Mark Scheme 4723 January 2007

M1

1 Attempt use of quotient rule to find derivative allow for numerator 'wrong way round'; or attempt use of product rule

Obtain
$$\frac{2(3x-1)-3(2x+1)}{(3x-1)^2}$$

A1 or equiv

Obtain $-\frac{5}{4}$ for gradient

A1 or equiv

Attempt eqn of straight line with numerical gradient

obtained from their $\frac{dy}{dx}$; tangent not normal

Obtain 5x + 4y - 11 = 0

5 or similar equiv

Attempt complete method for finding $\cot \theta$ 2 (i) Obtain $\frac{5}{12}$

M1rt-angled triangle, identities, calculator, ...

A1 2 or exact equiv

Attempt relevant identity for $\cos 2\theta$ (ii)

 $+2\cos^{2}\theta + 1$ or $+1 + 2\sin^{2}\theta$ or M1 $\pm(\cos^2\theta-\sin^2\theta)$

State correct identity with correct value(s) substituted Obtain $-\frac{119}{169}$

A₁

A1 3 correct answer only earns 3/3

3 (a) Sketch reasonable attempt at $y = x^5$

*B1 accept non-zero gradient at O but curvature to be correct in first and third quadrants

B1

Sketch straight line with negative gradient Indicate in some way single point of intersection B1 3 dep *B1 *B1

existing at least in (part of) first quadrant

allow if not part of subsequent iteration

(b) Obtain correct first iterate Carry out process to find at least 3 iterates in all M1 Obtain at least 1 correct iterate after the first

allow for recovery after error; showing at least 3 d.p. in iterates

Conclude 2.175

A1 4 answer required to precisely 3 d.p.

 $[0 \rightarrow 2.21236 \rightarrow 2.17412 \rightarrow 2.17480 \rightarrow 2.17479;$ $1 \rightarrow 2.19540 \rightarrow 2.17442 \rightarrow 2.17480 \rightarrow 2.17479$; $2 \rightarrow 2.17791 \rightarrow 2.17473 \rightarrow 2.17479 \rightarrow 2.17479$;

 $3 \rightarrow 2.15983 \rightarrow 2.17506 \rightarrow 2.17479 \rightarrow 2.17479$

Obtain derivative of form $k(4t+9)^{-\frac{1}{2}}$ 4 (i)

M1 any constant k

Obtain correct $2(4t+9)^{-\frac{1}{2}}$

A1 or (unsimplified) equiv

Obtain derivative of form $k e^{\frac{1}{2}x+1}$

M1any constant k different from 6

Obtain correct $3e^{\frac{1}{2}x+1}$

A1 4 or equiv

Either: Form product of two derivatives M1 (ii) Substitute for t and x in product M1 Obtain 39.7

numerical or algebraic

using t = 4 and calculated value of x

3 allow ± 0.1 ; allow greater accuracy

differentiating $y = 6e^{\frac{1}{2}(4t+9)^{\frac{1}{2}}+1}$ M1

Obtain $k(4t+9)^n e^{\frac{1}{2}(4t+9)^{\frac{1}{2}}+1}$ Or:

Obtain correct $6(4t+9)^{-\frac{1}{2}}e^{\frac{1}{2}(4t+9)^{\frac{1}{2}}+1}$

A1 or equiv

Substitute t = 4 to obtain 39.7 A1 (3) allow ± 0.1 ; allow greater accuracy

Obtain $R = \sqrt{17}$ or 4.12 or 4.1

B1 or greater accuracy

Attempt recognisable process for finding α Obtain $\alpha = 14$

3 or greater accuracy 14.036...

allow for sin/cos confusion

M1

(ii) Attempt to find at least one value of θ + α M1
 Obtain or imply value 61 A1√ following R value; or value rounding to 61
 Obtain 46.9 A1 allow ±0.1; allow greater accuracy
 Show correct process for obtaining second angle M1
 Obtain -75 A1 5 allow ±0.1; allow greater accuracy; max of 4/5 if extra angles between -180 and 180

- 6 (i) Obtain integral of form $k(3x+2)^{\frac{1}{2}}$ M1 any constant kObtain correct $\frac{2}{3}(3x+2)^{\frac{1}{2}}$ A1 or equiv
 Substitute limits 0 and 2 and attempt evaluation M1 for integral of form $k(3x+2)^n$ Obtain $\frac{2}{3}(8^{\frac{1}{2}}-2^{\frac{1}{2}})$ A1 4 or exact equiv suitably simplified
 - (ii) State or imply $\pi \int \frac{1}{3x+2} dx$ or unsimplified version B1 allow if dx absent or wrong Obtain integral of form $k \ln(3x+2)$ M1 any constant k involving π or not Obtain $\frac{1}{3}\pi \ln(3x+2)$ or $\frac{1}{3}\ln(3x+2)$ A1 Show correct use of $\ln a \ln b$ property M1 Obtain $\frac{1}{3}\pi \ln 4$ A1 5 or (similarly simplified) equiv

- 7 (i) State a in x-direction B1 or clear equiv State factor 2 in x-direction B1 2 or clear equiv
 - (ii) Show (largely) increasing function crossing *x*-axis
 Show curve in first and fourth quadrants only A1 2 not touching *y*-axis and with no maximum point; ignore intercept
 - (iii) Show attempt at reflecting negative part in *x*-axis Show (more or less) correct graph M1 A1 $\sqrt{2}$ following their graph in (ii) and showing correct curvatures
 - (iv) Identify 2a as asymptote or 2a + 2 as intercept B1 allow anywhere in question State $2a < x \le 2a + 2$ B1 2 allow < or \le for each inequality

8 (i) Obtain $-2xe^{-x^2}$ as derivative of e^{-x^2} B1

Attempt product rule *M1 allow if sign errors or no chain rule

Obtain $8x^7e^{-x^2} - 2x^9e^{-x^2}$ A1 or (unsimplified) equiv

Either: Equate first derivative to zero and attempt solution M1 dep *M; taking at least one step of solution

Confirm 2 A1 5 AG

Or: Substitute 2 into derivative and show attempt at evaluation M1

Obtain 0 A1 (5) AG; necessary correct detail required

(ii) Attempt calculation involving attempts at y values

M1 with each of 1, 4, 2 present at least once as coefficients

Attempt $k(y_0 + 4y_1 + 2y_2 + 4y_3 + y_4)$

M1 with attempts at five *y* values corresponding to correct *x* values

Obtain $\frac{1}{6}(0 + 4 \times 0.00304 + 2 \times 0.36788$

$$+4 \times 2.70127 + 4.68880$$
)

Obtain 2.707

A1 or equiv with at least 3 d.p. or exact values

A1 4 or greater accuracy; allow ± 0.001

(iii) Attempt 4(y value) - 2(part (ii))

Obtain 13.3

M1 or equiv

A1 2 or greater accuracy; allow ± 0.1

9 (i) State $-2 \le y \le 2$

State $y \le 4$

B1 allow <; any notation

B1 2 allow <; any notation

(ii) Show correct process for composition M1 Obtain or imply 0.959 and hence 2.16 A1

Obtain g(0.5) = 3.5

Observe that 3.5 not in domain of f

right way round

AG; necessary detail required B1 or (unsimplified) equiv

B1 4 or equiv

(iii) Relate quadratic expression to at least one end

of range of f

M1

Obtain both of $4 - 2x^2 < -2$ and $4 - 2x^2 > 2$

A1 or equiv; allow any sign in each (< or \le or > or \ge or =)

Obtain at least two of the x values $-\sqrt{3}$, -1, 1, $\sqrt{3}$ A1

Obtain all four of the *x* values

A1

or equiv

Attempt solution involving four x values M1

to produce at least two sets of values

Obtain $x < -\sqrt{3}$, -1 < x < 1, $x > \sqrt{3}$

A1 **6** allow \leq instead of < and/or \geq instead of >