



1.  $f(x) = x^4 + x^3 + 2x^2 + ax + b$

where  $a$  and  $b$  are constants.

When  $f(x)$  is divided by  $(x - 1)$ , the remainder is 7.

(a) Show that  $a + b = 3$ . (2)

When  $f(x)$  is divided by  $(x + 2)$ , the remainder is  $-8$ .

(b) Find the value of  $a$  and the value of  $b$ . (5)

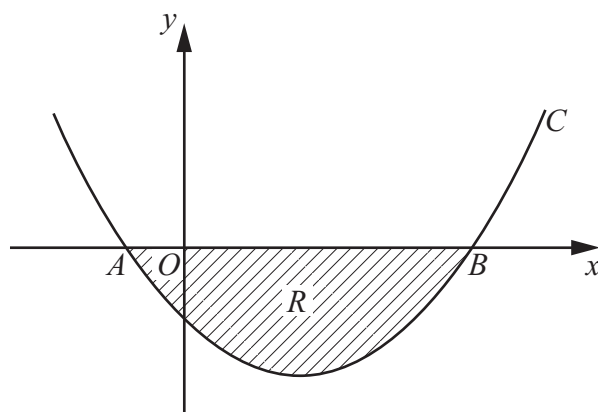
Lined area for writing answers.







4.



**Figure 1**

Figure 1 shows a sketch of part of the curve  $C$  with equation

$$y = (x + 1)(x - 5)$$

The curve crosses the  $x$ -axis at the points  $A$  and  $B$ .

- (a) Write down the  $x$ -coordinates of  $A$  and  $B$ . **(1)**

The finite region  $R$ , shown shaded in Figure 1, is bounded by  $C$  and the  $x$ -axis.

- (b) Use integration to find the area of  $R$ . **(6)**

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5. Given that  $\binom{40}{4} = \frac{40!}{4!b!}$ ,

- (a) write down the value of  $b$ . **(1)**

In the binomial expansion of  $(1+x)^{40}$ , the coefficients of  $x^4$  and  $x^5$  are  $p$  and  $q$  respectively.

- (b) Find the value of  $\frac{q}{p}$ . **(3)**

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6.

$$y = \frac{5}{3x^2 - 2}$$

(a) Complete the table below, giving the values of  $y$  to 2 decimal places.

$x$	2	2.25	2.5	2.75	3
$y$	0.5	0.38			0.2

(2)

(b) Use the trapezium rule, with all the values of  $y$  from your table, to find an

approximate value for  $\int_2^3 \frac{5}{3x^2 - 2} dx$ .

(4)

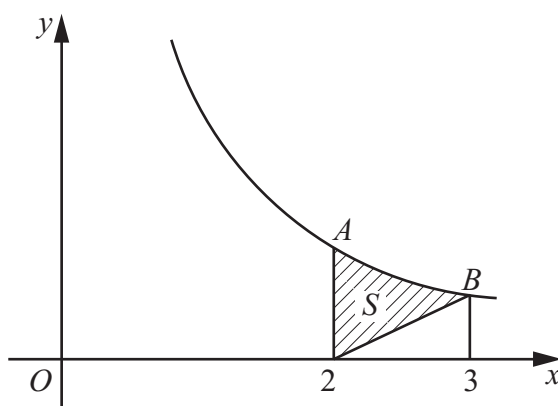


Figure 2

Figure 2 shows a sketch of part of the curve with equation  $y = \frac{5}{3x^2 - 2}$ ,  $x > 1$ .

At the points  $A$  and  $B$  on the curve,  $x = 2$  and  $x = 3$  respectively.

The region  $S$  is bounded by the curve, the straight line through  $B$  and  $(2, 0)$ , and the line through  $A$  parallel to the  $y$ -axis. The region  $S$  is shown shaded in Figure 2.

(c) Use your answer to part (b) to find an approximate value for the area of  $S$ .

(3)

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7. (a) Show that the equation

$$3 \sin^2 x + 7 \sin x = \cos^2 x - 4$$

can be written in the form

$$4 \sin^2 x + 7 \sin x + 3 = 0$$

(2)

(b) Hence solve, for  $0 \leq x < 360^\circ$ ,

$$3 \sin^2 x + 7 \sin x = \cos^2 x - 4$$

giving your answers to 1 decimal place where appropriate.

(5)

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8. (a) Sketch the graph of  $y = 7^x$ ,  $x \in \mathbb{R}$ , showing the coordinates of any points at which the graph crosses the axes.

**(2)**

- (b) Solve the equation

$$7^{2x} - 4(7^x) + 3 = 0$$

giving your answers to 2 decimal places where appropriate.

**(6)**



9. The points  $A$  and  $B$  have coordinates  $(-2, 11)$  and  $(8, 1)$  respectively.

Given that  $AB$  is a diameter of the circle  $C$ ,

(a) show that the centre of  $C$  has coordinates  $(3, 6)$ , **(1)**

(b) find an equation for  $C$ . **(4)**

(c) Verify that the point  $(10, 7)$  lies on  $C$ . **(1)**

(d) Find an equation of the tangent to  $C$  at the point  $(10, 7)$ , giving your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are constants. **(4)**

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