



1.

$$f(x) = 2x^3 - 7x^2 - 5x + 4$$

(a) Find the remainder when  $f(x)$  is divided by  $(x-1)$ . (2)

(b) Use the factor theorem to show that  $(x+1)$  is a factor of  $f(x)$ . (2)

(c) Factorise  $f(x)$  completely. (4)

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2. (a) Find the first 3 terms, in ascending powers of  $x$ , of the binomial expansion of

$$(3 + bx)^5$$

where  $b$  is a non-zero constant. Give each term in its simplest form.

**(4)**

Given that, in this expansion, the coefficient of  $x^2$  is twice the coefficient of  $x$ ,

(b) find the value of  $b$ .

**(2)**

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4. The circle  $C$  has equation  $x^2 + y^2 + 4x - 2y - 11 = 0$

Find

(a) the coordinates of the centre of  $C$ , (2)

(b) the radius of  $C$ , (2)

(c) the coordinates of the points where  $C$  crosses the  $y$ -axis, giving your answers as simplified surds. (4)

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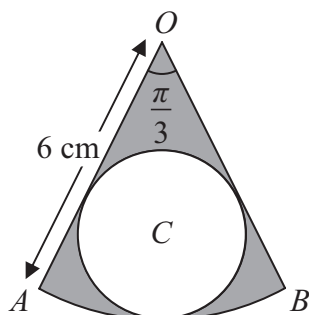
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5.



**Figure 1**

The shape shown in Figure 1 is a pattern for a pendant. It consists of a sector  $OAB$  of a circle centre  $O$ , of radius 6 cm, and angle  $AOB = \frac{\pi}{3}$ . The circle  $C$ , inside the sector, touches the two straight edges,  $OA$  and  $OB$ , and the arc  $AB$  as shown.

Find

(a) the area of the sector  $OAB$ , (2)

(b) the radius of the circle  $C$ . (3)

The region outside the circle  $C$  and inside the sector  $OAB$  is shown shaded in Figure 1.

(c) Find the area of the shaded region. (2)

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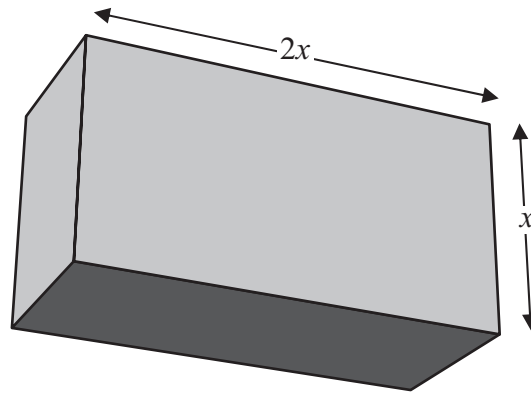








8.



**Figure 2**

A cuboid has a rectangular cross-section where the length of the rectangle is equal to twice its width,  $x$  cm, as shown in Figure 2.

The volume of the cuboid is 81 cubic centimetres.

(a) Show that the total length,  $L$  cm, of the twelve edges of the cuboid is given by

$$L = 12x + \frac{162}{x^2} \tag{3}$$

(b) Use calculus to find the minimum value of  $L$ . (6)

(c) Justify, by further differentiation, that the value of  $L$  that you have found is a minimum. (2)

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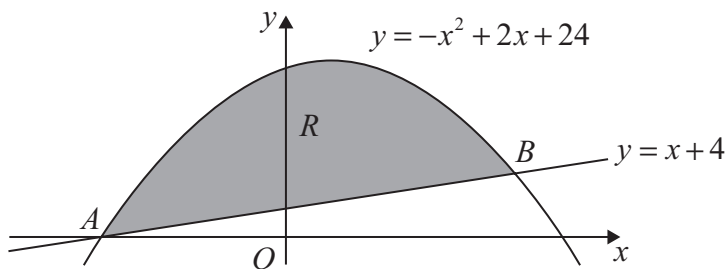
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9.



**Figure 3**

The straight line with equation  $y = x + 4$  cuts the curve with equation  $y = -x^2 + 2x + 24$  at the points  $A$  and  $B$ , as shown in Figure 3.

(a) Use algebra to find the coordinates of the points  $A$  and  $B$ . **(4)**

The finite region  $R$  is bounded by the straight line and the curve and is shown shaded in Figure 3.

(b) Use calculus to find the exact area of  $R$ . **(7)**

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