Mark Scheme

4752 (C2) Concepts for Advanced Mathematics

4752

| 1 | | $\frac{1}{2}x^2 + 3x^{-1} + c$ o.e. | 3 | 1 for each term | 3 |
|---|---------------|--|----------|--|---|
| 2 | (i) | 5 with valid method | 1 | eg sequence has period of 4 nos. | |
| | (ii) | 165 www | 2 | M1 for $13 \times (1 + 3 + 5 + 3) + 1 + 3 + 5$ or for $14 \times (1 + 3 + 5 + 3) - 3$ | 3 |
| 3 | | rt angled triangle with $\sqrt{2}$ on one side | 1 | or M1 for $\cos^2 \theta = 1 - \sin^2 \theta$ used | |
| | | Pythag. used to obtain remaining side $=\sqrt{7}$ | 1 | A1 for $\cos \theta = \frac{\sqrt{7}}{\sqrt{9}}$ | |
| | | $ \tan \theta = \frac{opp}{adj} = \frac{\sqrt{2}}{\sqrt{7}} \text{ o.e.} $ | 1 | A1 for $\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\sqrt{2}}{\sqrt{7}}$ o.e. | 3 |
| 4 | | radius = 6.5 [cm] | 3 | M1 for $\frac{1}{2} \times r^2 \times 0.4$ [= 8.45] o.e. | 3 |
| | | | | and M1 for $r^2 = \frac{169}{4}$ o.e. [= 42.25] | 5 |
| 5 | (i) | sketch of correct shape with P ($-0.5,2$) Q ($0,4$) and R ($2,2$) | 2 | 1 if Q and one other are correct | |
| | (ii) | sketch of correct shape with P $(-1,0.5)$ Q $(0,1)$ and R $(4,0.5)$ | 2 | 1 if Q and one other are correct | 4 |
| 6 | (i) | 205 | 3 | M1 for AP identified with $d = 4$ and M1 for $5 + 50 d$ used | |
| | (ii) | $\frac{25}{3}$ o.e. | 2 | M1 for $r = \frac{2}{5}$ o.e. | 5 |
| 7 | (i) | $\frac{\sin A}{\sin A} = \frac{\sin 79}{\sin 79}$ s.o.i. | M1 | | |
| | | 5.6 8.4 [A =] 40.87 to 41 | A1 | | |
| | (ii) | $[BC^{2} =] 5.6^{2} + 7.8^{2} - 2 \times 5.6 \times 7.8 \times$ | M1 | | |
| | | $\cos((180-79'))$ = 108.8 to 108.9 | A1 A1 | | 5 |
| | | [BC =] 10.4() | | | |
| 8 | | $y' = 3x^{-\frac{1}{2}}$ | M1 | condone if unsimplified | |
| | | $\frac{3}{4}$ when $x = 16$ | A1 | | |
| | | y = 24 when $x = 16y - their 24 = their 3/4 (x - 16)$ | B1 M1 | 4. | |
| | | $y - 24 = \frac{3}{4} (x - 16)$ o.e. | A1 | dependent on $\frac{dy}{dx}$ used for <i>m</i> | 5 |

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|------|---------|--|------|--|--------------|--|
| 9 | (i) | У 🛉 | G1 | for curve of correct shape in both | | |
| | | | | quadrants | | |
| | | | DC1 | must as through (0, 1) shows | | |
| | | | DGI | must go through (0, 1) shown | | |
| | | | | | | |
| | | X | | | | |
| | (ii) | $2x + 1 = \frac{\log 10}{\log 10}$ o.e. | M1 | or M1 for $2x + 1 = \log_3 10$ | 5 | |
| | | log 3 | A2 | A1 for other versions of 0.547or 0.548 | | |
| | | [x =] 0.55 | | | | |
| 10 | (i) | $3x^2 - 6x - 9$ | M1 | | | |
| | | use of their $y' = 0$ | M1 | | | |
| | | x = -1 | | | | |
| | | x = 3 | M1 | | | |
| | | of turning point | | | | |
| | | max at $x = -1$ and min at $x = 3$ | A1 | c.a.o. | 6 | |
| | | | | | | |
| | (ii) | $x(x^2 - 3x - 9)$ | M1 | | | |
| | | $3\pm\sqrt{45}$ 3.2 9 | | | | |
| | | $\frac{1}{2}$ or $(x - \frac{3}{2})^2 = 9 + \frac{1}{4}$ | M1 | | | |
| | | $3\sqrt{45}$ | | | | |
| | | $0, \frac{5}{2} \pm \frac{\sqrt{45}}{2}$ o.e. | AI | | 3 | |
| | | | | | | |
| | | sketch of cubic with two turning | G1 | | | |
| | () | points correct way up | | | | |
| | | x-intercepts – negative, 0, positive | DG1 | | 2 | |
| | | shown | | | | |
| 11 | (i) | 47.625 $[m^2]$ to 3 sf or more, with | 4 | M3 for $\frac{1.5}{1.5}$ × (2.3 + 2 + 2)(2.7 + 3.3 + 4 + | | |
| | | correct method shown | | $\frac{1}{2}$ x (2.5 + 2 + 2[2.7 + 5.5 + 4 + | 4 | |
| | | | | 4.8 + 5.2 + 5.2 + 4.4]) | | |
| | | 12.05 | | | | |
| | (11) | 43.05 | 2 | M1 IOF 1.5 \times (2.2+2.7+2.2+4+4.8+5.2+4.4+2) | 2 | |
| | | | | $1.3 \land (2.3+2.7+3.3+4+4.8+3.2+4.4+2)$ | | |
| | (iii) | $-0.013x^{4}/4 + 0.16x^{3}/3 - 0.082x^{2}/2 +$ | M2 | M1 for three terms correct | | |
| | Ì | 2.4 <i>x</i> o.e. | | | | |
| | | their integral evaluated at $x = 12$ (and | M1 | dep on integration attempted | | |
| | | 0) only | | | | |
| | | 47.6 to 47.7 | A1 | | 4 | |
| | (i-1) | 5.30 found | 1 | | | |
| | (1) | compared with 5.2 s.o.i | | | 2 | |
| | | compared with 5.2 s.o.i. | | | 2 | |
| 12 | (i) | $\log P = \log a + bt$ www | 1 | | | |
| | | comparison with $y = mx + c$ s.o.i. | 1 | must be with correct equation | | |
| | | intercept = $\log_{10} a$ | 1 | dependent on correct equation | 3 | |
| | | | | | | |
| | (ii) | [2.12, 2.21], 2.32, 2.44, 2.57, 2.69 | 1 | | | |
| | | plots ft miled line of best fit | | P_{atwaan} (10, 2,08) and (10, 2,12) | 2 | |
| | | ruled line of dest fit | 1 | between (10, 2.08) and (10, 2.12) | 3 | |
| | | | | | | |

| (iii) $0.0100 \le m < 0.0125$ $a = 10^{c}$ or $\log a = c$ $P = 10^{c} \times 10^{mt}$ or 10^{mt+c} B1 $M1$ for $\frac{y - \text{step}}{x - \text{step}}$ B1 $1.96 \le c \le 2.02$ B1 f.t. their m and a | | | | | |
|--|-------|---|----------|--|---|
| $a = 10^c$ or $loga = c$ $B1$ $1.96 \le c \le 2.02$ 4 $P = 10^c \times 10^{mt}$ or 10^{mt+c} $B1$ $f.t.$ their m and a 4 | (iii) | $0.0100 \le m < 0.0125$ | B2 | M1 for $\frac{y - \text{step}}{x - \text{step}}$ | |
| $P = 10^{\rm c} \times 10^{\rm mt}$ or $10^{\rm mt+c}$ B1 f.t. their m and a | | $a = 10^{c}$ or $loga = c$ | B1 | $1.96 \le c \le 2.02$ | |
| | | $P = 10^{\rm c} \times 10^{\rm mt} \text{ or } 10^{\rm mt+c}$ | B1 | f.t. their m and a | 4 |
| (iv) use of $t = 105$ 1.0 - 2.0 billion approx B1 B1 | (iv) | use of $t = 105$ 1.0 – 2.0 billion approx | B1 B1 | | |
| unreliable since extrapolation o.e. E1 3 | | unreliable since extrapolation o.e. | E1 | | 3 |