

Mathematics

Advanced GCE

Unit **4732**: Probability and Statistics 1

Mark Scheme for January 2012

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Any enquiries about publications should be addressed to:

OCR Publications
PO Box 5050
Annesley
NOTTINGHAM
NG15 0DL

Telephone: 0870 770 6622
Facsimile: 01223 552610
E-mail: publications@ocr.org.uk

Annotations and abbreviations

Annotation in scoris	Meaning
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Subject-specific Marking Instructions for GCE Mathematics (OCR) Statistics strand

- a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

Candidates are expected to give numerical answers to an appropriate degree of accuracy. 3 significant figures may often be the norm for this, but this always needs to be considered in the context of the problem in hand. For example, in quoting probabilities from Normal tables, we generally expect *some* evidence of interpolation and so quotation to 4 decimal places will often be appropriate. But even this does not always apply – quotations of the standard critical points for significance tests such as 1.96, 1.645, 2.576 (maybe even 2.58 – but not 2.57) will commonly suffice, especially if the calculated value of a test statistic is nowhere near any of these values. Sensible discretion *must* be exercised in such cases.

Discretion must also be exercised in the case of small variations in the degree of accuracy to which an answer is given. For example, if 3 significant figures are expected (either because of an explicit instruction or because the general context of a problem demands it) but only 2 are given, loss of an accuracy ("A") mark is likely to be appropriate; but if 4 significant figures are given, this should not normally be penalised. Likewise, answers which are slightly deviant from what is expected in a very minor manner (for example a Normal probability given, after an attempt at interpolation, as 0.6418 whereas 0.6417 was expected) should not be penalised. However, answers which are *grossly* over- or under-specified should normally result in the loss of a mark. This includes cases such as, for example, insistence that the value of a test statistic is (say) 2.128888446667 merely because that is the value that happened to come off the candidate's calculator. Note that this applies to answers that are given as final stages of calculations; intermediate working should usually be carried out, and quoted, to a greater degree of accuracy to avoid the danger of premature approximation.

The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h Genuine misreading (of numbers or symbols, occasionally even of text) occurs. If this results in the object and/or difficulty of the question being considerably changed, it is likely that all the marks for that question, or section of the question, will be lost. However, misreads are often such that the object and/or difficulty remain substantially unaltered; these cases are considered below.

The simple rule is that *all* method ("M") marks [and of course all independent ("B") marks] remain accessible but at least some accuracy ("A") marks do not. It is difficult to legislate in an overall sense beyond this global statement because misreads, even when the object and/or difficulty remains unchanged, can vary greatly in their effects. For example, a misread of 1.02 as 10.2 (perhaps as a quoted value of a sample mean) may well be catastrophic; whereas a misread of 1.6748 as 1.6746 may have so slight an effect as to be almost unnoticeable in the candidate's work.

A misread should normally attract *some* penalty, though this would often be only 1 mark and should rarely if ever be more than 2. Commonly in sections of questions where there is a numerical answer either at the end of the section or to be obtained and commented on (eg the value of a test statistic), this answer will have an "A" mark that may actually be designated as "cao" [correct answer only]. This should be interpreted *strictly* – if the misread has led to failure to obtain this value, then this "A" mark must be withheld even if all method marks have been earned. It will also often be the case that such a mark is implicitly "cao" even if not explicitly designated as such.

On the other hand, we commonly allow "fresh starts" within a question or part of question. For example, a follow-through of the candidate's value of a test statistic is generally allowed (and often explicitly stated as such within the marking scheme), so that the candidate may exhibit knowledge of how to compare it with a critical value and draw conclusions. Such "fresh starts" are not affected by any earlier misreads. A misread may be of a symbol rather than a number – for example, an algebraic symbol in a mathematical expression. Such misreads are more likely to bring about a considerable change in the object and/or difficulty of the question; but, if they do not, they should be treated as far as possible in the same way as numerical misreads, *mutatis mutandis*. This also applied to misreads of text, which are fairly rare but can cause major problems in fair marking.

The situation regarding any particular cases that arise while you are marking for which you feel you need detailed guidance should be discussed with your Team Leader.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Note: "(3 sf)" means "answer which rounds to ... to 3 sf". If correct ans seen to ≥ 3 sf, ISW for later rounding
 Penalise over-rounding only once in paper. NB If marking by question and over-rounding is seen, must mark whole paper.

Question		Answer	Marks	Guidance	
1	(i)	$0.1 + 0.3 + 2p + p = 1$ oe $p = 0.2$	M1 A1 [2]		
1	(ii)	$\sum xp$ $= 2.7$ oe	M1 A1f [2]	≥ 2 terms correct, FT p	eg $\div 4$: M0A0
2	(i)	x because values (or depths) are fixed (or controlled or chosen or predetermined or manipulated or given oe) because they can be changed or it is changed or because it is not measured ie not "read off" oe or because we change the values ourselves	B1 [1]	Allow "because it goes up in intervals" or "because it is taken at set intervals" Ignore all else NB " x is changed" B1, but " x changes" B0	NOT: x , as values are constant x , as y depends on x x as % sand depends on depth Depth, as not affected by % sand content x , as it is not dependent x , because y is measured x , because it changes y , which is the depth and this is controlled
2	(ii)	$S_{xx} = 7344 - \frac{216^2}{9}$ (= 2160) $S_{yy} = 30595 - \frac{512.4^2}{9}$ (= 1422.36) $S_{xy} = 10674 - \frac{216 \times 512.4}{9}$ (= - 1623.6) $r = \frac{-1623.6}{\sqrt{2160 \times 1422.36}}$ $= -0.926$ (3 sfs)	M1 M1 A1 [3]	correct subst in any S formula correct subst in all S s & in r	

Question		Answer	Marks	Guidance
2	(iii) (a)	$b = \frac{-1623.6}{2160}$ or $-0.75\dots$ or $-\frac{451}{600}$ $y - \frac{512.4}{9} = "-0.75\dots"(x - \frac{216}{9})$ $y = -0.75x + 75(.0)$ (2 sf) or $y = -\frac{451}{600}x + \frac{5623}{75}$	M1 M1 A1 [3]	ft S_{xy} & S_{xx} from (ii) or $a = \frac{512.4}{9} - 0.75\dots \times (-\frac{216}{9})$ or $\frac{5623}{75}$ 2 sf is enough Allow $y = -0.75x + (-75)$ If ans to (i) is y, & x on y found here: $b' = \frac{-1623.6}{1422.36}$ (= -1.14) M1 $x - \frac{216}{9} = "-1.14"(y - \frac{512.4}{9})$ M1 $x = -1.14y + 89(.0)$ A1 If ans to (i) is x, but x on y found here: B1 only for $x = -1.14y + 89(.0)$
2	(iii) (b)	r close to -1 (or high or strong), r close to 1 25 within range of data oe, so reliable 100 outside range of data oe, so unreliable Must give reasons Allow "accurate" instead of "reliable"	B1 B1 B1 [3]	Allow strong or good or high corr'n or rel'nship etc or so more reliable or so less reliable If (ii) $ r < 0.7$: poor corr'n oe B1f 25 unreliable B1f 100 unreliable B1f or strong neg corr'n. Award this mark even if comment linked to 100 instead of linked to 25. BUT: "r close to -1, so unreliable": B0 Can still score next marks if mention "within" and "outside range" or 100 gives neg %age "Reliable because r near -1" B1B0B0 "Small sample so unreliable" B0B0B0 Ignore all else
3	(i)	$(1 - 0.12)^{13}$ or $13 \times (1 - 0.12)^{12} \times 0.12$ $(1 - 0.12)^{13} + 13 \times (1 - 0.12)^{12} \times 0.12$ = 0.526 (3 sf)	M1 M1 A1[3]	Either seen Fully correct method 1 - correct terms: M1M0A0
3	(ii)	${}^{13}C_2 \times 0.12^2 \times (1 - 0.12)^{11}$ $2 \times "0.275275" \times (1 - "0.275275")$ = 0.399 (3 sf)	M1 M1 A1 [3]	or 0.275(...) Correct method except allow omit "2 x" Allow if x or + something NB unlike 2 nd M1 in (i) which is for fully correct method NB $2 \times 0.12 \times 0.88$: M0M0A0

Question		Answer	Marks	Guidance	
6	(i)	V	B1	X because mode = 1 oe or Highest prob is P(1) oe B2	For answer V the first B1 is indep, but not for other answers, ie: V with no reason or incorrect reason scores B1B0, but Z or X or any other letter with no reason or incorrect reason scores BOB0. In all cases, once mark(s) have been scored, ignore all other comments.
		because [probs or values or geometric or etc] decreasing or halving or Highest prob is 1st Allow if word “decreasing” or “halving” or “sloping downwards” or any equivalent seen NOT “Positive skew”	B1	Z because P(0) = 0 or variable can't be 0 oe Allow “Geo distr'n cannot be zero” oe B2 “None of them”: Ignore any reason given. B2	
6	(ii)	Y. Peaks at 2 Y. Like normal, peak at 2 Y. Highest prob is middle one (or is at 2) Y. P(X = 2) is max Y. Increase to 2 then decr Y. 1 4 6 4 1 alone or with $0.5^4 \times$ Y. 0.0625, 0.25, 0.375, 0.25, 0.0625 Y. P(1) = P(3) and P(2) is greater/different	B1B1B1	Ignore all else	If values of <u>some</u> probs listed: 2 to 4 values: B1 Y: B1 For 3 rd B1 must link list with Y diag, eg “symmetrical” or “peak in middle” or “peak at 2” or “1 st = last” or “2 nd = 4 th ” “same shape as Y diag”. etc etc
		or equiv of any of the above			
		If none of the above applies: Any implication that values not all equal eg: Not uniform or values increase (then decrease) or there is a peak Symmetrical or mirror image oe or ${}^4C_0 = {}^4C_4$ or 2nd = 4th or similar or mean = 2, or E(X) = 2, or 2 is hi'est prob, or peak at 2, or peak is middle value Y	B1	${}^4C_0, {}^4C_1, {}^4C_2$, etc indep	
			B1	indep	
			B1	indep	
			[3]		

Question			Answer	Marks	Guidance
7	(i)		Geo(0.6) or G(0.6) or Geo with $p = 0.6$ P(woman) const or chance of woman const Each voter has same prob Whether one voter is a woman is indep of whether any other is a woman	B1B1 B1 B1 [4]	Allow Geo(60%) B1B1 or %age of women is constant Allow: “voter(s) independent”, “Men & women are independent” “P(woman) is indep” “Each woman is indep” Bin(..., 0.6) B0B1. Can still score comment marks In context Allow “vote indep” In context (EACH comment must be in context) Ignore all else
7	(ii)		$0.4^3 \times 0.6$ $= \frac{2^4}{625}$ or 0.0384	M1 A1f [2]	ft their Geo(p) from (i) ft their Geo(p) from (i) Allow $0.3^3 \times 0.6$ (but no other $q^3 \times 0.6$) eg if $p = 0.4$, ans 0.0864 M1A1f
7	(iii)		0.4^3 alone, or $(0.4^4 + 0.4^3 \times 0.6)$ or $(0.4^4 +$ (ii)) $= \frac{8}{125}$ or 0.064	M1 A1f [2]	$1 - (0.6 + 0.4 \times 0.6 + 0.4^2 \times 0.6)$ (allow extra term $0.4^3 \times 0.6)$ ft their Geo(p) from (i) ft their Geo(p) from (i) Allow M1 for 0.4^4 alone (= 0.0256) M0 for $0.4^r \times 0.6$ and for $1 - 0.4^3$ eg if $p = 0.4$, ans 0.216 M1A1f
8	(i)		Binomial stated $1 - 0.9648$ $= 0.0352$ (3 sfs) or $\frac{9}{256}$	M1 M1 A1 [3]	or implied by $C \times 0.5^r$ or use of table or ${}^8C_7 \times 0.5^7 \times 0.5 + 0.5^8$ fully correct method or $0.5^7 \times 0.5 + 0.5^8$ or $0.5^8 + 0.5^8$ $1 - (0.5^8 + 8 \times 0.5^8 + {}^8C_2 0.5^8 \dots)$ all correct
8	(ii)	(a)	${}^{22}C_{11} \times 0.5^{11} \times 0.5^{11}$ $= 0.168$ (3 sfs)	M1 A1 [2]	Fully correct method. Not ISW eg 0.168^2 or 2×0.168 or $1 - 0.168$: M0A0

Question			Answer	Marks	Guidance
8	(ii)	(b)	$1 - \text{"0.168"}$ $\frac{1}{2}(1 - \text{"0.168"})$ $= 0.416$ (3 sfs)	M1 M1 A1 [3]	or $0.5^{22}({}^{22}C_{12} + {}^{22}C_{13} + {}^{22}C_{14} + \dots + 22 + 1)$ All 11 correct terms seen, or correct ans: M2 or $P(X = 12, 13, \dots, 21, 22)$ stated or implied with ≥ 2 terms shown or one extra term M1 or $1 - ({}^{22}C_{12} + {}^{22}C_{13} + {}^{22}C_{14} + \dots + 22 + 1)$ $1 -$ all 12 correct terms M2 or similar marks for $P(X = 10, 9, 8, \dots, 0)$
9	(i)	(a)	9P_4 or ${}^9!/5!$ or ${}^9C_4 \times 4!$ $= 3024$	M1 A1 [2]	alone oe eg ${}^9C_1 \times {}^8C_1 \times {}^7C_1 \times {}^6C_1$ or $9 \times 8 \times 7 \times 6$
9	(i)	(b)	8P_3 or $8 \times 7 \times 6$ oe or ${}^8C_3 \times 3!$ $\times 5$ (or 5C_1) $= 1680$	M1 M1 A1 [3]	Allow $\times \dots$ or $\div \dots$ Correct $\times 5$ or ${}^8C_3 \times 5$ (or 5C_1) Not ISW, eg $1680/3024$: M1M1A0 or $({}^9P_4 \text{ or "3024"}) \times 5/9$ M2
					SC: consistent use of with replacement in (i) (or if only (a) or (b) attempted) (ia) M0A0 (ib) 999×5 or 4995 M1 M0A0

Question			Answer	Marks	Guidance	
9	(ii)	(a)	${}^5C_3 \times {}^4C_1$ or 5C_4 oe ${}^5C_3 \times {}^4C_1 + {}^5C_4$ oe correct method so far (= 45) $\div {}^9C_4$ Allow anything $\div {}^9C_4$ $= \frac{5}{14}$ or 0.357 (3 sfs) oe, eg $\frac{35}{98}$ or $\frac{45}{126}$	M1 M1 M1 A1 [4]	${}^5C_3 \times {}^4C_1 \times 4!$ (or ${}^5P_3 \times 4 \times 4$) or $5!$ (or 5P_4) $960 + 120$ oe correct method so far $\div {}^9P_4$ [must involve any P or any !] $\div {}^9P_4$ Marks must come from one method, not mixture of two methods	$\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{4}{6}$ Allow \times or $+$... $\times 4$ correct method so far $\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{2}{6}$ Allow \times or $+$... or: $\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{4}{6}$ or $\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7}$ M1 $\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times \frac{4}{6} \times 3 + \frac{5}{9} \times \frac{4}{8} \times \frac{3}{7}$ M1 NB $\frac{5}{9} \times \frac{4}{8} \times \frac{3}{7} \times 3 = \frac{5}{14}$ M0M0M0A0
		(b)	9, 8, 7, 4 or 9, 8, 6, 5 No mark yet $\frac{2}{\div {}^9C_4}$ oe Must be (1 or 2 or 4) $\div {}^9C_4$ $= \frac{1}{63}$ oe or 0.0159 (3 sfs)	M1 M1 A1 [3]	$\frac{1}{9} \times \frac{1}{8} \times \frac{1}{7} \times \frac{1}{6}$; $\frac{4}{9} \times \frac{3}{8} \times \frac{2}{7} \times \frac{1}{6}$ Allow \times or $+$... $\times 4! \times 2$; $\times 2$ fully correct method NB Marks from one method only, not mixed methods SC: consistent use of with replacement in (ii), (or if only (a) or (b) attempted) (iia) $(\frac{5}{9})^4$ M1 $+ {}^4C_3 (\frac{5}{9})^3 (\frac{4}{9})$ (= 0.400) M1 M0A0 (iib) $(\frac{1}{9})^4$ (=0.000152) M1 attempt find no of gps M1A0	$4! + 4!$ or $2 \times 4!$ oe $\div {}^9P_4$ or \div (i)(a) oe Must be (96 or 48 or 24) $\div {}^9P_4$ $\frac{2}{9} \times \frac{2}{8} \times \frac{1}{7} \times \frac{1}{6}$ allow \times or $+$... M1 $\times 4! / 4 \times 2$ fully correct method M1 $1 - ((\frac{4}{9})^4 + 4(\frac{4}{9})^3(\frac{5}{9}) + {}^4C_2(\frac{4}{9})^2(\frac{5}{9})^2)$ M2 One term missing or extra or wrong M1

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

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