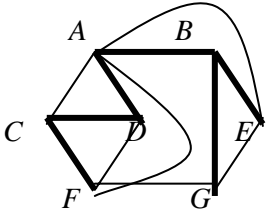


4736 Decision Mathematics 1

1	(i)	5 2 4 3 8 Bin 1: 5 2 3 Bin 2: 4 Bin 3: 8	M1 A1	First bin correct All correct in three bins	[2]
	(ii)	8 5 4 3 2 Bin 1: 8 2 Bin 2: 5 4 Bin 3: 3	M1 A1	First bin correct All correct in three bins	[2]
	(iii)	The heaviest box is originally at the bottom of the stack	B1	Referring to the physical act of sorting the weights into decreasing order	[1]
	(iv)	Bins in any order and boxes in any order Bin 1: 8 or 8 Bin 2: 5 3 5 2 Bin 3: 4 2 4 3	B1	Any valid packing into three bins of capacity 8 kg.	[1]
Total = 6					

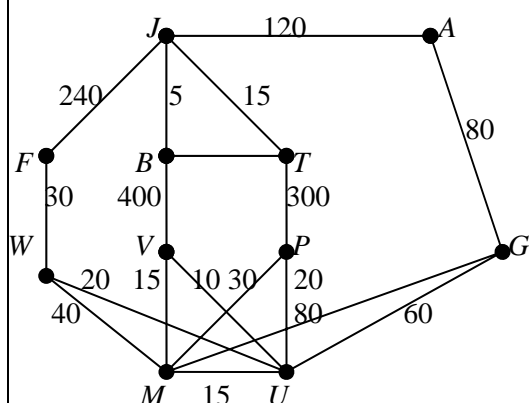
2	(i)	<p>4 moves</p>	M1 A1 B1	A connected graph with nine vertices labelled 1 to 9 Correct graph Stating 4	[3]
	(ii)	<p>Neither</p> <p>It has four odd nodes</p> <p>The nodes 2, 4, 6, 8 each have three arcs joined to them whereas an Eulerian graph has no odd nodes and a semi-Eulerian graph has exactly two odd nodes</p>	M1 A1	<p>‘Neither’, together with an attempt at a reason</p> <p>A correct reference to the number of odd nodes for this graph. Be careful about whether ‘odd’ refers to the parity or the value.</p> <p>However, just defining Eulerian and semi-Eulerian, without reference to this graph, is not enough</p>	[2]
Total = 5					

ANSWERED ON INSERT

3	(i)	<p> $AD = 16$ $CD = 18$ $CF = 21$ $AC = 23$ $DF = 34$ $BE = 35$ $BG = 46$ $AB = 50$ $EG = 55$ $FG = 58$ $AE = 80$ $AF = 100$ </p>  <p>Total weight = 186</p>	<p>M1 A1</p> <p>M1 A1</p> <p>B1</p>	<p>Using Kruskal: Not selecting AC and DF Selecting correct arcs in list, or implied (16+18+21+35+46+50, in this order with no others, can imply M1, A1)</p> <p>Drawing a spanning tree for these six vertices Correct (minimum) spanning tree drawn</p> <p>186 (cao)</p>	[5]
	(ii)	<p>Delete BG from spanning tree $186 - 46 = 140$</p> <p>Two shortest arcs from G are BG and EG $140 + 46 + 55 = 241$ Lower bound = 241</p>	<p>B1</p> <p>M1 A1</p>	<p>Correct working for wrong vertex deleted can score B1, M1, A0</p> <p>Weight of MST on reduced network (ft from part (i))</p> <p>Adding two shortest arcs to MST 241 (cao)</p>	[3]
	(iii)	<p>$A-D-C-F-G- \dots$ or $16+18+21+58+ \dots$ $A-D-C-F-G-B-E-A$</p> <p>Upper bound = 274</p>	<p>M1 A1</p> <p>B1</p>	<p>Using nearest neighbour Correct closed tour listed, not just weights added 274 (cao)</p>	[3]
Total = 11					

ANSWERED ON INSERT

4 (i)



Strictly, these are directed arcs, but they are shown as undirected arcs

J	<table><tr><td>1</td><td>0</td></tr><tr><td colspan="2"></td></tr></table>	1	0			A	<table><tr><td>4</td><td>120</td></tr><tr><td colspan="2">120</td></tr></table>	4	120	120							
1	0																
4	120																
120																	
F	<table><tr><td>6</td><td>240</td></tr><tr><td colspan="2">240</td></tr></table>	6	240	240		B	<table><tr><td>2</td><td>5</td></tr><tr><td colspan="2">5</td></tr></table>	2	5	5		T	<table><tr><td>3</td><td>15</td></tr><tr><td colspan="2">15</td></tr></table>	3	15	15	
6	240																
240																	
2	5																
5																	
3	15																
15																	
		V	<table><tr><td></td><td></td></tr><tr><td colspan="2">405</td></tr></table>			405		P	<table><tr><td></td><td></td></tr><tr><td colspan="2">315</td></tr></table>			315					
405																	
315																	
W	<table><tr><td>8</td><td></td></tr><tr><td colspan="2">270</td></tr></table>	8		270				G	<table><tr><td>5</td><td>200</td></tr><tr><td colspan="2">200</td></tr></table>	5	200	200					
8																	
270																	
5	200																
200																	
		M	<table><tr><td>9</td><td>275</td></tr><tr><td colspan="2">280 275</td></tr></table>	9	275	280 275		U	<table><tr><td>7</td><td>260</td></tr><tr><td colspan="2">260</td></tr></table>	7	260	260					
9	275																
280 275																	
7	260																
260																	

Alternatively, if treating as undirected:
J, A, F, B and T are unchanged, then

Or $V = 8^{\text{th}}$
and $W = 9^{\text{th}}$

Or $V = 8^{\text{th}}$
and $W = 9^{\text{th}}$

W	<table> <tr> <td>8</td> <td>270</td> </tr> <tr> <td colspan="2">270</td> </tr> </table>	8	270	270		V	<table> <tr> <td>9</td> <td>270</td> </tr> <tr> <td colspan="2">405 270</td> </tr> </table>	9	270	405 270		P	<table> <tr> <td></td> <td></td> </tr> <tr> <td colspan="2">315 280</td> </tr> </table>			315 280	
8	270																
270																	
9	270																
405 270																	
315 280																	
M	<table> <tr> <td>10</td> <td>275</td> </tr> <tr> <td colspan="2">280 275</td> </tr> </table>	10	275	280 275		U	<table> <tr> <td>7</td> <td>260</td> </tr> <tr> <td colspan="2">260</td> </tr> </table>	7	260	260		G	<table> <tr> <td>5</td> <td>200</td> </tr> <tr> <td colspan="2">200</td> </tr> </table>	5	200	200	
10	275																
280 275																	
7	260																
260																	
5	200																
200																	

Route: J - A - G - U - M

B1

Times for flying route,
JA = 120 AG = 80
GU = 60 UM = 15 GM = 80

B1

Times for train route correct
JT = 15 JB = 5 BT = 20
TP = 300 PU = 20 PM = 30

B1

Times for coach route and driving route correct
BV = 400 VU = 10 VM = 15
JF = 240 FW = 30 WU = 20 WM = 40

[3]

Follow through their arc weights
if reasonable

M1

Permanent values correct at A, F, B, T
A = 120, F = 240, B = 5, T = 15

M1 d

Both 280 and 275 seen at M
(updating at M)

A1 ft

All temporary labels correct (or implied)
and no extras

B1 ft

All permanent labels correct (or implied)
(condone labelling past M)

B1 ft

Order of labelling correct
(condone labelling past M)

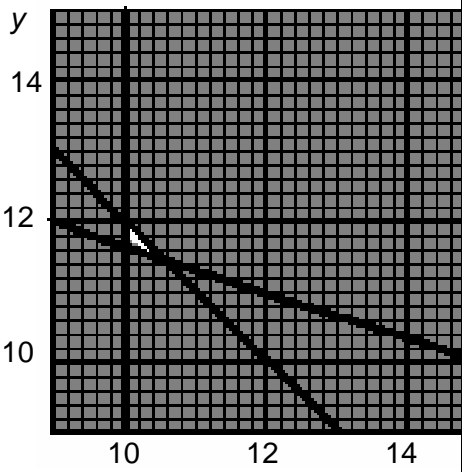
Marked as above

B1

Correct answer only

[6]

(ii)	The quickest journey time from Jenny's house to the meeting venue	B1	Quickest journey / least travel time or equivalent	[1]
(iii)	Does not allow for waiting for connections There may be delays at the airport She may not want to fly because of the 'carbon footprint' She may want to choose the cheapest route rather than the quickest route She may not like flying She may want to see her friend She may want to break the journey overnight	B1 B1	Any reasonable suggestion for why she may not want to use the drive/fly/underground route or why she may want to use a different route Any second reasonable suggestion	[2]
Total = 12				

5	(i)	x = area of wall to be panelled (m^2) y = area to be painted z = area to be covered with pinboard	B1 B1	Reference to area or m^2 (at least once) Identifying x as panelling, y as paint and z as pinboard, in any way	[2]
	(ii)	Cost \leq £150 $\Rightarrow 8x + 4y + 10z \leq 150$ $\Rightarrow 4x + 2y + 5z \leq 75$ (given)	B1 B1	Use of word 'cost' or equivalent $8x + 4y + 10z \leq 150$ seen or explicitly referred to	[2]
	(iii)	(Minimise $P \Rightarrow$) $15x + 30y + 20z$	B1 ft	Any positive multiple of this eg $3x + 6y + 4z$ or $\frac{1}{4}x + \frac{1}{2}y + \frac{1}{3}z$	[1]
	(iv)	(Minimise $P = 480 +$) $- 5x + 10y$ Subject to $x + 3y \geq 45$ $x \geq 10$ $y \geq 0$ $x + y \leq 22$	B1 ft B1 B1	Any positive multiple of this, eg $2y - x (+ c)$ - or maximise a negative multiple Any equivalent simplified form $x \geq 10$ may be implied $y \geq 0$ may be implied $x + y \leq 22$, any equivalent simplified form	[3]
	(v)		M1 M1 M1 A1	ANSWERED ON GRAPH PAPER $x = 10$ drawn accurately with a sensible scale $x + y = 22$ drawn accurately with a sensible scale Their $x + 3y = 45$ drawn accurately with a sensible scale Shading correct or identification of the feasible region (triangle with $(10, 11\frac{2}{3})$, $(10, 12)$ and $(10\frac{1}{2}, 11\frac{1}{2})$ as vertices)	[4]
Total = 12					

6	(i)	<table><tr><td>P</td><td>x</td><td>y</td><td>z</td><td>s</td><td>t</td><td></td></tr><tr><td>1</td><td>-25</td><td>-14</td><td>32</td><td>0</td><td>0</td><td>0</td></tr><tr><td>0</td><td>6</td><td>-4</td><td>3</td><td>1</td><td>0</td><td>24</td></tr><tr><td>0</td><td>5</td><td>-3</td><td>10</td><td>0</td><td>1</td><td>15</td></tr></table>	P	x	y	z	s	t		1	-25	-14	32	0	0	0	0	6	-4	3	1	0	24	0	5	-3	10	0	1	15	B1	Rows and columns may be in any order	[2]
		P	x	y	z	s	t																										
		1	-25	-14	32	0	0	0																									
		0	6	-4	3	1	0	24																									
0	5	-3	10	0	1	15																											
	B1	Objective row with -25, -14, 32																															
		Constraint rows correct (condone omission of P column)																															
	(ii)	x column has a negative value in objective row	B1	‘negative in top row’, ‘-25’, or similar	[3]																												
		Cannot use y column since it has negative entries in all the other rows	B1	‘most negative in top row’ \Rightarrow bod B1																													
		$24 \div 6 = 4$ $15 \div 5 = 3$	B1	Correct reason for not choosing y column																													
		Least non-negative ratio is 3, so pivot on 5		Both divisions seen and correct choice made (or both divisions seen and correct choice implied from pivoting)																													
	(iii)	<table><tr><td>1</td><td>0</td><td>-29</td><td>82</td><td>0</td><td>5</td><td>75</td></tr><tr><td>0</td><td>0</td><td>-0.4</td><td>-9</td><td>1</td><td>-1.2</td><td>6</td></tr><tr><td>0</td><td>1</td><td>-0.6</td><td>2</td><td>0</td><td>0.2</td><td>3</td></tr></table>	1	0	-29	82	0	5	75	0	0	-0.4	-9	1	-1.2	6	0	1	-0.6	2	0	0.2	3	M1	Follow through their sensible tableau (with two slack variable columns) and pivot	[2]							
		1	0	-29	82	0	5	75																									
		0	0	-0.4	-9	1	-1.2	6																									
		0	1	-0.6	2	0	0.2	3																									
		A1	Pivot row correct (no numerical errors) Other rows correct (no numerical errors)																														
		B1	Calculation for pivot row	[3]																													
		B1	Calculation for objective row																														
		B1	Calculation for other row																														
		B1 ft	x, y and z from their tableau	[2]																													
		B1 ft	P from their tableau, provided $P \geq 0$																														
	(iv)	Problem is unbounded	B1	Any one of these, or equivalent.	[1]																												
		No limit to how big y (and hence P) can be Only negative in objective row is y column, but all entries in this column are negative		If described in terms of pivot choices, must be complete and convincing																													
Total = 13																																	

$F = N \div B$ $G = \text{INT}(F)$ $H = B \times G$ $C = N - H$ $N = G$							For reference only		
7	(i)	F	G	H	C	N	M1	A reasonable attempt at first pass (presented in any form)	[5]
		2.5	2	4	1	2	A1	$F = 2.5$ and $G = 2$	
		1	1	2	0	1	A1	$H = 4$ (or double their G value) and $C = 5 -$ their H	
		0.5	0	0	1	0	A1	F, G, H, C and N correct for second pass (ft their N value)	
							A1	F, G, H, C and N correct for third pass (ft their N value)	
	(ii)	F	G	H	C	N	M1	A reasonable attempt	[4]
		-2.5	-3	-6	1	-3	M1 d	First pass correct (or implied)	
		-1.5	-2	-4	1	-2			
		-1	-1	-2	0	-1			
		-0.5	-1	-2	1	-1	A1	Reaching two lines with the same value for G	
		-0.5	-1	-2	1	-1		If described in words only, then M1 for a correct statement; M1 d for all correct statements (sufficient to guarantee result), and A1 for convincingly correct explanation of how they know these to be true and why the result follows	
		Does not terminate					B1	Saying ‘does not stop’, or equivalent	
	(iii)	F	G	H	C	N	M1	First pass correct	[4]
		3.7	3	30	7	3	A1	All correct	
		0.3	0	0	3	0			
		The first value is the units digit of N , the second value is the tens digit, the third value is the hundreds digit, and so on.					M1	Outputs are digits of N	
							A1	In reverse order	
Total = 13									