

ADVANCED SUBSIDIARY GCE UNIT MATHEMATICS

4721/01

Core Mathematics 1 **TUESDAY 16 JANUARY 2007**

Morning

Time: 1 hour 30 minutes

Additional Materials: Answer Booklet (8 pages) List of Formulae (MF1)

INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer all the questions.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are not permitted to use a calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- The total number of marks for this paper is 72.

ADVICE TO CANDIDATES

- Read each question carefully and make sure you know what you have to do before starting your answer.
- You are reminded of the need for clear presentation in your answers.



WARNING

You are not allowed to use a calculator in this paper.

This document consists of 4 printed pages.

1 Express $\frac{5}{2-\sqrt{3}}$ in the form $a+b\sqrt{3}$, where a and b are integers. [3]

2 Evaluate

(i)
$$6^0$$
, [1]

(ii)
$$2^{-1} \times 32^{\frac{4}{5}}$$
. [3]

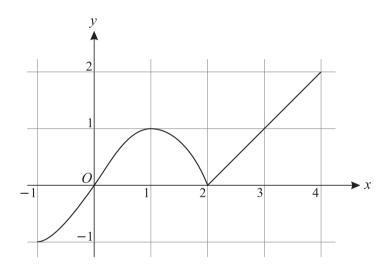
3 Solve the inequalities

(i)
$$3(x-5) \le 24$$
, [2]

(ii)
$$5x^2 - 2 > 78$$
.

4 Solve the equation $x^{\frac{2}{3}} + 3x^{\frac{1}{3}} - 10 = 0$. [5]

5



The graph of y = f(x) for $-1 \le x \le 4$ is shown above.

(i) Sketch the graph of
$$y = -f(x)$$
 for $-1 \le x \le 4$. [2]

- (ii) The point P(1, 1) on y = f(x) is transformed to the point Q on y = 3f(x). State the coordinates of Q.
- (iii) Describe the transformation which transforms the graph of y = f(x) to the graph of y = f(x + 2). [2]

6 (i) Express
$$2x^2 - 24x + 80$$
 in the form $a(x - b)^2 + c$. [4]

(ii) State the equation of the line of symmetry of the curve
$$y = 2x^2 - 24x + 80$$
. [1]

(iii) State the equation of the tangent to the curve $y = 2x^2 - 24x + 80$ at its minimum point. [1]

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7 Find $\frac{dy}{dx}$ in each of the following cases.

(i)
$$y = 5x + 3$$

(ii)
$$y = \frac{2}{x^2}$$
 [3]

(iii)
$$y = (2x+1)(5x-7)$$
 [4]

- 8 (i) Find the coordinates of the stationary points of the curve $y = 27 + 9x 3x^2 x^3$. [6]
 - (ii) Determine, in each case, whether the stationary point is a maximum or minimum point. [3]
 - (iii) Hence state the set of values of x for which $27 + 9x 3x^2 x^3$ is an increasing function. [2]
- 9 A is the point (2, 7) and B is the point (-1, -2).
 - (i) Find the equation of the line through A parallel to the line y = 4x 5, giving your answer in the form y = mx + c.
 - (ii) Calculate the length of AB, giving your answer in simplified surd form. [3]
 - (iii) Find the equation of the line which passes through the mid-point of AB and which is perpendicular to AB. Give your answer in the form ax + by + c = 0, where a, b and c are integers. [6]
- **10** A circle has equation $x^2 + y^2 + 2x 4y 8 = 0$.
 - (i) Find the centre and radius of the circle. [3]
 - (ii) The circle passes through the point (-3, k), where k < 0. Find the value of k. [3]
 - (iii) Find the coordinates of the points where the circle meets the line with equation x + y = 6. [6]

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