

- $$\sqrt{(9+8x)}, \quad |x| < \frac{9}{8}$$

(5)

- (3)

[illegible]

Question 1 continued

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Q1

(Total 8 marks)



2.

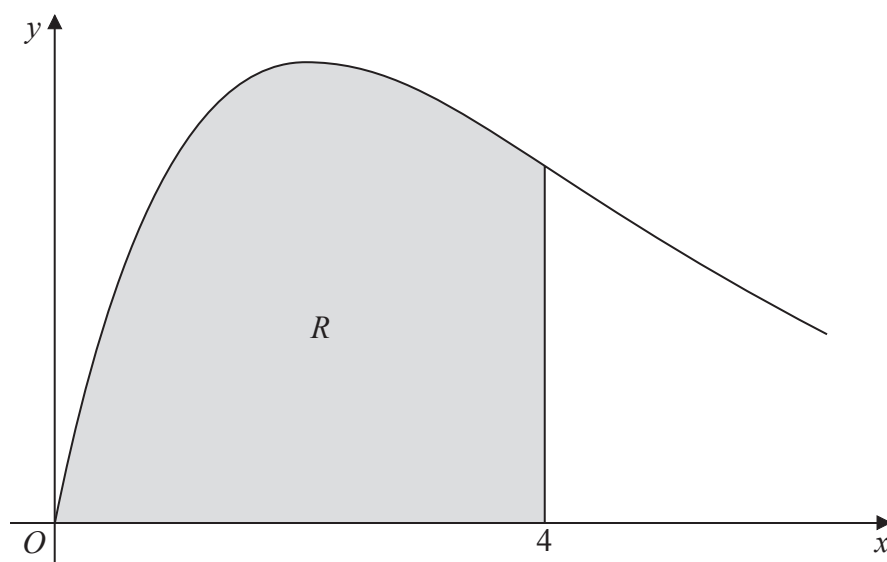


Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = xe^{-\frac{1}{2}x}$, $x \geq 0$.

The finite region R , shown shaded in Figure 1, is bounded by the curve, the x -axis, and the line $x = 4$.

The table shows corresponding values of x and y for $y = xe^{-\frac{1}{2}x}$.

x	0	1	2	3	4
y	0	$e^{-\frac{1}{2}}$		$3e^{-\frac{3}{2}}$	$4e^{-2}$

(a) Complete the table with the value of y corresponding to $x = 2$ (1)

(b) Use the trapezium rule, with all the values of y in the completed table, to obtain an estimate for the area of R , giving your answer to 2 decimal places. (4)

(c) (i) Find $\int xe^{-\frac{1}{2}x} dx$.
 (ii) Hence find the exact area of R , giving your answer in the form $a + be^{-2}$, where a and b are integers. (6)



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Question 2 continued

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Question 2 continued

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(Total 11 marks)

Q2

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3. A curve C has parametric equations

$$x = 2t + 5, \quad y = 3 + \frac{4}{t}, \quad t \neq 0$$

- (a) Find the value of $\frac{dy}{dx}$ at the point on C with coordinates $(9, 5)$.

(4)

- (b) Find a cartesian equation of the curve in the form

$$y = \frac{ax + b}{cx + d}$$

where a, b, c and d are integers.

(3)



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Question 3 continued



[illegible]



P 4 2 8 2 7 A 0 1 0 3 2

Question 3 continued

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Q3

(Total 7 marks)



4. With respect to a fixed origin O , the line l_1 has vector equation

$$\mathbf{r} = \begin{pmatrix} -9 \\ 8 \\ 5 \end{pmatrix} + \mu \begin{pmatrix} 5 \\ -4 \\ -3 \end{pmatrix}$$

where μ is a scalar parameter.

The point A is on l_1 where $\mu = 2$.

- (a) Write down the coordinates of A .

(1)

The acute angle between OA and l_1 is θ , where O is the origin.

- (b) Find the value of $\cos \theta$.

(3)

The point B is such that $\overrightarrow{OB} = 3\overrightarrow{OA}$.

The line l_2 passes through the point B and is parallel to the line l_1 .

- (c) Find a vector equation of l_7 .

(2)

- (d) Find the length of OB , giving your answer as a simplified surd.

(1)

The point X lies on l_j . Given that the vector \overrightarrow{OX} is perpendicular to l_j ,

- (e) find the length of OX , giving your answer to 3 significant figures.

(3)

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Question 4 continued





Question 4 continued

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(Total 10 marks)

Q4

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5. The curve C has the equation

$$\sin(\pi y) - y - x^2 y = -5, \quad x > 0$$

- (a) Find $\frac{dy}{dx}$ in terms of x and y . (5)

The point P with coordinates $(2, 1)$ lies on C .
The tangent to C at P meets the x -axis at the point A .

- (b) Find the exact value of the x -coordinate of A . (4)

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Question 5 continued





Question 5 continued

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Q5

(Total 9 marks)



(3)

(3)

(5)

$$\int \frac{1}{x + x^{\frac{1}{3}}} dx, \quad x > 0$$

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Question 6 continued





Question 6 continued

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Handwriting practice lines for Question 6 continued.

(Total 11 marks)

Q6

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7.

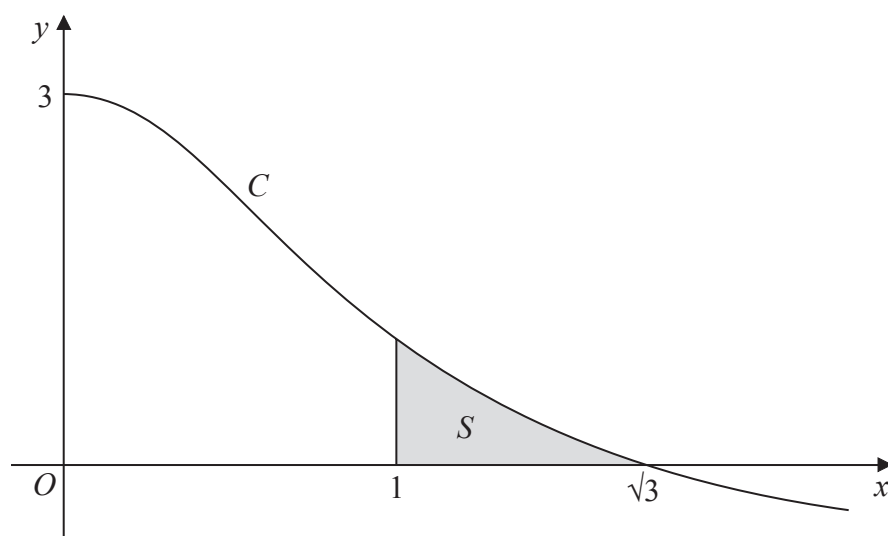


Figure 2

Figure 2 shows a sketch of part of the curve C with parametric equations

$$x = \tan \theta, \quad y = 1 + 2\cos 2\theta, \quad 0 \leq \theta < \frac{\pi}{2}$$

The curve C crosses the x -axis at $(\sqrt{3}, 0)$. The finite shaded region S shown in Figure 2 is bounded by C , the line $x=1$ and the x -axis. This shaded region is rotated through 2π radians about the x -axis to form a solid of revolution.

(a) Show that the volume of the solid of revolution formed is given by the integral

$$k \int_{\frac{\pi}{4}}^{\frac{\pi}{3}} (16 \cos^2 \theta - 8 + \sec^2 \theta) \, d\theta$$

where k is a constant.

(5)

(b) Hence, use integration to find the exact value for this volume.

(5)



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Question 7 continued





Question 7 continued

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Q7

(Total 10 marks)



8.

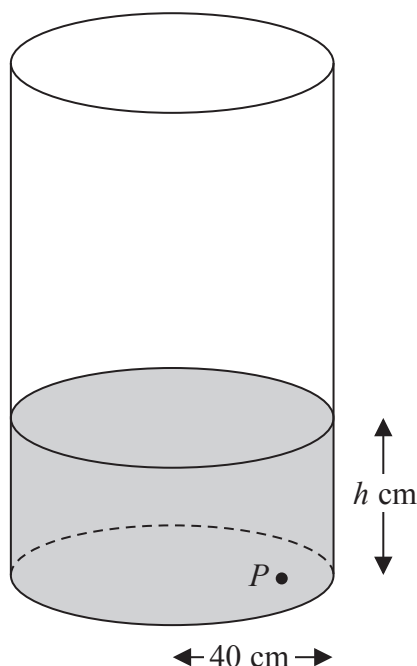


Figure 3

Figure 3 shows a large vertical cylindrical tank containing a liquid. The radius of the circular cross-section of the tank is 40 cm. At time t minutes, the depth of liquid in the tank is h centimetres. The liquid leaks from a hole P at the bottom of the tank.

The liquid leaks from the tank at a rate of $32\pi\sqrt{h}$ cm³ min⁻¹.

- (a) Show that at time t minutes, the height h cm of liquid in the tank satisfies the differential equation

$$\frac{dh}{dt} = -0.02\sqrt{h} \quad (4)$$

- (b) Find the time taken, to the nearest minute, for the depth of liquid in the tank to decrease from 100 cm to 50 cm. (5)



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Question 8 continued





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Question 8 continued

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Question 8 continued

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Q8

(Total 9 marks)

TOTAL FOR PAPER: 75 MARKS

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