

1 **a)** $-p$ **b)** $2q$ **c)** $\frac{1}{2}p$ **d)** p **e)** $-q$ **f)** $p + q$
g) $\frac{1}{2}p + 2q$ **h)** $p - q$ **i)** $2q - p$ **j)** $-p - 2q$ **k)** $\frac{1}{2}p - q$ **l)** $-\frac{1}{2}p - 2q$

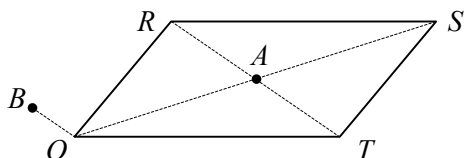
2 **a) $\mathbf{u} + \mathbf{v}$** **b) $\mathbf{w} - \mathbf{u}$** **c) $\mathbf{u} + \mathbf{v} - \mathbf{w}$**

3 **a) q** **b) $p + r$** **c) $r - q$** **d) $p + q + r$** **e) $-q - r$** **f) $q + r - p$**

$$\begin{aligned} \text{4} \quad \text{a} \quad \text{i} &= (\mathbf{a} + 2\mathbf{b}) + (\mathbf{a} - 2\mathbf{b}) \\ &= 2\mathbf{a} \\ \text{ii} &= (\mathbf{a} + 2\mathbf{b}) - (\mathbf{a} - 2\mathbf{b}) \\ &= 4\mathbf{b} \end{aligned}$$

b $\overrightarrow{OA} = \frac{1}{2} \overrightarrow{OS}$, $\overrightarrow{OB} = \frac{1}{4} \overrightarrow{TR}$

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$$\begin{aligned} \text{5} \quad \mathbf{a} \cdot \mathbf{i} &= \frac{1}{2} \mathbf{a} \\ \text{ii} &= \mathbf{b} - \mathbf{a} \\ \text{iii} &= \frac{1}{2}(\mathbf{b} - \mathbf{a}) \\ \text{iv} &= \mathbf{a} + \frac{1}{2}(\mathbf{b} - \mathbf{a}) = \frac{1}{2}(\mathbf{a} + \mathbf{b}) \\ \text{v} &= \frac{1}{2}(\mathbf{a} + \mathbf{b}) - \frac{1}{2} \mathbf{a} = \frac{1}{2} \mathbf{b} \end{aligned}$$

b they are parallel (and the magnitude of $\overrightarrow{CD}$ is half that of $\overrightarrow{OB}$)

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- a** parallel, $3\mathbf{p} = \frac{3}{2}(2\mathbf{p})$
- b** not parallel
- c** parallel, $(\mathbf{p} - \frac{1}{3}\mathbf{q}) = \frac{1}{3}(3\mathbf{p} - \mathbf{q})$
- d** parallel, $(4\mathbf{q} - 2\mathbf{p}) = -2(\mathbf{p} - 2\mathbf{q})$
- e** parallel, $(6\mathbf{p} + 8\mathbf{q}) = 8(\frac{3}{4}\mathbf{p} + \mathbf{q})$
- f** not parallel

7 **a** $= (2\mathbf{m} + 3\mathbf{n}) - (4\mathbf{m} + 2\mathbf{n})$
 $= \mathbf{n} - 2\mathbf{m}$
 b $\overrightarrow{OM} = \frac{1}{2} \overrightarrow{OC} = \mathbf{m} + \frac{3}{2} \mathbf{n}$
 $\overrightarrow{AM} = (\mathbf{m} + \frac{3}{2} \mathbf{n}) - 4\mathbf{m} = \frac{3}{2} \mathbf{n} - 3\mathbf{m}$
 $\therefore \overrightarrow{AM} = \frac{3}{2} \overrightarrow{BC}$
 $\therefore AM$ is parallel to BC

$$8 \quad \mathbf{a} \quad \overrightarrow{OM} = \frac{1}{2} \overrightarrow{OA} = 3\mathbf{u} - 2\mathbf{v}$$

$$\overrightarrow{AB} = (3\mathbf{u} - \mathbf{v}) - (6\mathbf{u} - 4\mathbf{v}) = 3\mathbf{v} - 3\mathbf{u}$$

$$\overrightarrow{ON} = \overrightarrow{OA} + \frac{1}{3} \overrightarrow{AB} = (6\mathbf{u} - 4\mathbf{v}) + \frac{1}{3}(3\mathbf{v} - 3\mathbf{u}) = 5\mathbf{u} - 3\mathbf{v}$$

$$\mathbf{b} \quad \overrightarrow{CM} = (3\mathbf{u} - 2\mathbf{v}) - (\mathbf{v} - 3\mathbf{u}) = 6\mathbf{u} - 3\mathbf{v}$$

$$\overrightarrow{CN} = (5\mathbf{u} - 3\mathbf{v}) - (\mathbf{v} - 3\mathbf{u}) = 8\mathbf{u} - 4\mathbf{v}$$

$$\therefore \overrightarrow{CN} = \frac{4}{3} \overrightarrow{CM}$$

$\therefore \overrightarrow{CN}$ and $\overrightarrow{CM}$ are parallel

common point $C \therefore C, M$ and N are collinear

$$9 \quad \mathbf{a} \quad a = 5, b = 3$$

$$\mathbf{b} \quad 2 + b = 0 \text{ and } a - 4 = 0$$

$$\therefore a = 4, b = -2$$

$$\mathbf{c} \quad -1 = b \text{ and } 4a = -2$$

$$\therefore a = -\frac{1}{2}, b = -1$$

$$\mathbf{d} \quad 2a + 6 = 0 \text{ and } b - a = 0$$

$$\therefore a = -3, b = -3$$

$$10 \quad \mathbf{a} \quad \overrightarrow{OC} = \frac{1}{2} \mathbf{a}$$

$$\overrightarrow{CB} = \mathbf{b} - \frac{1}{2} \mathbf{a}$$

$$\overrightarrow{OD} = \frac{1}{2} \mathbf{a} + \frac{1}{2} (\mathbf{b} - \frac{1}{2} \mathbf{a}) = \frac{1}{4} \mathbf{a} + \frac{1}{2} \mathbf{b}$$

$$\mathbf{b} \quad \overrightarrow{AB} = \mathbf{b} - \mathbf{a}$$

$$\overrightarrow{OE} = \overrightarrow{OA} + k \overrightarrow{AB}$$

$$\therefore \overrightarrow{OE} = \mathbf{a} + k(\mathbf{b} - \mathbf{a})$$

$$\mathbf{c} \quad \overrightarrow{OE} = l \overrightarrow{OD}$$

$$\therefore \mathbf{a} + k(\mathbf{b} - \mathbf{a}) = l(\frac{1}{4} \mathbf{a} + \frac{1}{2} \mathbf{b})$$

$$\therefore 1 - k = \frac{1}{4} l$$

$$\text{and } k = \frac{1}{2} l$$

$$\text{adding } 1 = \frac{3}{4} l$$

$$l = \frac{4}{3}$$

$$\therefore \overrightarrow{OE} = \frac{4}{3} (\frac{1}{4} \mathbf{a} + \frac{1}{2} \mathbf{b}) = \frac{1}{3} \mathbf{a} + \frac{2}{3} \mathbf{b}$$

$$\mathbf{d} \quad k = \frac{1}{2} l = \frac{2}{3}$$

$$\therefore \overrightarrow{AE} = \frac{2}{3} \overrightarrow{AB}$$

$$\therefore AE : EB = 2 : 1$$