















7.

Figure 1

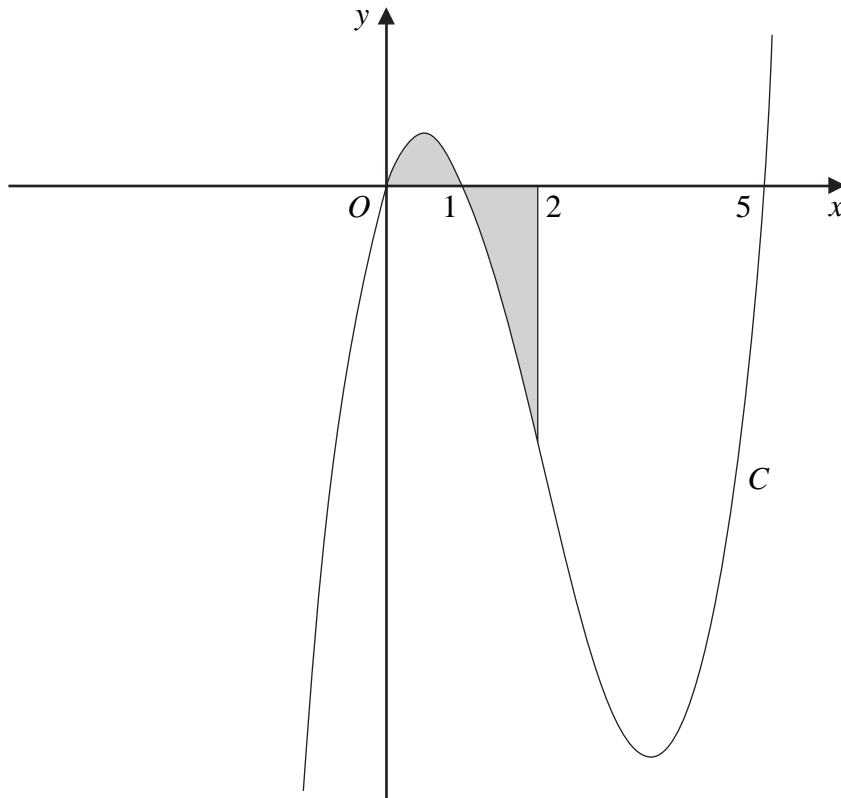


Figure 1 shows a sketch of part of the curve  $C$  with equation

$$y = x(x - 1)(x - 5).$$

Use calculus to find the total area of the finite region, shown shaded in Figure 1, that is between  $x = 0$  and  $x = 2$  and is bounded by  $C$ , the  $x$ -axis and the line  $x = 2$ .

(9)

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8. A diesel lorry is driven from Birmingham to Bury at a steady speed of  $v$  kilometres per hour. The total cost of the journey, £ $C$ , is given by

$$C = \frac{1400}{v} + \frac{2v}{7}.$$

(a) Find the value of  $v$  for which  $C$  is a minimum. (5)

(b) Find  $\frac{d^2C}{dv^2}$  and hence verify that  $C$  is a minimum for this value of  $v$ . (2)

(c) Calculate the minimum total cost of the journey. (2)

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9.

Figure 2

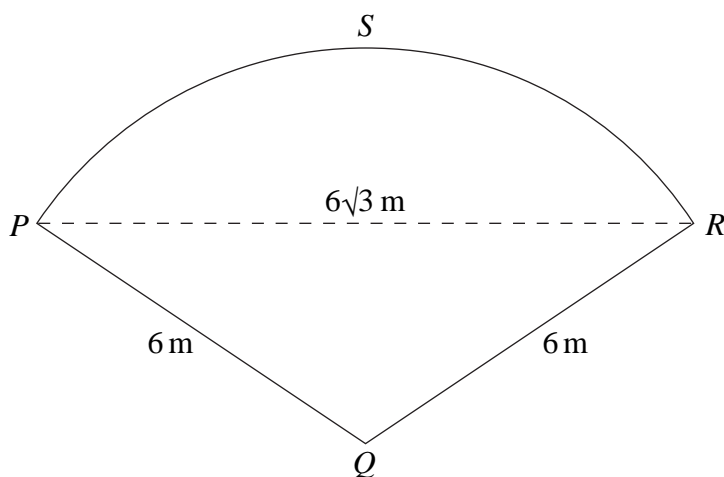


Figure 2 shows a plan of a patio. The patio  $PQRS$  is in the shape of a sector of a circle with centre  $Q$  and radius  $6\text{ m}$ .

Given that the length of the straight line  $PR$  is  $6\sqrt{3}\text{ m}$ ,

- (a) find the exact size of angle  $PQR$  in radians. (3)
- (b) Show that the area of the patio  $PQRS$  is  $12\pi\text{ m}^2$ . (2)
- (c) Find the exact area of the triangle  $PQR$ . (2)
- (d) Find, in  $\text{m}^2$  to 1 decimal place, the area of the segment  $PRS$ . (2)
- (e) Find, in  $\text{m}$  to 1 decimal place, the perimeter of the patio  $PQRS$ . (2)

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