24)</math> bracket.</p> <p>A1ft for the correct bracket {...} following through candidate's y-ordinates found in part (a).</p> <p>A1 for answer of awrt 0.32 .</p> <p><b>Bracketing mistake: Unless the final answer implies that the calculation has been done correctly</b></p> <p>then award M1A0A0 for either <math>\frac{1}{2} \times 0.25 \times 0.5 + 2(0.38 + \text{their } 0.30 + \text{their } 0.24) + 0.2</math></p> <p>(nb: yielding final answer of 2.1025) so that the 0.5 is only multiplied by <math>\frac{1}{2} \times 0.25</math></p> <p>or <math>\frac{1}{2} \times 0.25 \times (0.5 + 0.2) + 2(0.38 + \text{their } 0.30 + \text{their } 0.24)</math></p> <p>(nb: yielding final answer of 1.9275) so that the <math>(0.5 + 0.2)</math> is multiplied by <math>\frac{1}{2} \times 0.25</math>.</p> <p><b>Need to see trapezium rule – answer only (with no working) gains no marks.</b></p> <p><b>Alternative:</b> Separate trapezia may be used, and this can be marked equivalently. (See appendix.)</p>	
(c)	<p>B1 for the area of the triangle identified as either <math>\frac{1}{2} \times 1 \times 0.2</math> or 0.1. May be identified on the diagram.</p> <p>M1 for “part (b) answer” – “0.1 only” or “part (b) answer – their attempt at 0.1 only”. (Strict attempt!)</p> <p>A1ft for correctly following through “part (b) answer” – 0.1. This is also dependent on the answer to (b) being greater than 0.1. Note: candidates may round answers here, so allow A1ft if they round their answer correct to 2 dp.</p>	

Question Number	Scheme	Marks
7. (a)	$3\sin^2 x + 7\sin x = \cos^2 x - 4; 0 \leq x < 360^\circ$ $3\sin^2 x + 7\sin x = (1 - \sin^2 x) - 4$ $4\sin^2 x + 7\sin x + 3 = 0$ <b>AG</b>	M1 A1 * cso (2)
(b)	$(4\sin x + 3)(\sin x + 1) \{= 0\}$ $\sin x = -\frac{3}{4}, \sin x = -1$ $( \alpha  = 48.59\dots)$ $x = 180 + 48.59$ or $x = 360 - 48.59$ $x = 228.59\dots, x = 311.41\dots$ $\{\sin x = -1\} \Rightarrow x = 270$	Valid attempt at factorisation and $\sin x = \dots$ M1 Both $\sin x = -\frac{3}{4}$ and $\sin x = -1$ . A1 Either $(180 +  \alpha )$ or $(360 -  \alpha )$ dM1 Both awrt 228.6 and awrt 311.4 A1 270 B1 (5) [7]
<b>Notes</b>		
(a)	M1 for a correct method to change $\cos^2 x$ into $\sin^2 x$ (must use $\cos^2 x = 1 - \sin^2 x$ ). Note that applying $\cos^2 x = \sin^2 x - 1$ , scores M0. A1 for obtaining the printed answer without error (except for implied use of zero.), although the equation at the end of the proof <b>must be = 0</b> . Solution <b>just</b> written only as above would score M1A1.	
(b)	1 <sup>st</sup> M1 for a valid attempt at factorisation, can use any variable here, $s, y, x$ or $\sin x$ , and an attempt to find at least one of the solutions. <i>Alternatively</i> , using a correct formula for solving the quadratic. Either the formula must be stated correctly or the correct form must be implied by the substitution. 1 <sup>st</sup> A1 for the two correct values of $\sin x$ . If they have used a substitution, a correct value of their $s$ or their $y$ or their $x$ . 2 <sup>nd</sup> M1 for solving $\sin x = -k, 0 < k < 1$ and realising a solution is either of the form $(180 +  \alpha )$ or $(360 -  \alpha )$ where $\alpha = \sin^{-1}(k)$ . Note that you <b>cannot</b> access this mark from $\sin x = -1 \Rightarrow x = 270$ . Note that this mark is dependent upon the 1 <sup>st</sup> M1 mark awarded. 2 <sup>nd</sup> A1 for both awrt 228.6 and awrt 311.4 B1 for 270. If there are any EXTRA solutions inside the range $0 \leq x < 360^\circ$ and the candidate would otherwise score FULL MARKS then withhold the final bA2 mark (the fourth mark in this part of the question). Also ignore EXTRA solutions outside the range $0 \leq x < 360^\circ$ . <b>Working in Radians:</b> Note the answers in radians are $x = 3.9896\dots, 5.4351\dots, 4.7123\dots$ If a candidate works in radians then mark part (b) as above awarding the 2 <sup>nd</sup> A1 for both awrt 4.0 and awrt 5.4 and the B1 for awrt 4.7 or $\frac{3\pi}{2}$ . If the candidate would then score FULL MARKS then withhold the final bA2 mark (the fourth mark in this part of the question.) <b>No working:</b> Award B1 for 270 seen without any working. Award M0A0M1A1 for awrt 228.6 and awrt 311.4 seen without any working. Award M0A0M1A0 for any one of awrt 228.6 or awrt 311.4 seen without any working.	

Question Number	Scheme	Marks
8.	<p>(a) Graph of <math>y = 7^x</math>, <math>x \in \mathbb{R}</math> and solving <math>7^{2x} - 4(7^x) + 3 = 0</math></p>  <p style="text-align: right;">At least two of the three criteria correct. (See notes below.) All three criteria correct. (See notes below.)</p>	<p>B1 B1 (2)</p>
(b)	$y^2 - 4y + 3 \{= 0\}$ $\{(y - 3)(y - 1) = 0 \text{ or } (7^x - 3)(7^x - 1) = 0\}$ $y = 3, y = 1 \text{ or } 7^x = 3, 7^x = 1$ $\{7^x = 3 \Rightarrow\} x \log 7 = \log 3$ $\text{or } x = \frac{\log 3}{\log 7} \text{ or } x = \log_7 3$ $x = 0.5645\dots$ $x = 0$	<p>Forming a quadratic {using "y" = 7^x}.</p> $y^2 - 4y + 3 \{= 0\}$ <p>Both <math>y = 3</math> and <math>y = 1</math>.</p> <p>A valid method for solving <math>7^x = k</math> where <math>k &gt; 0, k \neq 1</math></p> <p>0.565 or awrt 0.56 <math>x = 0</math> stated as a solution.</p> <p>M1 A1 A1 dM1 A1 B1 (6) [8]</p>
<b>Notes</b>		
(a)	<p>B1B0: Any two of the following three criteria below correct. B1B1: All three criteria correct. Criteria number 1: Correct shape of curve for <math>x \geq 0</math>. Criteria number 2: Correct shape of curve for <math>x &lt; 0</math>. Criteria number 3: (0, 1) stated or 1 marked on the y-axis. Allow (1, 0) rather than (0, 1) if marked in the "correct" place on the y-axis.</p>	

Question Number	Scheme	Marks
(b)	<p>1<sup>st</sup> M1 is an attempt to form a quadratic equation {using "y" = 7<sup>x</sup>. }</p> <p>1<sup>st</sup> A1 mark is for the correct quadratic equation of <math>y^2 - 4y + 3 \{= 0\}</math>.</p> <p>Can use any variable here, eg: <math>y, x</math> or <math>7^x</math>. Allow M1A1 for <math>x^2 - 4x + 3 \{= 0\}</math>.</p> <p>Writing <math>(7^x)^2 - 4(7^x) + 3 = 0</math> is also sufficient for M1A1.</p> <p>Award M0A0 for seeing <math>7^{x^2} - 4(7^x) + 3 = 0</math> by itself without seeing <math>y^2 - 4y + 3 \{= 0\}</math> or <math>(7^x)^2 - 4(7^x) + 3 = 0</math>.</p> <p>1<sup>st</sup> A1 mark for both <math>y = 3</math> and <math>y = 1</math> or both <math>7^x = 3</math> and <math>7^x = 1</math>. Do not give this accuracy mark for both <math>x = 3</math> and <math>x = 1</math>, unless these are recovered in later working by candidate applying logarithms on these.</p> <p>Award M1A1A1 for <math>7^x = 3</math> and <math>7^x = 1</math> written down with no earlier working.</p> <p>3<sup>rd</sup> dM1 for solving <math>7^x = k, k &gt; 0, k \neq 1</math> to give either <math>x \ln 7 = \ln k</math> or <math>x = \frac{\ln k}{\ln 7}</math> or <math>x = \log_7 k</math>.</p> <p>dM1 is dependent upon the award of M1.</p> <p>2<sup>nd</sup> A1 for 0.565 or awrt 0.56. B1 is for the solution of <math>x = 0</math>, from <i>any</i> working.</p>	

Question Number	Scheme	Marks
9.	<p>(a) <math>C\left(\frac{-2+8}{2}, \frac{11+1}{2}\right) = C(3, 6)</math> <b>AG</b> Correct method (no errors) for finding the mid-point of <math>AB</math> giving <math>(3, 6)</math></p> <p>(b) <math>(8-3)^2 + (1-6)^2</math> or <math>\sqrt{(8-3)^2 + (1-6)^2}</math> or <math>(-2-3)^2 + (11-6)^2</math> or <math>\sqrt{(-2-3)^2 + (11-6)^2}</math> Applies distance formula in order to find the radius. Correct application of formula. <math>(x \pm 3)^2 + (y \pm 6)^2 = k</math>, <math>k</math> is a positive <u>value</u>. <math>(x-3)^2 + (y-6)^2 = 50</math> (Not <math>7.07^2</math>)</p> <p>(c) {For <math>(10, 7)</math>, } <math>\underline{(10-3)^2 + (7-6)^2 = 50}</math>, {so the point lies on <math>C</math>.}</p> <p>(d) {Gradient of radius } = <math>\frac{7-6}{10-3}</math> or <math>\frac{1}{7}</math> This must be seen in part (d). Gradient of tangent = <math>\frac{-7}{1}</math> Using a perpendicular gradient method. <math>y-7 = -7(x-10)</math> <math>y-7 = (\text{their gradient})(x-10)</math> <math>y = -7x + 77</math> <math>y = -7x + 77</math> or <math>y = 77 - 7x</math></p>	<p>B1* (1)</p> <p>M1 A1 M1 A1 (4)</p> <p><u>B1</u> (1)</p> <p>B1 M1 M1 A1 cao (4) <b>[10]</b></p>
<b>Notes</b>		
(a)	Alternative method: $C\left(-2 + \frac{8-2}{2}, 11 + \frac{1-11}{2}\right)$ or $C\left(8 + \frac{-2-8}{2}, 1 + \frac{11-1}{2}\right)$	
(b)	<p>You need to be convinced that the candidate is attempting to work out the radius and not the diameter of the circle to award the first M1. Therefore allow 1<sup>st</sup> M1 generously for <math>\frac{(-2-8)^2 + (11-1)^2}{2}</math></p> <p>Award 1<sup>st</sup> M1A1 for <math>\frac{(-2-8)^2 + (11-1)^2}{4}</math> or <math>\frac{\sqrt{(-2-8)^2 + (11-1)^2}}{2}</math>.</p> <p>Correct answer in (b) with no working scores full marks.</p>	
(c)	<p>B1 awarded for correct verification of <math>\underline{(10-3)^2 + (7-6)^2 = 50}</math> with no errors.</p> <p>Also to gain this mark candidates need to have the correct equation of the circle either from part (b) or re-attempted in part (c). They cannot verify <math>(10, 7)</math> lies on <math>C</math> without a correct <math>C</math>. Also a candidate could either substitute <math>x = 10</math> in <math>C</math> to find <math>y = 7</math> or substitute <math>y = 7</math> in <math>C</math> to find <math>x = 10</math>.</p>	

Question Number	Scheme	Marks
(d)	<p>2<sup>nd</sup> M1 mark also for the complete method of applying <math>7 = (\text{their gradient})(10) + c</math>, finding <math>c</math>.  <b>Note:</b> Award 2<sup>nd</sup> M0 in (d) if their numerical gradient is either 0 or <math>\infty</math>.</p> <p><b>Alternative:</b> For first two marks (differentiation):  <math>2(x - 3) + 2(y - 6)\frac{dy}{dx} = 0</math> (or equivalent) scores B1.</p> <p>1<sup>st</sup> M1 for substituting <b>both</b> <math>x = 10</math> and <math>y = 7</math> to find a value for <math>\frac{dy}{dx}</math>, which must contain both <math>x</math> and <math>y</math>. (This M mark can be awarded generously, even if the attempted “differentiation” is not “implicit”.)  <b>Alternative:</b> <math>(10 - 3)(x - 3) + (7 - 6)(y - 6) = 50</math> scores B1M1M1 which leads to  <math>y = -7x + 77</math>.</p>	

Question Number	Scheme	Marks
10. (a)	$V = 4x(5 - x)^2 = 4x(25 - 10x + x^2)$ So, $V = 100x - 40x^2 + 4x^3$ $\frac{dV}{dx} = 100 - 80x + 12x^2$	$\pm \alpha x \pm \beta x^2 \pm \gamma x^3$ , where $\alpha, \beta, \gamma \neq 0$ $V = 100x - 40x^2 + 4x^3$ At least two of their expanded terms differentiated correctly. $100 - 80x + 12x^2$ M1 A1 M1 A1 cao (4)
(b)	$100 - 80x + 12x^2 = 0$ $\{\Rightarrow 4(3x^2 - 20x + 25) = 0 \Rightarrow 4(3x - 5)(x - 5) = 0\}$ $\{\text{As } 0 < x < 5\} x = \frac{5}{3}$ $x = \frac{5}{3}, V = 4\left(\frac{5}{3}\right)\left(5 - \frac{5}{3}\right)^2$ So, $V = \frac{2000}{27} = 74\frac{2}{27} = 74.074\dots$	Sets their $\frac{dV}{dx}$ from part (a) = 0 $x = \frac{5}{3}$ or $x = \text{awrt } 1.67$ Substitute candidate's value of $x$ <b>where</b> $0 < x < 5$ into a formula for $V$ . Either $\frac{2000}{27}$ or $74\frac{2}{27}$ or awrt 74.1 M1 A1 dM1 A1 (4)
(c)	$\frac{d^2V}{dx^2} = -80 + 24x$ When $x = \frac{5}{3}, \frac{d^2V}{dx^2} = -80 + 24\left(\frac{5}{3}\right)$ $\frac{d^2V}{dx^2} = -40 < 0 \Rightarrow V$ is a maximum	Differentiates their $\frac{dV}{dx}$ <b>correctly</b> to give $\frac{d^2V}{dx^2}$ . $\frac{d^2V}{dx^2} = -40$ and <u>&lt; 0 or negative</u> and <u>maximum</u> . M1 A1 cso (2) [10]
<b>Notes</b>		
(a)	$1^{\text{st}}$ M1 for a three term cubic in the form $\pm \alpha x \pm \beta x^2 \pm \gamma x^3$ . Note that an un-combined $\pm \alpha x \pm \lambda x^2 \pm \mu x^2 \pm \gamma x^3$ , $\alpha, \lambda, \mu, \gamma \neq 0$ is fine for the $1^{\text{st}}$ M1. $1^{\text{st}}$ A1 for either $100x - 40x^2 + 4x^3$ or $100x - 20x^2 - 20x^2 + 4x^3$ . $2^{\text{nd}}$ M1 for any two of their expanded terms differentiated correctly. NB: If expanded expression is divided by a constant, then the $2^{\text{nd}}$ M1 can be awarded for at least two terms are correct. Note for un-combined $\pm \lambda x^2 \pm \mu x^2, \pm 2\lambda x \pm 2\mu x$ counts as one term differentiated correctly. $2^{\text{nd}}$ A1 for $100 - 80x + 12x^2$ , <b>cao</b> . <b>Note:</b> See appendix for those candidates who apply the product rule of differentiation.	



Question Number	Scheme	Marks
(b)	<p><b>Note you can mark parts (b) and (c) together.</b>            Ignore the extra solution of <math>x = 5</math> (and <math>V = 0</math>). Any extra solutions for <math>V</math> inside found for values inside the range of <math>x</math>, then award the final A0.</p>	
(c)	<p>M1 is for their <math>\frac{dV}{dx}</math> differentiated <b>correctly (follow through)</b> to give <math>\frac{d^2V}{dx^2}</math>.</p> <p>A1 for all three of <math>\frac{d^2V}{dx^2} = -40</math> and <u>&lt; 0 or negative</u> and <u>maximum</u>.</p> <p>Ignore any second derivative testing on <math>x = 5</math> for the final accuracy mark.</p> <p><b><u>Alternative Method: Gradient Test:</u></b> M1 for finding the gradient either side of their <math>x</math>-value from part (b) where <math>0 &lt; x &lt; 5</math>. A1 for <u>both gradients calculated correctly to the near integer, using &gt; 0 and &lt; 0 respectively or a correct sketch and maximum</u>. (See appendix for gradient values.)</p>	

Question Number	Scheme	Marks
<p><i>Aliter</i></p> <p>4 (b) Way 2</p>	$(x + 1)(x - 5) = \underline{x^2 - 4x - 5} \text{ or } \underline{x^2 - 5x + x - 5}$ $- \int (x^2 - 4x - 5) dx = -\frac{x^3}{3} + \frac{4x^2}{2} + 5x \{+ c\}$ $\left[ -\frac{x^3}{3} + \frac{4x^2}{2} + 5x \right]_{-1}^5 = (\dots) - (\dots)$ $\left\{ \left( -\frac{125}{3} + \frac{100}{2} + 25 \right) - \left( \frac{1}{3} + 2 - 5 \right) \right\}$ $\left\{ = \left( \frac{100}{3} \right) - \left( -\frac{8}{3} \right) \right\}$ <p>Hence, Area = 36</p>	<p>Can be implied by later working.</p> <p>M: <math>x^n \rightarrow x^{n+1}</math> for any one term.</p> <p>1<sup>st</sup> A1 any two out of three terms correctly ft.</p> <p>Substitutes 5 and -1 (or limits from part(a)) into an “integrated function” and subtracts, either way round.</p> <p>B1</p> <p>M1A1ft A1</p> <p>dM1</p> <p>A1</p> <p>(6)</p>

Question Number	Scheme	Marks
<p><i>Aliter</i> 6 (b) Way 2</p>	$0.25 \times \left\{ \frac{0.5 + 0.38}{2} + \frac{0.38 + 0.30}{2} + \frac{0.30 + 0.24}{2} + \frac{0.24 + 0.2}{2} \right\}$ <p>which is equivalent to:</p> $\frac{1}{2} \times 0.25 ; \times \left\{ (0.5 + 0.2) + 2(0.38 + \text{their } 0.30 + \text{their } 0.24) \right\}$ $\left\{ = \frac{1}{8}(2.54) \right\} = \text{awrt } 0.32$	<p>0.25 and a divisor of 2 on all terms inside brackets. One of first and last ordinates, two of the middle ordinates inside brackets ignoring the denominator of 2. Correct expression inside brackets if <math>\frac{1}{2}</math> was to be factorised out. awrt 0.32</p> <p>B1 M1 A1 <math>\sqrt{\quad}</math> A1 (4)</p>

Question Number	Scheme	Marks
<p><i>Aliter</i> 10 (a) Way2</p> <p><i>Aliter</i> 10 (a) Way3</p>	<p><b>Product Rule Method:</b></p> $\left\{ \begin{array}{l} u = 4x \qquad v = (5 - x)^2 \\ \frac{du}{dx} = 4 \qquad \frac{dv}{dx} = 2(5 - x)^1(-1) \end{array} \right\}$ $\frac{dy}{dx} = 4(5 - x)^2 + 4x(2)(5 - x)^1(-1)$ $\frac{dy}{dx} = 4(5 - x)^2 - 8x(5 - x)$ $\left\{ \begin{array}{l} u = 4x \qquad v = 25 - 10x + x^2 \\ \frac{du}{dx} = 4 \qquad \frac{dv}{dx} = -10 + 2x \end{array} \right\}$ $\frac{dy}{dx} = 4(25 - 10x + x^2) + 4x(-10 + 2x)$ $\frac{dV}{dx} = 100 - 80x + 12x^2$	<p><math>\pm(\text{their } u')(5 - x)^2 \pm (4x)(\text{their } v')</math> M1</p> <p>A correct attempt at differentiating any one of either <math>u</math> or <math>v</math> correctly. dM1</p> <p>Both <math>\frac{du}{dx}</math> and <math>\frac{dv}{dx}</math> correct A1</p> <p><math>4(5 - x)^2 - 8x(5 - x)</math> A1</p> <p>(4)</p> <p><math>\pm(\text{their } u')(\text{their}(5 - x)^2) \pm (4x)(\text{their } v')</math> M1</p> <p>A correct attempt at differentiating any one of either <math>u</math> or <b>their</b> <math>v</math> correctly. dM1</p> <p>Both <math>\frac{du}{dx}</math> and <math>\frac{dv}{dx}</math> correct A1</p> <p><math>100 - 80x + 12x^2</math> A1</p> <p>(4)</p>
	<p><b>Note:</b> The candidate needs to use a complete product rule method in order for you to award the the first M1 mark here. The second method mark is dependent on the first method mark awarded.</p>	

Question Number	Scheme	Marks																																								
<p><i>Aliter</i></p> <p>10 (c)</p> <p><i>Way 2</i></p>	<p><b>Gradient Test Method:</b></p> $\frac{dV}{dx} = 100 - 80x + 12x^2$ <p><b>Helpful table!</b></p> <table border="1" data-bbox="371 488 616 1290"> <thead> <tr> <th><math>x</math></th> <th><math>\frac{dV}{dx}</math></th> </tr> </thead> <tbody> <tr><td>0.8</td><td>43.68</td></tr> <tr><td>0.9</td><td>37.72</td></tr> <tr><td>1</td><td>32</td></tr> <tr><td>1.1</td><td>26.52</td></tr> <tr><td>1.2</td><td>21.28</td></tr> <tr><td>1.3</td><td>16.28</td></tr> <tr><td>1.4</td><td>11.52</td></tr> <tr><td>1.429</td><td>10.204</td></tr> <tr><td>1.5</td><td>7</td></tr> <tr><td>1.6</td><td>2.72</td></tr> <tr><td>1.7</td><td>-1.32</td></tr> <tr><td>1.8</td><td>-5.12</td></tr> <tr><td>1.9</td><td>-8.68</td></tr> <tr><td>2</td><td>-12</td></tr> <tr><td>2.1</td><td>-15.08</td></tr> <tr><td>2.2</td><td>-17.92</td></tr> <tr><td>2.3</td><td>-20.52</td></tr> <tr><td>2.4</td><td>-22.88</td></tr> <tr><td>2.5</td><td>-25</td></tr> </tbody> </table>	$x$	$\frac{dV}{dx}$	0.8	43.68	0.9	37.72	1	32	1.1	26.52	1.2	21.28	1.3	16.28	1.4	11.52	1.429	10.204	1.5	7	1.6	2.72	1.7	-1.32	1.8	-5.12	1.9	-8.68	2	-12	2.1	-15.08	2.2	-17.92	2.3	-20.52	2.4	-22.88	2.5	-25	
$x$	$\frac{dV}{dx}$																																									
0.8	43.68																																									
0.9	37.72																																									
1	32																																									
1.1	26.52																																									
1.2	21.28																																									
1.3	16.28																																									
1.4	11.52																																									
1.429	10.204																																									
1.5	7																																									
1.6	2.72																																									
1.7	-1.32																																									
1.8	-5.12																																									
1.9	-8.68																																									
2	-12																																									
2.1	-15.08																																									
2.2	-17.92																																									
2.3	-20.52																																									
2.4	-22.88																																									
2.5	-25																																									

Question Number	Scheme	Marks																																																				
8 (b)	<p><b>Method of trial and improvement</b></p> <p><b>Helpful table:</b></p> <table border="1" data-bbox="280 376 632 1451"> <thead> <tr> <th><math>x</math></th> <th><math>y = 7^{2x} - 4(7^x) + 3</math></th> </tr> </thead> <tbody> <tr><td>0</td><td>0</td></tr> <tr><td>0.1</td><td>-0.38348</td></tr> <tr><td>0.2</td><td>-0.72519</td></tr> <tr><td>0.3</td><td>-0.95706</td></tr> <tr><td>0.4</td><td>-0.96835</td></tr> <tr><td>0.5</td><td>-0.58301</td></tr> <tr><td>0.51</td><td>-0.51316</td></tr> <tr><td>0.52</td><td>-0.43638</td></tr> <tr><td>0.53</td><td>-0.3523</td></tr> <tr><td>0.54</td><td>-0.26055</td></tr> <tr><td>0.55</td><td>-0.16074</td></tr> <tr><td>0.56</td><td>-0.05247</td></tr> <tr><td>0.561</td><td>-0.04116</td></tr> <tr><td>0.562</td><td>-0.02976</td></tr> <tr><td>0.563</td><td>-0.01828</td></tr> <tr><td>0.564</td><td>-0.0067</td></tr> <tr><td>0.565</td><td>0.00497</td></tr> <tr><td>0.57</td><td>0.064688</td></tr> <tr><td>0.58</td><td>0.19118</td></tr> <tr><td>0.59</td><td>0.327466</td></tr> <tr><td>0.6</td><td>0.474029</td></tr> <tr><td>0.7</td><td>2.62723</td></tr> <tr><td>0.8</td><td>6.525565</td></tr> <tr><td>0.9</td><td>13.15414</td></tr> <tr><td>1</td><td>24</td></tr> </tbody> </table> <p>For a full method of trial and improvement by trialing  <math>f(\text{value between } 0.1 \text{ and } 0.5645) = \text{value}</math> and <math>f(\text{value between } 0.5645 \text{ and } 1) = \text{value}</math>            Any one of these values correct to 1sf or truncated 1sf.            Both of these values correct to 1sf or truncated 1sf.            A method to confirm root to 2 dp by finding by trialing  <math>f(\text{value between } 0.56 \text{ and } 0.5645) = \text{value}</math> and  <math>f(\text{value between } 0.5645 \text{ and } 0.565) = \text{value}</math>            Both values correct to 1sf or truncated 1sf and the confirmation that the root is  <math>x = 0.56</math> (only)  <math>x = 0</math></p>	$x$	$y = 7^{2x} - 4(7^x) + 3$	0	0	0.1	-0.38348	0.2	-0.72519	0.3	-0.95706	0.4	-0.96835	0.5	-0.58301	0.51	-0.51316	0.52	-0.43638	0.53	-0.3523	0.54	-0.26055	0.55	-0.16074	0.56	-0.05247	0.561	-0.04116	0.562	-0.02976	0.563	-0.01828	0.564	-0.0067	0.565	0.00497	0.57	0.064688	0.58	0.19118	0.59	0.327466	0.6	0.474029	0.7	2.62723	0.8	6.525565	0.9	13.15414	1	24	<p>M1 A1 A1 M1 A1 B1 (6)</p>
$x$	$y = 7^{2x} - 4(7^x) + 3$																																																					
0	0																																																					
0.1	-0.38348																																																					
0.2	-0.72519																																																					
0.3	-0.95706																																																					
0.4	-0.96835																																																					
0.5	-0.58301																																																					
0.51	-0.51316																																																					
0.52	-0.43638																																																					
0.53	-0.3523																																																					
0.54	-0.26055																																																					
0.55	-0.16074																																																					
0.56	-0.05247																																																					
0.561	-0.04116																																																					
0.562	-0.02976																																																					
0.563	-0.01828																																																					
0.564	-0.0067																																																					
0.565	0.00497																																																					
0.57	0.064688																																																					
0.58	0.19118																																																					
0.59	0.327466																																																					
0.6	0.474029																																																					
0.7	2.62723																																																					
0.8	6.525565																																																					
0.9	13.15414																																																					
1	24																																																					
	<p><b>Note:</b> If a candidate goes from <math>7^x = 3</math> with no working to <math>x = 0.5645\dots</math> then give M1A1 implied.</p>																																																					



Further copies of this publication are available from  
Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467

Fax 01623 450481

Email [publications@linneydirect.com](mailto:publications@linneydirect.com)

Order Code US026235 January 2011

For more information on Edexcel qualifications, please visit [www.edexcel.com/quals](http://www.edexcel.com/quals)

Edexcel Limited. Registered in England and Wales no.4496750  
Registered Office: One90 High Holborn, London, WC1V 7BH