

**Mark Scheme 4728  
January 2007**

1	(i)	Net force on trailer is	B1	
		$\pm(700 - R_T)$	M1	For applying Newton's second law to the trailer with 2 terms on LHS (no vertical forces)
	(ii)	$700 - R_T = 600 \times 0.8$	A1ft	ft cv ( $\pm(700 - R_T)$ )
		Resistance is 220N	A1	4
	(ii)		M1	For applying Newton's second law to the car or to the whole, with $a = \pm 0.8$ (no vertical forces)
		$2100 - 700 - R_C =$	A1ft	
	$1100 \times 0.8$		ft cv(220)	
	or			
$2100 - (R_C + 220) =$				
$(1100 + 600) \times$				
0.8				
Resistance is 520N	A1	3		

  

2	(i)		M1	For resolving forces vertically
		$15 \times 0.28$ and $11 \times 0.8$	A1	Allow use of $\sin = 16.3$ and $\cos = 53.1$
	(ii)	$Y = 15 \times 0.28 + 11 \times 0.8 - 13$	A1ft	Ft cv( $15 \times 0.28$ and $11 \times 0.8$ )
		Component is zero	A1	4
	(ii)	AG	M1	For resolving forces horizontally
		$X = 15 \times 0.96 - 11 \times 0.6$	A1	Allow use of $\sin = 16.3$ and $\cos = 53.1$
	(iii)	Magnitude is 7.8N	A1	3
		Direction is that of the (+ve) x -axis	B1	1
				Accept 7.79, -7.8
				Do not allow horizontal, $90^\circ$ from vertical. Do not award if $\sin = 16.3$ and $\cos = 53.1$ have been used.

  

3	(i)	$T = 0.3g$	B1	At particle (or $0.3g - T = 0.3a$ )
		$F = T$	B1	Or $F = cv(T \text{ at particle})$ (or $T - F = 0.4a$ )
	(ii)	$R = 0.4g$	B1	
		Coefficient is 0.75	M1	For using $F = \mu R$
	(ii)		A1	5
		$X = 0.3g + 0.3g$	M1	For resolving 3 relevant forces on B horizontally, $a=0$
	$X = 5.88N$	A1ft	Ft $X = 0.3g + cv(\mu)$	
				cv(R)

4	(i)	Momentum before collision $= +/- (0.8 \times 4 - 0.6 \times 2)$	B1	4	Or momentum change L $0.8 \times 4 +/- 0.8 v_L$ Accept inclusion of g in both terms
		Momentum after collision $= +/- 0.8 v_L + 0.6 \times 2$	B1		Momentum change N $0.6 \times 2 + 0.6 \times 2$ Accept inclusion of g in both terms
		Speed is $1 \text{ ms}^{-1}$	M1		For using the principle of conservation of momentum even if g is included throughout
			A1		Accept -1 from correct work (g not used).
	(ii)(a)	$0.6 \times 2 - 0.7 \times 0.5$	M1	4	Must be a difference. <b>SR</b> $0.6 \times 1 - 0.7 \times 0.5$ M1
		Total is $0.85 \text{ kgms}^{-1}$	A1		Must be positive
		<u>Total</u> momentum +ve after the collision. If N continues in its original direction, both particles have a negative momentum. N must reverse its direction.	DM 1		Or $0.6v + 0.7w$ is positive, confirming that the momentum is shared between two particles. No reference need be made to the physically impossible scenario where M and N both might continue in their original directions.
	(ii)(b)	$0.6 \times 2 - 0.7 \times 0.5 (= 0.85) = 0.7v$	A1ft	2	ft cv (0.85). Award M1 if not given in ii(a).
		Speed is $1.21 \text{ ms}^{-1}$	A1		Positive. Accept (a.r.t) 1.2 from correct work

5	(i)	$1.8t^2/2$ (+C)	M*1	3	For using $v = \int adt$
		(t = 0, v = 0) C = 0	B1		May be awarded in (ii). Accept c written and deleted.
	(ii)	Expression is $1.8t^2/2$	A1	4	also for $1.8t^2 + c$
		$0.9t^3/3$ (+K)	M1		For using $s = \int vdt$
	(iii)	$0.3 \times 64$	A1	5	<b>SR</b> Award B1 for (s = 0, t = 0) K = 0 if not already given in (i), or +K included and limits used.
		19.2m AG	M1		For using limits 0 to 4 (or equivalent)
		$u = 0.9 \times 4^2$	A1		For using 'u' = v(4)
		$s = 14.4 \times 3 + \frac{1}{2} \times 7.2 \times 3^2$	D*		For using $s = ut + \frac{1}{2} \times 7.2t^2$ with non-zero u (s = 75.6)
		$19.2 + 75.6$	M1		For adding distances for the two distinct stages
		Displacement is 94.8m	A1		
		OR			
		$v = \int 7.2dt$	D*		For finding v(4)
		t = 0, v = 14.4, c = 14.4	M1		Integration and finding non-zero integration constant Nb Using t=4, v=14.4 gives c = -14.4
		$s = \int 7.2t + 14.4dt$			$s = \int 7.2t - 14.4dt$
	t = 0, s = 0, k = 0		Integration and finding integration constant. Nb t=4 with s=19.2 and v=7.2t-14.4 gives k=19.2		
$s = 3.6 \times 3^2 + 14.4 \times 3$	M1	Substituting t = 3 (OR 7 into $s = 3.6t^2 - 14.4t + 19.2$ ) (s=75.6) (OR $s = 3.6 \times 7^2 - 14.4 \times 7 + 19.2$ )			
$19.2 + 75.6 = 94.8$	A1	Adding two distinct stages OR			
Displacement is 94.8m	M1 A1	$s = 3.6 \times 7^2 - 14.4 \times 7 + 19.2 = 94.8$ final M1A1			

6	(i)	$\frac{1}{2} 25v_m = 8$ or $\frac{1}{2} T v_m + \frac{1}{2} (25 - T) v_m =$	B*1	Do not accept solution based on isosceles or right angled triangle
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	8			
	Greatest speed is	D*B	2	
	0.64	1		
	ms <sup>-1</sup>			
(ii)		M1		For using $v = u + at$ or the idea that gradient represents acceleration
	$V = 0.02 \times 40$	A1		
	$V = 0.8$	A1	3	
(iii)		M1		For using the idea that the area represents displacement. nb trapezium area is $16+8+8$
		M1		For $A = \frac{1}{2}(L_1 + L_2)h$ or other appropriate breakdown
	$\frac{1}{2}(70 + T) \times 0.8 = 40 - 8$	A1ft		$\frac{1}{2}(30 + T) \times 0.8 = 40 - 8 - \frac{1}{2} \times 40 \times 0.8$ ft cv(0.8)
	8			
	Duration is 10s	A1	4	
(iv)		M1		For using $v = u + at$ or the idea that gradient represents acceleration
	$0 = 0.8 + a(30 - 10)$	A1ft		ft cv(10) and cv(0.8)
	Deceleration is	A1	3	Accept -0.04 from correct work
	$0.04\text{ms}^{-2}$			
	Or	M1		Using the idea that the area represents displacement.
	$40 - 8 - \frac{1}{2} \times 40 \times 0.8 - 10 \times 0.8$	A1ft		Ft cv(0.8 and 10)
	$= 0.8(30 - 10) - a(30 - 10)^2/2$	A1		Accept -0.04 from correct work. d=-0.04 A0
	Deceleration is			
	$0.04\text{ms}^{-2}$			

7	(i)	$R = 0.5g\cos 40^\circ$	B1	$R = 3.7536$	
		$F = 0.6 \times 0.5g\cos 40^\circ$	M1	For using $F = \mu R$	
		Magnitude is 2.25N AG	A1	3	
	(ii)		M1	For applying Newton's second law (either case) //slope, two forces	
		$-/+0.5g\sin 40^\circ - F = 0.5a$	A1	Either case	
		(a) Acceleration is – $10.8\text{ms}^{-2}$	A1	Accept 10.8 from correct working (both forces have the same sign)	
		(b) Acceleration is $1.79\text{ms}^{-2}$	A1	4	Accept -1.79 from correct working (the forces have opposite sign) Accept ! 1.8(0)
	(iii)a)	$0 = 4 + (-10.8)T_1$	M1	Requires appropriate sign	
		$T_1 = 0.370(3)$	A1	Accept 0.37	
	b)		M1	For complete method of finding distance from A to highest point using a(up) with appropriate sign	
		$0 = 4^2 + 2(-10.8)s$ or $s = (0 + 4) \times 0.37/2$ or $s = 4(0.370) + \frac{1}{2}(-10.8)(0.370)^2$	A1 ft	ft a(up) and/or $T_1$ ( $s = 0.7405$ )	
			M1	For method of finding time taken from highest point to A and not using a(up)	
$0.7405 = \frac{1}{2}(1.79)T_2^2$		A1ft	ft a(down) and cv(0.7405) ( $T_2 = 0.908$ approx)		
$0.370 + 0.908 = 1.28\text{s}$		M1 A1	Using $T = T_1 + T_2$ with different values for $T_1, T_2$ 3 significant figures cao	8	