## DIFFERENTIATION

**C4** 

1	Differentiate with respect to x			
	<b>a</b> 4 <i>y</i> <b>b</b>	$y^3$	<b>c</b> $\sin 2y$	<b>d</b> $3e^{y^2}$
2	Find $\frac{dy}{dx}$ in terms of x and y in each case.			
	$\mathbf{a}  x^2 + y^2 = 2$	<b>b</b> $2x - y + y^2$	$c^2 = 0$ c	$y^4 = x^2 - 6x + 2$
	<b>d</b> $x^2 + y^2 + 3x - 4y = 9$	<b>e</b> $x^2 - 2y^2 +$	$x + 3y - 4 = 0 \qquad \mathbf{f}$	$\sin x + \cos y = 0$
	$g  2e^{3x} + e^{-2y} + 7 = 0$	<b>h</b> $\tan x + \cos x$	$\sec 2y = 1 \qquad i$	$\ln\left(x-2\right) = \ln\left(2y+1\right)$
3	Differentiate with respect to x			
	<b>a</b> xy <b>b</b>	$x^2y^3$	<b>c</b> $\sin x \tan y$	$\mathbf{d}  (x-2y)^3$
4	Find $\frac{dy}{dx}$ in terms of x and y in each case.			
	<b>a</b> $x^2y = 2$	<b>b</b> $x^2 + 3xy - y^2 = 0$ <b>c</b> $4x^2 - 2xy + 3y^2 = 8$		
	$\mathbf{d}  \cos 2x \sec 3y + 1 = 0$	e  y = (x + y)	<sup>2</sup> <b>f</b>	$xe^{y} - y = 5$
	$\mathbf{g}  2xy^2 - x^3y = 0$	<b>h</b> $y^2 + x \ln y$	= 3 i	$x\sin y + x^2\cos y = 1$
5	Find an equation for the tangent to each curve at the given point on the curve.			
	<b>a</b> $x^2 + y^2 - 3y - 2 = 0$ ,	(2, 1)	$\mathbf{b}  2x^2 - xy + y^2 =$	28, (3, 5)
	$\mathbf{c}  4\sin y - \sec x = 0,$	$\left(\frac{\pi}{3},\frac{\pi}{6}\right)$	<b>d</b> $2 \tan x \cos y =$	$1, \qquad \left(\frac{\pi}{4}, \frac{\pi}{3}\right)$
6	A curve has the equation $x^2 + 2y^2 - x + 4y = 6$ .			
	<b>a</b> Show that $\frac{dy}{dx} = \frac{1-2x}{4(y+1)}$ .			
	<b>b</b> Find an equation for the normal to the curve at the point $(1, -3)$ .			
7	A curve has the equation $x^2 + 4xy - 3y^2 = 36$ .			
,	<b>a</b> Find an equation for the tangent to the curve at the point $P(4, 2)$ .			
	Given that the tangent to the curve at the point $Q$ on the curve is parallel to the tangent at $P$ ,			
	<b>b</b> find the coordinates of $Q$ .			
8	A curve has the equation $y = a^x$ , where <i>a</i> is a positive constant.			
	By first taking logarithms, find an expression for $\frac{dy}{dx}$ in terms of <i>a</i> and <i>x</i> .			
9	Differentiate with respect to x			
	<b>a</b> 3 <sup>x</sup> <b>b</b>	6 <sup>2x</sup>	<b>c</b> $5^{1-x}$	<b>d</b> $2^{x^3}$
10	A biological culture is growing exponentially such that the number of bacteria present, $N$ , at time $t$ minutes is given by			
	$N = 800(1.04)^t$ .			

Find the rate at which the number of bacteria is increasing when there are 4000 bacteria present.