

1 Integrate with respect to x

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|-------------------------|--|-------------------------------|-------------------------------------|
| a $2 \cos x$ | b $\sin 4x$ | c $\cos \frac{1}{2}x$ | d $\sin(x + \frac{\pi}{4})$ |
| e $\cos(2x - 1)$ | f $3 \sin(\frac{\pi}{3} - x)$ | g $\sec x \tan x$ | h $\operatorname{cosec}^2 x$ |
| i $5 \sec^2 2x$ | j $\operatorname{cosec} \frac{1}{4}x \cot \frac{1}{4}x$ | k $\frac{4}{\sin^2 x}$ | l $\frac{1}{\cos^2(4x+1)}$ |

2 Evaluate

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| a $\int_0^{\frac{\pi}{2}} \cos x \, dx$ | b $\int_0^{\frac{\pi}{6}} \sin 2x \, dx$ | c $\int_0^{\frac{\pi}{2}} 2 \sec \frac{1}{2}x \tan \frac{1}{2}x \, dx$ |
| d $\int_0^{\frac{\pi}{3}} \cos(2x - \frac{\pi}{3}) \, dx$ | e $\int_{\frac{\pi}{4}}^{\frac{\pi}{3}} \sec^2 3x \, dx$ | f $\int_{\frac{\pi}{2}}^{\frac{2\pi}{3}} \operatorname{cosec} x \cot x \, dx$ |

3 a Express $\tan^2 \theta$ in terms of $\sec \theta$.

b Show that $\int \tan^2 x \, dx = \tan x - x + c$.

4 a Use the identity for $\cos(A + B)$ to express $\cos^2 A$ in terms of $\cos 2A$.

b Find $\int \cos^2 x \, dx$.

5 Find

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|---|--|--------------------------------------|
| a $\int \sin^2 x \, dx$ | b $\int \cot^2 2x \, dx$ | c $\int \sin x \cos x \, dx$ |
| d $\int \frac{\sin x}{\cos^2 x} \, dx$ | e $\int 4 \cos^2 3x \, dx$ | f $\int (1 + \sin x)^2 \, dx$ |
| g $\int (\sec x - \tan x)^2 \, dx$ | h $\int \operatorname{cosec} 2x \cot x \, dx$ | i $\int \cos^4 x \, dx$ |

6 Evaluate

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|---|--|---|
| a $\int_0^{\frac{\pi}{2}} 2 \cos^2 x \, dx$ | b $\int_0^{\frac{\pi}{4}} \cos 2x \sin 2x \, dx$ | c $\int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \tan^2 \frac{1}{2}x \, dx$ |
| d $\int_{\frac{\pi}{6}}^{\frac{\pi}{4}} \frac{\cos 2x}{\sin^2 2x} \, dx$ | e $\int_0^{\frac{\pi}{4}} (1 - 2 \sin x)^2 \, dx$ | f $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \sec^2 x \operatorname{cosec}^2 x \, dx$ |

7 a Use the identities for $\sin(A + B)$ and $\sin(A - B)$ to show that

$$\sin A \cos B \equiv \frac{1}{2} [\sin(A + B) + \sin(A - B)].$$

b Find $\int \sin 3x \cos x \, dx$.

8 Integrate with respect to x

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|-----------------------------|---------------------------|-----------------------------|---|
| a $2 \sin 5x \sin x$ | b $\cos 2x \cos x$ | c $4 \sin x \cos 4x$ | d $\cos(x + \frac{\pi}{6}) \sin x$ |
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