

GCE

Edexcel GCE

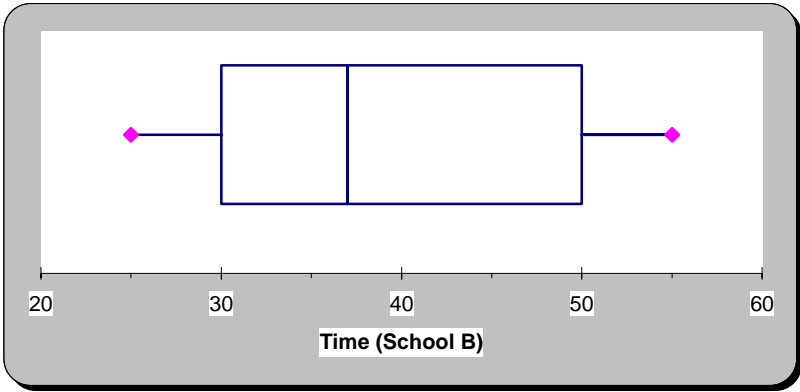
Statistics S1 (6683)

June 2006

advancing learning, changing lives

Mark Scheme
(Results)

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6683 Statistics S1
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Question Number	Scheme	Marks
1(a)	<p>Indicates max / median / min / upper quartile/ lower quartile (2 or more)</p> <p>Indicates outliers (or equivalent description)</p> <p>Illustrates skewness (or equivalent description e.g. shape) Any 3 rows</p> <p>Allows comparisons</p> <p>Indicates range / IQR / spread</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>(3)</p>
(b)(i)	37 (minutes)	B1
(ii)	Upper quartile or Q_3 or third quartile or 75 th percentile or P_{75}	B1
(c)	<p>Outlier s</p> <p>How to calculate correctly</p> <p>‘Observations that are very different from the other observations and need to be treated with caution’</p> <p>These two children probably walked / took a lot longer</p> <p style="text-align: right;">Any 2</p>	<p>B1</p> <p>B1</p> <p>(2)</p>
(d)	 <p style="text-align: right;">Box & median & whiskers Sensible scale 30, 37, 50 25, 55</p>	<p>M1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>(4)</p>
(e)	<p>Children from school A generally took less time Any correct 4 lines</p> <p>50% of B \leq 37 mins, 75% of A < 37 mins (similarly for 30)</p> <p>Median/Q1/Q3 of A < median/Q1/Q3 of B (1 or more)</p> <p>A has outliers, (B does not)</p> <p>Both positive skew</p> <p>IQR of A < IQR of B, range of A > range of B</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>(4)</p> <p>Total 15</p>

Question Number	Scheme	Marks
2. (a)	$P(\text{both longer than 24.5}) = \frac{11}{55} \times \frac{10}{54} = \frac{1}{27} \text{ or } 0.\dot{0}3\dot{7} \text{ or } 0.037 \quad \text{2 fracs x w/o rep.}$ <p style="text-align: right;">awrt 0.037</p>	M1A1
(b)	<p>Estimate of mean time spent on their conversations is</p> $\bar{x} = \frac{1060}{55} = 19\frac{3}{11} \text{ or } 19.\dot{2}\dot{7} \text{ or } 19.3 \quad \text{1060/total, awrt 19.3 or 19mins 16s}$	M1A1
(c)	$\frac{1060 + \sum fy}{80} = 21 \quad \text{21x80=1680}$ $\sum fy = 620 \quad \text{Subtracting 'their 1060'}$ $\therefore \bar{y} = \frac{620}{25} = 24.8 \quad \text{Dividing their 620 by 25}$	B1 M1 M1A1
(d)	<p>Increase in mean value. Length of conversations increased considerably during 25 weeks relative to 55 weeks</p> <p style="text-align: right;">context - ft only from comment above</p>	B1 B1 ∫
		(2)
		Total 10
3. (a)	$\sum x = \sum t = 337.1, \quad \sum y = 16.28 \quad \text{Can be implied}$ $S_{xy} = 757.467 - \frac{337.1 \times 16.28}{8} = 71.4685 \quad \text{either method, awrt 71.5}$ $S_{xx} = 15965.01 - \frac{337.1^2}{8} = 1760.45875 \quad \text{awrt 1760}$	B1, B1 M1A1 A1
(b)	$b = \frac{71.4685}{1760.45875} = 0.04059652 \quad \text{/ correct way up, awrt 0.0406}$ $a = \frac{16.28}{8} - b \times \frac{337.1}{8} = 0.324364 \quad \text{using correct formula, awrt 0.324}$ $y = 0.324 + 0.0406x \quad \text{3 sf or better but award for copying from above}$	M1A1 A1 ∫
(c)	At $t = 40$, $x = 40$, $y = 1.948$, $l = 2461.948$ sub $x=40$, awrt 1.95, awrt 2461.95	M1A1A1 ∫
(d)	$l - 2460 = 0.324 + 0.0406t$ $l = 2460.324 + 0.0406t$ <p style="text-align: right;">LHS required awrt 2460.32, f.t. their 0.0406, / and t</p>	M1
(e)	At $t = 90$, $l = 2463.978$ awrt 2464	B1
(f)	90°C outside range of data unlikely to be reliable	B1

<p>4 (a)</p> <p>(b)</p> <p>M1A1</p> <p>(c)</p>	<p>$E(X) = 3;$</p> <p>$\text{Var}(X) = \frac{25-1}{12} = 2$ **AG**</p> <p>$\text{Var}(X) = 1^2 \times \frac{1}{5} + 2^2 \times \frac{1}{5} + 3^2 \times \frac{1}{5} \dots - 3^2 = 11 - 9 = 2$ **AG**</p> <p>Accept (55/5)-9 as minimum evidence.</p> <p>$E(3X - 2) = 3E(X) - 2 = 7$</p> <p>$\text{Var}(4 - 3x) = 3^2 \text{Var}(X) = 18$</p>	<p>B1</p> <p>M1A1</p> <p>(3)</p> <p>(2)</p> <p>M1A1</p> <p>(2)</p> <p>Total 7</p>
<p>5(a)</p> <p>(b)</p> <p>(c)</p>	<div data-bbox="413 808 1169 1218" data-label="Figure"> </div> <p>2 separate sketches OK.</p> <p>Bell Shape 1.78 & 0.2 1.65 & 0.3</p> <p>Accept clear alternatives to 0.3: 0.7/0.5/0.2</p> <p>$\frac{1.78 - \mu}{\sigma} = 0.8416 \Rightarrow 1.78 - \mu = 0.8416\sigma$ either for method 0.8416</p> <p>$\frac{1.65 - \mu}{\sigma} = -0.5244 \Rightarrow 1.65 - \mu = -0.5244\sigma$ (-)0.5244</p> <p>Solving gives $\mu = 1.70, \sigma = 0.095$ N.B. awrt 0.84, 0.52 B1B0 awrt 1.7, 0.095 cao</p> <p>$P(\text{height} \geq 1.74) = 1 - P(\text{height} < 1.74)$ 'one minus'</p> <p>$= 1 - P\left(Z < \frac{1.74 - 1.70}{0.095}\right)$ standardise with their mu and sigma</p> <p>$= 1 - P(Z < 0.42) = 0.3372$ awrt 0.337</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>(3)</p> <p>M1</p> <p>B1</p> <p>B1</p> <p>M1A1A1</p> <p>(6)</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>(3)</p> <p>Total 12</p>

<p>6.(a)</p>	<div data-bbox="395 215 1217 864" data-label="Figure"> </div> <div data-bbox="866 891 1278 1070" data-label="Text"> <p>3 closed curves that intersect Subtract at either stage 9,7,5 10,6,12 41 & box</p> </div> <div data-bbox="92 1126 132 1164" data-label="Text"> <p>(b)</p> </div> <div data-bbox="387 1111 687 1187" data-label="Equation-Block"> $P(\overline{G}, \overline{LH}, \overline{D}) = \frac{10}{100} = \frac{1}{10}$ </div> <div data-bbox="92 1249 132 1288" data-label="Text"> <p>(c)</p> </div> <div data-bbox="387 1229 624 1305" data-label="Equation-Block"> $P(\overline{G}, \overline{LH}, \overline{D}) = \frac{41}{100}$ </div> <div data-bbox="92 1366 132 1404" data-label="Text"> <p>(d)</p> </div> <div data-bbox="387 1346 868 1422" data-label="Equation-Block"> $P(\text{Only two attributes}) = \frac{9+7+5}{100} = \frac{21}{100}$ </div> <div data-bbox="92 1525 132 1563" data-label="Text"> <p>(e)</p> </div> <div data-bbox="387 1467 1240 1619" data-label="Equation-Block"> $P(G LH \& DH) = \frac{P(G \& LH \& DH)}{P(LH \& DH)} = \frac{\frac{10}{100}}{\frac{15}{100}} = \frac{10}{15} = \frac{2}{3} \quad \text{awrt } 0.667$ </div> <div data-bbox="478 1624 978 1662" data-label="Text"> <p>N.B. Assumption of independence M0</p> </div>	<div data-bbox="1444 891 1500 1104" data-label="Text"> <p>M1 M1 A1 A1 A1 (6)</p> </div> <div data-bbox="1348 1126 1500 1227" data-label="Text"> <p>B1 ∫ (1)</p> </div> <div data-bbox="1348 1249 1500 1350" data-label="Text"> <p>B1 ∫ (1)</p> </div> <div data-bbox="1340 1366 1500 1467" data-label="Text"> <p>M1A1 ∫ (2)</p> </div> <div data-bbox="1348 1525 1500 1731" data-label="Text"> <p>M1A1 ∫ A1 (3) Total 13</p> </div>
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