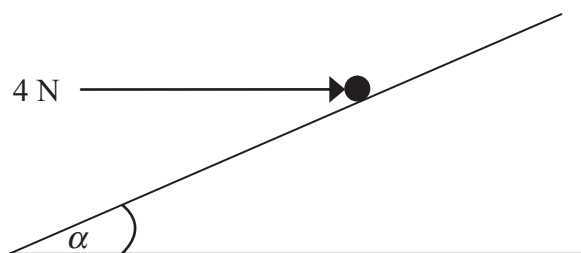








3.



**Figure 1**

A particle of weight  $W$  newtons is held in equilibrium on a rough inclined plane by a horizontal force of magnitude 4 N. The force acts in a vertical plane containing a line of greatest slope of the inclined plane. The plane is inclined to the horizontal at an angle  $\alpha$ , where  $\tan \alpha = \frac{3}{4}$ , as shown in Figure 1.

The coefficient of friction between the particle and the plane is  $\frac{1}{2}$ .

Given that the particle is on the point of sliding down the plane,

- (i) show that the magnitude of the normal reaction between the particle and the plane is 20 N,
- (ii) find the value of  $W$ .

**(9)**

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**Question 3 continued**

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P 3 8 1 6 1 R R A 0 7 2 4

4. A girl runs a 400 m race in a time of 84 s. In a model of this race, it is assumed that, starting from rest, she moves with constant acceleration for 4 s, reaching a speed of  $5 \text{ m s}^{-1}$ . She maintains this speed for 60 s and then moves with constant deceleration for 20 s, crossing the finishing line with a speed of  $V \text{ m s}^{-1}$ .
- (a) Sketch, in the space below, a speed-time graph for the motion of the girl during the whole race. (2)
- (b) Find the distance run by the girl in the first 64 s of the race. (3)
- (c) Find the value of  $V$ . (5)
- (d) Find the deceleration of the girl in the final 20 s of her race. (2)





5. A plank  $PQR$ , of length 8 m and mass 20 kg, is in equilibrium in a horizontal position on two supports at  $P$  and  $Q$ , where  $PQ = 6$  m.

A child of mass 40 kg stands on the plank at a distance of 2 m from  $P$  and a block of mass  $M$  kg is placed on the plank at the end  $R$ . The plank remains horizontal and in equilibrium. The force exerted on the plank by the support at  $P$  is equal to the force exerted on the plank by the support at  $Q$ .

By modelling the plank as a uniform rod, and the child and the block as particles,

- (a) (i) find the magnitude of the force exerted on the plank by the support at  $P$ ,  
 (ii) find the value of  $M$ . (10)
- (b) State how, in your calculations, you have used the fact that the child and the block can be modelled as particles. (1)

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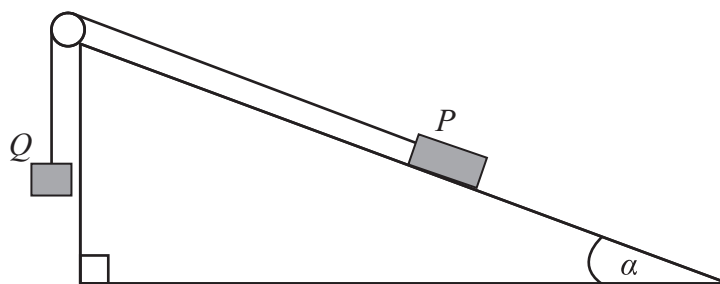


Figure 2

Two particles  $P$  and  $Q$  have masses  $0.3 \text{ kg}$  and  $m \text{ kg}$  respectively. The particles are attached to the ends of a light inextensible string. The string passes over a small smooth pulley which is fixed at the top of a fixed rough plane. The plane is inclined to the horizontal at an angle  $\alpha$ , where  $\tan \alpha = \frac{3}{4}$ . The coefficient of friction between  $P$  and the plane is  $\frac{1}{2}$ .

The string lies in a vertical plane through a line of greatest slope of the inclined plane. The particle  $P$  is held at rest on the inclined plane and the particle  $Q$  hangs freely below the pulley with the string taut, as shown in Figure 2.

The system is released from rest and  $Q$  accelerates vertically downwards at  $1.4 \text{ m s}^{-2}$ . Find

(a) the magnitude of the normal reaction of the inclined plane on  $P$ , (2)

(b) the value of  $m$ . (8)

When the particles have been moving for  $0.5 \text{ s}$ , the string breaks. Assuming that  $P$  does not reach the pulley,

(c) find the further time that elapses until  $P$  comes to instantaneous rest. (6)

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7. [In this question  $\mathbf{i}$  and  $\mathbf{j}$  are unit vectors due east and due north respectively. Position vectors are given relative to a fixed origin  $O$ .]

Two ships  $P$  and  $Q$  are moving with constant velocities. Ship  $P$  moves with velocity  $(2\mathbf{i} - 3\mathbf{j}) \text{ km h}^{-1}$  and ship  $Q$  moves with velocity  $(3\mathbf{i} + 4\mathbf{j}) \text{ km h}^{-1}$ .

(a) Find, to the nearest degree, the bearing on which  $Q$  is moving. (2)

At 2 pm, ship  $P$  is at the point with position vector  $(\mathbf{i} + \mathbf{j}) \text{ km}$  and ship  $Q$  is at the point with position vector  $(-2\mathbf{j}) \text{ km}$ .

At time  $t$  hours after 2 pm, the position vector of  $P$  is  $\mathbf{p} \text{ km}$  and the position vector of  $Q$  is  $\mathbf{q} \text{ km}$ .

(b) Write down expressions, in terms of  $t$ , for

(i)  $\mathbf{p}$ ,

(ii)  $\mathbf{q}$ ,

(iii)  $\overrightarrow{PQ}$ .

(5)

(c) Find the time when

(i)  $Q$  is due north of  $P$ ,

(ii)  $Q$  is north-west of  $P$ .

(4)

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