



**BLANK PAGE**



(a)  $25^{\frac{1}{2}}$

(1)

(b)  $25^{-\frac{3}{2}}$

(2)

**(Total 3 marks)**



2. Given that  $y = 2x^5 + 7 + \frac{1}{x^3}$ ,  $x \neq 0$ , find, in their simplest form,

$$(a) \quad \frac{dy}{dx}, \quad (3)$$

$$(b) \int y \, dx. \tag{4}$$

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

Q2

**(Total 7 marks)**





Q3

**(Total 5 marks)**



4. Solve the simultaneous equations

$$\begin{aligned}x + y &= 2 \\ 4y^2 - x^2 &= 11\end{aligned}$$

(7)





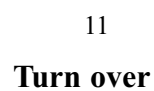
**Q4**

**(Total 7 marks)**





**(Total 7 marks)**

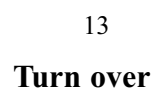


(2)

(5)

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**(Total 7 marks)**



7.

$$f(x) = x^2 + (k+3)x + k$$

where  $k$  is a real constant.

- (a) Find the discriminant of  $f(x)$  in terms of  $k$ .

(2)

- (b) Show that the discriminant of  $f(x)$  can be expressed in the form  $(k+a)^2 + b$ , where  $a$  and  $b$  are integers to be found.

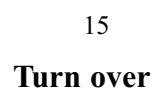
(2)

- (c) Show that, for all values of  $k$ , the equation  $f(x) = 0$  has real roots.

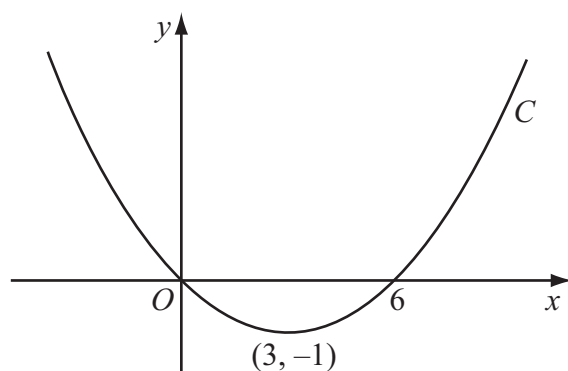
**(2)**

This image shows a full page of blank, lined paper. It features approximately 20 evenly spaced horizontal grey lines across its entire width, providing a template for writing or drawing. The margins are consistent on all sides.

**(Total 6 marks)**



8.



**Figure 1**

Figure 1 shows a sketch of the curve  $C$  with equation  $y = f(x)$ .  
The curve  $C$  passes through the origin and through  $(6, 0)$ .  
The curve  $C$  has a minimum at the point  $(3, -1)$ .

On separate diagrams, sketch the curve with equation

(a)  $y = f(2x)$ , (3)

(b)  $y = -f(x)$ , (3)

(c)  $y = f(x + p)$ , where  $p$  is a constant and  $0 < p < 3$ . (4)

On each diagram show the coordinates of any points where the curve intersects the  $x$ -axis and of any minimum or maximum points.





**Question 8 continued**



**Question 8 continued**



Question 8 continued

Q8

(Total 10 marks)





[illegible]

This image shows a full page of blank, lined paper. It features approximately 28 horizontal grey lines spaced evenly apart, typical of standard notebook paper. The lines extend across the entire width of the page, leaving small margins at the top and bottom. There are no vertical lines, text, or other markings present.

This image shows a full page of blank, lined paper. It features approximately 20 horizontal grey lines spaced evenly apart, typical of notebook paper. The lines extend across the entire width of the page, leaving small margins at the top and bottom. There are no vertical lines, text, or other markings present.

**Q9**



10. The curve  $C$  has equation

$$y = (x+1)(x+3)^2$$

(a) Sketch  $C$ , showing the coordinates of the points at which  $C$  meets the axes. (4)

(b) Show that  $\frac{dy}{dx} = 3x^2 + 14x + 15$ . (3)

The point  $A$ , with  $x$ -coordinate  $-5$ , lies on  $C$ .

(c) Find the equation of the tangent to  $C$  at  $A$ , giving your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are constants. (4)

Another point  $B$  also lies on  $C$ . The tangents to  $C$  at  $A$  and  $B$  are parallel.

(d) Find the  $x$ -coordinate of  $B$ . (3)





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This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

**Question 10 continued**

**(Total 14 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

