

# Mark Scheme (Results)

Summer 2014

Pearson Edexcel GCE in Core Mathematics 2 (6664\_01)



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## **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## **General Instructions for Marking**

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- **\*** The answer is printed on the paper or ag- answer given
- \_\_\_\_ or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

**General Principles for Core Mathematics Marking** 

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

## 1. Factorisation

 $(x^2 + bx + c) = (x + p)(x + q)$ , where |pq| = |c|, leading to  $x = \dots$ 

 $(ax^2 + bx + c) = (mx + p)(nx + q)$ , where |pq| = |c| and |mn| = |a|, leading to x = ...

## 2. Formula

Attempt to use the correct formula (with values for a, b and c).

#### 3. Completing the square

Solving 
$$x^2 + bx + c = 0$$
:  $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0$ ,  $q \neq 0$ , leading to  $x = \dots$ 

#### Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1 ( $x^n \rightarrow x^{n-1}$ )

#### 2. Integration

Power of at least one term increased by 1.  $(x^n \rightarrow x^{n+1})$ 

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

#### Exact answers

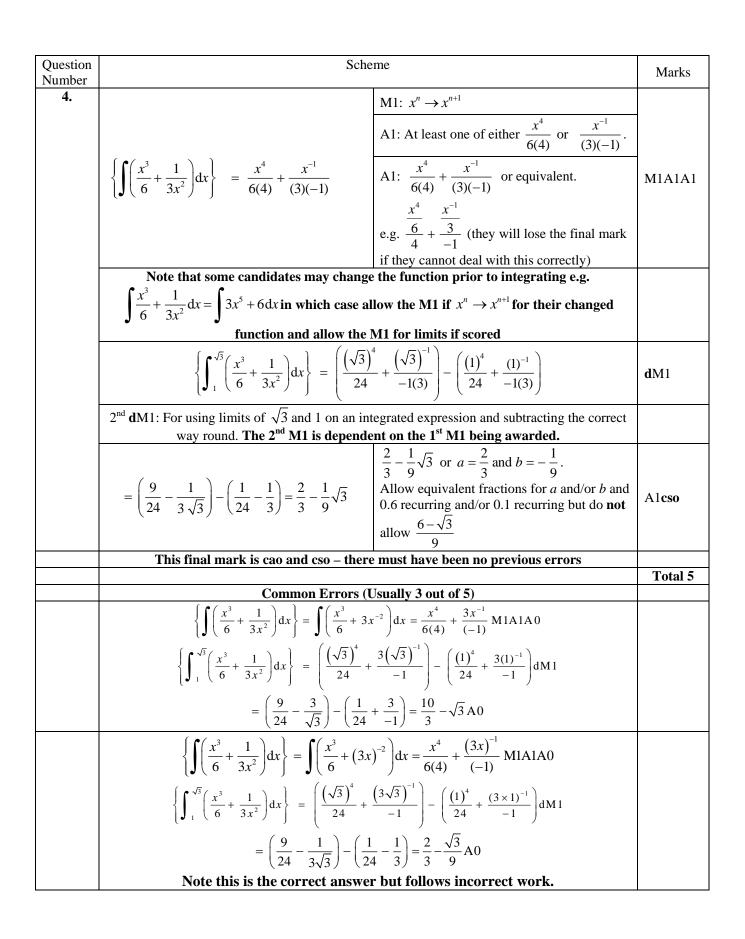
Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Question Number	Scheme			Marks		
110000	x 1	1.25	1.5	1.75	2	
	y 1.414	1.601	1.803	2.016	2.236	
<b>1.</b> (a)	$\{At x = 1.25, \} y = 1.601 \text{ (only)}$ 1.601 (May not be in the table and can score if seen as part of their working in (b))		B1 cao			
					[1]	
	$\frac{1}{2} \times 0.25; \times \frac{\{1.414 + 2.236 + 2(\text{their } 1.601 + 1.803 + 2.016)\}}{(1.414 + 2.236 + 2(\text{their } 1.601 + 1.803 + 2.016))}$			B1; <u>M1 A1ft</u>		
	B1; for using $\frac{1}{2} \times 0.25$ or $\frac{1}{8}$ or equivalent.	<u>M1: Str</u> {	<u>ucture of</u>	as show	r the correct expression rn following through te's y value found in	
( <b>b</b> )	M1 requires the correct structure for the <i>y</i> values. It needs to contain first <i>y</i> value <b>plus</b> last <i>y</i> value and the second bracket to be multiplied by 2 and to be the summation of the remaining <i>y</i> values in the table with no additional values. If the only mistake is a copying error or is to omit one value from 2() bracket this may be regarded as a slip and the M mark can be allowed (nb: an extra repeated term, however, forfeits the M mark). M0 if any values used are <i>x</i> values instead of <i>y</i> values. A1ft: for the correct underlined expression as shown following through candidate's <i>y</i> value found in part (a). Bracketing mistakes: e.g. $\left(\frac{1}{2} \times \frac{1}{4}\right) (1.414 + 2.236) + 2 (\text{their } 1.601 + 1.803 + 2.016) (=11.29625)$ $\left(\frac{1}{2} \times \frac{1}{4}\right) 1.414 + 2.236 + 2 (\text{their } 1.601 + 1.803 + 2.016) (=13.25275)$ Both score B1 M1 A0 unless the final answer implies that the calculation has been done					
	correctly (then full marks could be given).Alternative: Separate trapezia may be used, and this can be marked equivalently. $\left[\frac{1}{8}(1.414+1.601) + \frac{1}{8}(1.601+1.803) + \frac{1}{8}(1.803+2.016) + \frac{1}{8}(2.016+2.236)\right]$ B1 for $\frac{1}{8}$ (aef), M1 for correct structure, 1st A1ft for correct expression, ft their 1.601 $\left\{=\frac{1}{8}(14.49)\right\} = 1.81125$ 1.81 or awrt 1.81Correct answer only in (b) scores no marks					A1
	If required accuracy is not se	en in (a), full	marks can s	still be score	ed in (b) (e.g. uses 1.6)	F 43
						[4] Total 5

Question Number	Scheme		Marks
	If there is no labelling, ma	rk (a) and (b) in that order	
	$f(x) = 2x^3 - $	$7x^2 + 4x + 4$	
	$f(2) = 2(2)^{3} - 7(2)^{2} + 4(2) + 4$	Attempts f(2) or f(-2)	M1
<b>2.</b> (a)	= 0, and so $(x - 2)$ is a factor.	f(2) = 0 with no sign or substitution errors $(2(2)^3 - 7(2)^2 + 4(2) + 4 = 0$ is sufficient) and for conclusion. Stating "hence factor" or "it is a factor" or a "tick" or "QED" or "no	
·	Note: Long division scores no marks in	part (a). The <u>factor theorem</u> is required.	[2]
	$f(x) = \{(x-2)\}(2x^2 - 3x - 2)$	M1: Attempts long division by $(x - 2)$ or other method using $(x - 2)$ , to obtain $(2x^2 \pm ax \pm b)$ , $a \neq 0$ , even with a remainder. Working need not be seen as this could be done "by inspection." A1: $(2x^2 - 3x - 2)$	M1 A1
(b)	$= (x - 2)(x - 2)(2x + 1) \operatorname{or} (x - 2)^{2}(2x + 1)$ or equivalent e.g. $= 2(x - 2)(x - 2)(x + \frac{1}{2}) \operatorname{or} 2(x - 2)^{2}(x + \frac{1}{2})$ Note = $(x - 2)(\frac{1}{2}x - 1)(4x + 2)$ would los	dM1: Factorises a 3 term quadratic. (see rule for factorising a quadratic in the General Principles for Core Maths Marking). This is dependent on the previous method mark being awarded but there must have been no remainder. Allow an attempt to solve the quadratic to determine the factors. A1: cao – needs all three factors on one line. Ignore following work (such as a solution to a quadratic equation.)	<b>d</b> M1 A1
•	Note $= (x - 2)(\frac{1}{2}x - 1)(4x + 2)$ would lose the last mark as it is not <b>fully</b> factorised For correct answers only award full marks in (b)		
	For correct answers only	y award full marks in (b)	[4]
			Total 6

Question Number	Schem	e	Marks
<b>3.</b> (a)	$(2-3x)^6 = 64 + \dots$	64 seen as the only constant term in their expansion.	B1
	$\left\{ (2-3x)^6 \right\} = (2)^6 + \frac{^6C_1}{(2)^5} (-$	$3\underline{x}$ ) + ${}^{6}C_{2}(2)^{4}(-3\underline{x})^{2}$ +	<u>M1</u>
	M1: $({}^{6}C_{1} \times \times x)$ or $({}^{6}C_{2} \times \times x^{2})$ . For <u>either</u>	the <i>x</i> term <u>or</u> the $x^2$ term. Requires <u>correct</u>	
	binomial coefficient in any form with the cor coefficient (perhaps including powers of 2 and/o can be "listed" rather than adde	rect power of $x$ , but the other part of the r $-3$ ) may be wrong or missing. The terms d. Ignore any extra terms.	
	${}^{6}C_{1}2^{5}-3x+{}^{6}C_{2}2^{4}-3x^{2}+$ Scores M0 unless later work implies a correct method		
	$= 64 - 576x + 2160x^2 +$	A1: Either $-576x$ or $2160x^{2}$ (Allow + $-576x$ here)	A 1 A 1
	$= 64 - 5/6x + 2160x + \dots$	A1: Both $-576x$ and $2160x^2$ (Do not allow $+ -576x$ here)	- A1A1
			[
(a) Way 2	$(2-3x)^6 = 64 + \dots$	64 seen as the only constant term in their expansion.	B1
	$\left(1 - \frac{3}{2}x\right)^{6} = 1 + \frac{{}^{6}C_{1}\left(\frac{-3}{2}\underline{x}\right)}{-3} + \frac{{}^{6}C_{2}\left(\frac{-3}{2}\underline{x}\right)^{2}}{-3} + \dots$	$\left(\frac{-3}{2}\underline{x}\right) + \frac{{}^{6}C_{2}}{\left(\frac{-3}{2}\underline{x}\right)^{2}} + \dots \begin{pmatrix} M1: \left({}^{6}C_{1} \times \dots \times x\right) \text{ or } \left({}^{6}C_{2} \times \dots \times x^{2}\right). \text{ For } \\ \frac{\text{either the } x \text{ term } \underline{\text{or the } x^{2} \text{ term. Requires }} \\ \frac{\text{correct binomial coefficient in any form } \\ \frac{\text{with the correct power of } x, \text{ but the other } \\ \text{part of the coefficient (perhaps including } \\ \text{powers of } 2 \text{ and/or } -3) \text{ may be wrong or } \\ \text{missing. The terms can be "listed" rather } \\ \text{than added. Ignore any extra terms.} \end{cases}$	
	$= 64 - 576x + 2160x^2 + \dots$	A1: Either $-576x$ or $2160x^{2}$ (Allow + $-576x$ here) A1: Both $-576x$ and $2160x^{2}$ (Do not allow + $-576x$ here)	- A1A1
(b)	Candidate writes down $\left(1+\frac{x}{x}\right)$ (their part	(a) answer at least up to the term in $r$ )	
	Candidate writes down $\left(1 + \frac{x}{2}\right) \times \left(\text{their part (a) answer, at least up to the term in } x\right).$		
	(Condone missing brackets) $\left(1+\frac{x}{2}\right)(64-576x+) \text{ or } \left(1+\frac{x}{2}\right)(64-576x+2160x^2+) \text{ or }$		M1
	$\left(1+\frac{x}{2}\right)64 - \left(1+\frac{x}{2}\right)576x \text{ or } \left(1+\frac{x}{2}\right)64 - \left(1+\frac{x}{2}\right)576x + \left(1+\frac{x}{2}\right)2160x^{2}$		
	or $64+32x$ , $-576x-288x^2$ , $2160x^2+1080x^3$ are fine.		
	$= 64 - 544x + 1872x^2 +$	A1: At least 2 terms correct as shown. (Allow + $-544x$ here) A1: $64 - 544x + 1872x^2$	A1A1
		The terms can be "listed" rather than added. Ignore any extra terms.	
			[
			Total
	SC: If a candidate expands in descending pow	vers of x, only the M marks are available	

SC: If a candidate expands in descending powers of *x*, only the M marks are available **e.g.**  $\{(2-3x)^6\} = (-3x)^6 + {}^6C_1(2)^2(-3x)^5 + {}^6C_2(2)^2(-3x)^4 + \dots$ 



Question Scheme Marks Number 5.(a) M1: Use of the correct formula or method for the Area *BDE* =  $\frac{1}{2}(5)^2(1.4)$ area of the sector M1A1  $=17.5 (cm^{2})$ A1: 17.5 oe [2] Parts (b) and (c) can be marked together **(b)**  $6.1^{2} = 5^{2} + 7.5^{2} - (2 \times 5 \times 7.5 \cos DBC) \quad \text{or} \quad \cos DBC = \frac{5^{2} + 7.5^{2} - 6.1^{2}}{2 \times 5 \times 7.5} \text{ (or equivalent)}$ M1 M1: A correct statement involving the angle DBC Angle DBC = 0.943201...awrt 0.943 A1 Note that work for (b) may be seen on the diagram or in part (c) [2] (c) Note that candidates may work in degrees in (c) (Angle DBC = 54.04...degrees) Area  $CBD = \frac{1}{2}5(7.5)\sin(0.943)$ Area  $CBD = \frac{1}{2}5(7.5)\sin(\text{their } 0.943)$  or awrt Angle  $EBA = \pi - 1.4 - "0.943"$ 15.2. (Note area of CBD = 15.177...) M1 (Maybe seen on the diagram) A correct method for the area of triangle CBD which can be implied by awrt 15.2  $\pi - 1.4 -$  "their 0.943" A value for angle EBA of awrt 0.8 (from 0.7985926536... or 0.7983916536...) or value for angle M1 *EBA* of (1.74159... - their angle DBC) would imply this mark.  $AB = 5\cos(\pi - 1.4 - "0.943")$ or  $AE = 5\sin(\pi - 1.4 - "0.943")$  $AB = 5\cos(\pi - 1.4 - \text{their } 0.943)$  $AB = 5\cos(0.79859...) = 3.488577938...$ Allow M1 for AB = awrt 3.49Or  $AE = 5\sin(\pi - 1.4 - \text{their } 0.943)$  $AE = 5\sin(0.79859...) = 3.581874365688...$ M1 Allow M1 for AE = awrt 3.58It must be clear that  $\pi - 1.4 - "0.943$ " is being used for angle EBA. Note that some candidates use the sin rule here but it must be used correctly do not allow mixing of degrees and radians. Area  $EAB = \frac{1}{2}5\cos(\pi - 1.4 - "0.943") \times 5\sin(\pi - 1.4 - "0.943")$ This is dependent on the previous M1 dM1 and there must be no other errors in finding the area of triangle EAB Allow M1 for area EAB = awrt 6.2Area ABCDE = 15.17...+ 17.5 + 6.24... = 38.92... awrt 38.9 A1cso

 [5]

 Note that a sign error in (b) can give the obtuse angle (2.198....) and could lead to the correct answer in (c) – this would lose the final mark in (c)

Question Number	Sc	cheme	Marks	
6(a)	s <sup>20</sup> . 160	M1: Use of a correct $S_{\infty}$ formula		
	$S_{\infty} = \frac{20}{1 - \frac{7}{8}}; = 160$	A1: 160	M1A1	
	Accept correct	answer only (160)		
			[2]	
<b>(b</b> )	$20(1-(\frac{7}{2})^{12})$	M1: Use of a correct $S_n$ formula with $n = 12$		
	$S_{12} = \frac{20\left(1 - \left(\frac{7}{8}\right)^{12}\right)}{1 - \frac{7}{2}}; = 127.77324$	(condone missing brackets around 7/8)	M1A1	
	$1-\frac{1}{8}$	A1: awrt 127.8		
	T & I in (b) requires all 12 terms to be calc	culated correctly for M1 and A1 for awrt 127.8		
(a)			[2	
(c)	$20(1-(7)^N)$	Applies $S_N$ ( <b>GP only</b> ) with $a = 20$ , $r = \frac{7}{8}$ and		
	$160 - \frac{20(1 - (\frac{7}{8})^{N})}{1 - \frac{7}{2}} < 0.5$	"uses" 0.5 and their $S_{\infty}$ at any point in their	M1	
	$1 - \frac{1}{8}$	working. (condone missing brackets around $7/8$ )(Allow =, <, >, $\ge$ , $\le$ ) but see note below.		
	$(7)^N$ $(7)^N$ $(05)$	Attempt to isolate $+160\left(\frac{7}{8}\right)^N$ or $+\left(\frac{7}{8}\right)^N$ oe		
	$160\left(\frac{7}{8}\right)^{N} < (0.5) \operatorname{or} \left(\frac{7}{8}\right)^{N} < \left(\frac{0.5}{160}\right)$	(Allow =, <, >, $\geq$ , $\leq$ ) but see note below.	<b>d</b> M1	
		Dependent on the previous M1		
		Uses the power law of logarithms or takes logs base 0.875 correctly to obtain an equation or an		
		inequality of the form	M1	
		$N \log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{\text{their } S_{-}}\right)$		
	$N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{160}\right)$	$N\log\left(\frac{1}{8}\right) < \log\left(\frac{1}{100}\right)$		
	(8) $(160)$	or		
		$N > \log_{0.875} \left( \frac{0.5}{\text{their } S_{\infty}} \right)$		
	(Allow $=, <, >, \ge, \le$ ) but see			
	$N > \frac{\log(\frac{0.5}{160})}{\log(\frac{7}{8})} = 43.19823 \Rightarrow N = 44$	$N = 44$ (Allow $N \ge 44$ but not $N > 44$	A1 cso	
	An incorrect <b>inequality</b> statement at any stage in a candidate's working loses the final mark.			
		tion of the inequality is reversed in the final line full marks for using =, as long as no incorrect		
	working own.		[4	
			Total 8	
	<u>Trial &amp; Im</u>	provement Method in (c):		
	1 <sup>st</sup> M1: Attempts 160 – $S_N$ or $S_N$ with at least one value for $N > 40$			
	$2^{\text{nd}}$ M1: Attempts $160 - S_N$ or $S_N$ with $N = 43$ or $N = 44$			
	$3^{rd}$ M1: For evidence of examining $160 - S_N$ or $S_N$ for both $N = 43$ and $N = 44$ with both			
	correct to 2 DP Eq: 160 S = swrt 0.51 and 160 S = swrt 0.45			
	Eg: $160 - S_{43}$ = awrt 0.51 and $160 - S_{44}$ = awrt 0.45 or $S_{43}$ = awrt 159.49 and $S_{44}$ = awrt 159.55			
-	A1: $N = 44 \operatorname{cso}$			
	4	$A_1: N = 44 cso$		

PM	Т

Question Number	Scheme		Marks
	(i) $9\sin(\theta + 60^{\circ})$	$=4; 0 \le \theta < 360^{\circ}$	
7.	(ii) $2\tan x - 3\sin x = 0; -\pi \le x < \pi$		
(i)	$\sin(\theta + 60^{\circ}) = \frac{4}{9}$ , so $(\theta + 60^{\circ}) = 26.3877$	Sight of $\sin^{-1}\left(\frac{4}{9}\right)$ or awrt 26.4° or 0.461°	
	$(\alpha = 26.3877)$	Can also be implied for $\theta = awrt - 33.6$ (i.e. 26.4 - 60)	M1
	So, $\theta + 60^{\circ} = \{153.6122, 386.3877\}$ and $\theta = \{93.6122, 326.3877\}$	$\mathbf{\theta} + 60^{\circ} = \text{either "180} - \text{their } \boldsymbol{\alpha}^{"} \text{ or }$ "360° + their $\boldsymbol{\alpha}^{"}$ and not for $\boldsymbol{\theta} = \text{either}$ "180 - their $\boldsymbol{\alpha}^{"}$ or "360° + their $\boldsymbol{\alpha}^{"}$ . This can be implied by later working. The candidate's $\boldsymbol{\alpha}$ could also be in radians but do not allow mixing of degrees and radians. A1: At least one of awrt 93.6° or awrt 326.4°	M1 A1 A1
		A1: Both awrt 93.6° and awrt 326.4°	
	Both answers are cso and n	nust come from correct work	
	Ignore extra solutions outside the range.		
	In an otherwise fully correct solution deduct the final A1for any extra solutions in range		[4]
(ii)	$2\left(\frac{\sin x}{\cos x}\right) - 3\sin x = 0$	Applies $\tan x = \frac{\sin x}{\cos x}$	[4] M1
	Note: Applies $\tan x = \frac{\sin x}{\cos x}$ can be implied	d by $2\tan x - 3\sin x = 0 \Longrightarrow \tan x (2 - 3\cos x)$	
	$2\sin x - 3\sin x \cos x = 0$		
	$\sin x(2-3\cos x) = 0$		-
	$\cos x = \frac{2}{3}$	$\cos x = \frac{2}{3}$	A1
	$x = \operatorname{awrt}\{0.84, -0.84\}$	A1: One of either awrt 0.84 or awrt $-0.84$ A1ft: You can apply ft for $x = \pm \alpha$ , where $\alpha = \cos^{-1}k$ and $-1 \le k \le 1$	A1A1ft
		ny extra answers in range in an otherwise	
	correct solution	withhold the A1ft.	
	$\{\sin x = 0 \Rightarrow\} x = 0 \text{ and } -\pi$	<b>Both</b> $x = 0$ and $-\pi$ or awrt $-3.14$ from sin $x = 0$ In this part of the solution, ignore extra solutions in range.	B1
	Note solutions are: $x = \{-3.1415, -0.8410, 0, 0.8410\}$		
	Ignore extra solutions outside the range		
	For <b>all</b> answers in degrees in (ii) M1A1A0A1ftB0 is possible		
	Allow the use of $\theta$ in place of x in (ii)		
			[5]

Ρ	M	Т

Question Number	Scheme			Marks
8.	Graph of $y = 3^x$ and solving	$y = 3^x$ and solving $3^{2x} - 9(3^x) + 18 = 0$		
(a)			the three criteria correct. notes below.)	B1
			e criteria correct. notes below.)	B1
	y <b>↑</b> /	curve for $x \ge 0$	er 1: Correct shape of and at least touches the	
		curve for $x < 0$	er 2: Correct shape of . Must not touch the x-	
	(0, 1)		y turning points. er 3: (0, 1) stated or in	
	O $x$		ked on the y-axis. her than $(0, 1)$ if	
		marked in the " axis.	correct" place on the y-	
<b>(1</b> )				[2]
(b)	$(3^x)^2 - 9(3^x) + 18 = 0$	Forms a quadratic of the correct form in $3^x$ or in "y" where "y" = $3^x$ or even in x		M1
	$y = 3^x \Longrightarrow y^2 - 9y + 18 = 0$	where " $x$ " = $3^x$		1111
	$y = 3^{x} \implies y^{2} - 9y + 18 = 0$ { (y-6)(y-3) = 0 or (3 <sup>x</sup> - 6)(3 <sup>x</sup> - 3) = 0 }			
	$y = 6$ , $y = 3$ or $3^x = 6$ , $3^x = 3$	<b>Both</b> $y = 6$ and	d  y = 3.	A1
		A valid method	for solving $3^x = k$	
	$\left\{3^x = 6 \implies\right\} x \log 3 = \log 6$	where $k > 0, k =$	$\neq 1, k \neq 3$	
	or $x = \frac{\log 6}{\log 3}$ or $x = \log_3 6$		$x \log 3 = \log k$ or	<b>d</b> M1
	$\log 3$ $\log 3$	to give either	$x = \frac{\log k}{\log 3}$ or $x = \log_3 k$ .	
	x = 1.63092 awrt 1.63		A1cso	
	Provided the first M1A1 is scored, the second M1A1 can be implied by awrt 1.63			
	<i>x</i> = 1	x = 1 stated as a solution from <i>any</i> working.		B1
				[5]
				Total 7

PM	Т

Scheme		
Mark (a) and (b) tog	gether	
$OQ^{2} = (6\sqrt{5})^{2} + 4^{2} \text{ or } OQ = \sqrt{(6\sqrt{5})^{2} + 4^{2}} \{= 14\}$	Uses the addition form of Pythagoras on $6\sqrt{5}$ and 4. Condone missing brackets on $(6\sqrt{5})^2$	M1
	(Working or 14 may be seen on the diagram)	
$v_{1} = \sqrt{14^{2} - 11^{2}}$	$y_Q = \sqrt{(\text{their } OQ)^2 - 11^2}$	<b>d</b> M1
	Must include √ and is dependent on the first M1 and requires OQ > 11	uivii
$=\sqrt{75}$ or $5\sqrt{3}$	$\sqrt{75}$ or $5\sqrt{3}$	A1cso
		[3]
$(x-11)^{2} + (y-5\sqrt{3})^{2} = 16$ Allow in expanded form for	Equation must be of this form and must use x and y not other letters. k could be their last answer to part (a). Allow their $k \neq 0$ or just the letter k. A1: $(x - 11)^2 + (y - 5\sqrt{3})^2 = 16$ or $(x - 11)^2 + (y - 5\sqrt{3})^2 = 4^2$ NB $5\sqrt{3}$ must come from correct work in (a) and allow awrt 8.66	- M1A1
e.g. $x^2 - 22x + 121 + y^2 - 10^4$	$\sqrt{3}y + 75 = 16$	
		[2]
		Total 5
Watch ou	t for:	
(a) $OQ = \sqrt{\left(6\sqrt{5}\right)^2}$	$\overline{+4^2} = \sqrt{46} \text{ M1}$	
$y_Q = \sqrt{46 - 11^2} \text{ M0 (OQ < 11)}$		
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	$y_{\varrho} = \sqrt{14^{2} - 11^{2}}$ $= \sqrt{75} \text{ or } 5\sqrt{3}$ $(x - 11)^{2} + (y - 5\sqrt{3})^{2} = 16$ Allow in expanded form for e.g. $x^{2} - 22x + 121 + y^{2} - 10$ Watch ou (a) $OQ = \sqrt{(6\sqrt{5})^{2}}$ $y_{\varrho} = \sqrt{46 - 11^{2}} M$ $y_{\varrho} = \sqrt{72}$	$OQ^{2} = (6\sqrt{5})^{2} + 4^{2} \text{ or } OQ = \sqrt{(6\sqrt{5})^{2} + 4^{2}}  \{=14\}$ on $6\sqrt{5}$ and 4. Condone missing brackets on $(6\sqrt{5})^{2}$ (Working or 14 may be seen on the diagram) $y_{Q} = \sqrt{(14^{2} - 11^{2})}$ $y_{Q} = \sqrt{(their OQ)^{2} - 11^{2}}$ Must include $\sqrt{4}$ and is dependent on the first M1 and requires $OQ > 11$ $= \sqrt{75} \text{ or } 5\sqrt{3}$ $\sqrt{75} \text{ or } 5\sqrt{3}$ $M1: (x \pm 11)^{2} + (y \pm their k)^{2} = 4^{2}$ Equation must be of this form and must use x and y not other letters. k could be their last answer to part (a) Allow their $k \neq 0$ or just the letter k. Al1: $(x - 11)^{2} + (y - 5\sqrt{3})^{2} = 16$ or $(x - 11)^{2} + (y - 5\sqrt{3})^{2} = 16$ or $(x - 11)^{2} + (y - 5\sqrt{3})^{2} = 4^{2}$ NB $5\sqrt{3}$ must come from correct work in (a) and allow awrt 8.66 Allow in expanded form for the final A1 e.g. $x^{2} - 22x + 121 + y^{2} - 10\sqrt{3}y + 75 = 16$ Watch out for: (a) $OQ = \sqrt{(6\sqrt{5})^{2} + 4^{2}} = \sqrt{46}$ M1

PMT
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Question Number	Scheme			Marks
<b>10.</b> (a)	$\frac{1}{2}(9x+6x)4x$ or $2x \times 15x$ or $\left(\frac{1}{2}4x \times (9x-6x)+6x \times 4x\right)$ or $6x^{2}+24x^{2}$ or $\left(9x \times 4x-\frac{1}{2}4x \times (9x-6x)\right)$ or $36x^{2}-6x^{2}$	trapezium. Note that 3 incorrect w If there is a area of the	t attempt at the area of a $0x^2$ on its own or $30x^2$ from ork e.g. $5x \times 6x$ is M0. clear intention to find the trapezium correctly allow the A1 can be withheld if there s.	M1A1 <b>cso</b>
	$\Rightarrow 30x^2y = 9600 \Rightarrow y = \frac{9600}{30x^2} \Rightarrow y = \frac{320}{x^2} *$		t proof with at least one e step and no errors seen. <b>quired.</b>	
				[2]
(b)	$\left(S=\right)\frac{1}{2}(9x+6x)4x+\frac{1}{2}(9x+6x)4x+6xy+9xy+5xy+4xy$			M1A1
	M1: An attempt to find the area of <b>six</b> faces of the prism. The 2 trapezia may be combined as $(9x + 6x)4x$ or $60x^2$ and the 4 other faces may be combined as $24xy$ but all six faces must be			
	included. There must be attempt at the areas of two trapezia that are dimensionally correct. A1: Correct expression in any form. Allow just $(S =) 60x^2 + 24xy$ for M1A1			
	$y = \frac{320}{x^2} \Rightarrow (S =) 30x^2 + 30x^2 + 24x \left(\frac{320}{x^2}\right)$			M1
	Substitutes $y = \frac{320}{x^2}$ into their expression for <i>S</i> (may be done earlier). <i>S</i> should have at least			
	one $x^2$ term and one xy term but there may be other terms which may be dimensionally incorrect.			
	So, $(S =) 60x^2 + \frac{7680}{x} *$		Correct solution only. " $S =$ " is <b>not</b> required here.	A1* <b>cso</b>
				[4]

$\frac{\mathrm{d}S}{\mathrm{d}x} = 120x - 76$	$580x^{-2} \left\{ = 120x - \frac{7680}{x^2} \right\}$	M1: Either $60x^2 \rightarrow 120x$ or $\frac{7680}{x} \rightarrow \frac{\pm \lambda}{x^2}$ A1: Correct differentiation (need not be	M1
u.		A1: Correct differentiation (need not be simplified).	A1 aef
		M1: $S' = 0$ and "their $x^3 = \pm$ value"	
		or "their $x^{-3} = \pm$ value" Setting their $\frac{dS}{dx} = 0$	
		and "candidate's ft <i>correct</i> power of <i>x</i> = a value". <b>The power of <i>x</i> must be consistent</b>	
		with their differentiation. If inequalities are	
		used this mark cannot be gained until candidate	
		states value of x or S from their x without	
120x	$x - \frac{7680}{x^2} = 0$	inequalities. $S' = 0$ can be implied by	
	$\Rightarrow x^3 = \frac{7680}{120}; = 64 \Rightarrow x = 4$	$120x = \frac{7680}{x^2}$ . Some may spot that $x = 4$ gives	M1A1cso
,	120	S' = 0 and provided they clearly show $S'(4) = 0$	
		allow this mark as long as $S'$ is correct. (If $S'$	
		is incorrect this method is allowed if their	
		derivative is clearly zero for their value of <i>x</i> )	
		A1: $x = 4$ only ( $x^3 = 64 \implies x = \pm 4$ scores A0)	
		Note that the value of <i>x</i> is not explicitly required	
		so the use of $x = \sqrt[3]{64}$ to give $S = 2880$ would	
		imply this mark.	
Note some o	Note some candidates stop here and do not go on to find S – maximum mark is 4/6		
	{ $x = 4$ ,} $S = 60(4)^2 + \frac{7680}{4} = 2880 \text{ (cm}^2\text{)}$	Substitute candidate's value of $x \ne 0$ into a	
		formula for S. Dependent on both previous M	<b>dd</b> M1
$S = 60(4)^2$		marks.	
5 - 00(4)		2880 cso (Must come from correct work)	A1 cao
		, , ,	and cso
			[6

10(d)	M1: Attempt $S''(x^n \to x^{n-1})$ and considers	
	$\frac{d^2S}{dx^2} = 120 + \frac{15360}{x^3} > 0$ $\Rightarrow Minimum$ $\frac{d^2S}{dx^2} = 120 + \frac{15360}{x^3} > 0$ $\Rightarrow Minimum$ $\frac{d^2S}{dx^2} = 120 + \frac{15360}{x^3} > 0$ $\Rightarrow Minimum$ $A1: 120 + \frac{15360}{x^3} \text{ and } > 0 \text{ and conclusion.}$ $Requires a \frac{\text{correct}}{x^3} \text{ second derivative of}$ $120 + \frac{15360}{x^3} \text{ (need not be simplified)} \text{ and } a$ $valid reason (e.g. > 0), \text{ and conclusion.}$ $Only follow through a correct second derivative$ $i.e. x may be incorrect but must be positive$	M1A1ft
	and/or $S''$ may have been <u>evaluated</u> incorrectly. <b>A correct</b> $S''$ followed by $S''("4") = "360"$ therefore minimum would score no marks in (d)	
	A correct S" followed by S"("4") = "360" which is positive therefore minimum would score	
	both marks	
		[2]
	Note parts (c) and (d) can be marked together.	
		Total 14

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