

4. A sequence x_1, x_2, x_3, \dots is defined by

$$x_1 = 1$$

$$x_{n+1} = ax_n + 5, \quad n \geq 1$$

where a is a constant.

(a) Write down an expression for x_2 in terms of a .

(1)

(b) Show that $x_3 = a^2 + 5a + 5$

(2)

Given that $x_3 = 41$

(c) find the possible values of a .

(3)



6.

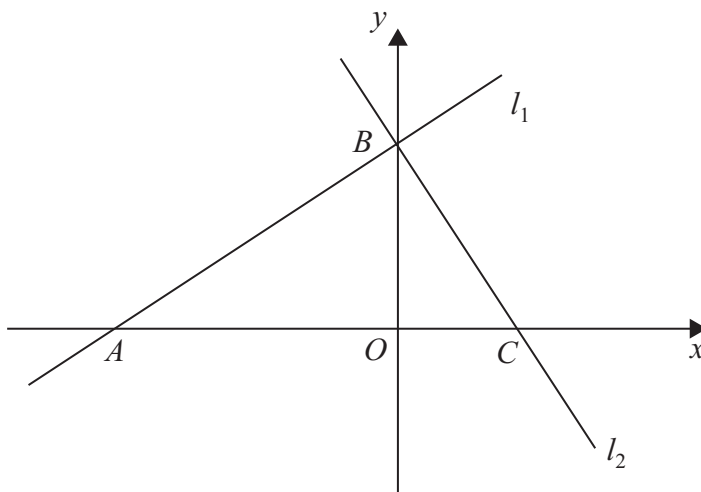


Figure 1

The line l_1 has equation $2x - 3y + 12 = 0$

- (a) Find the gradient of l_1 . (1)

The line l_1 crosses the x -axis at the point A and the y -axis at the point B , as shown in Figure 1.

The line l_2 is perpendicular to l_1 and passes through B .

- (b) Find an equation of l_2 . (3)

The line l_2 crosses the x -axis at the point C .

- (c) Find the area of triangle ABC . (4)

10.

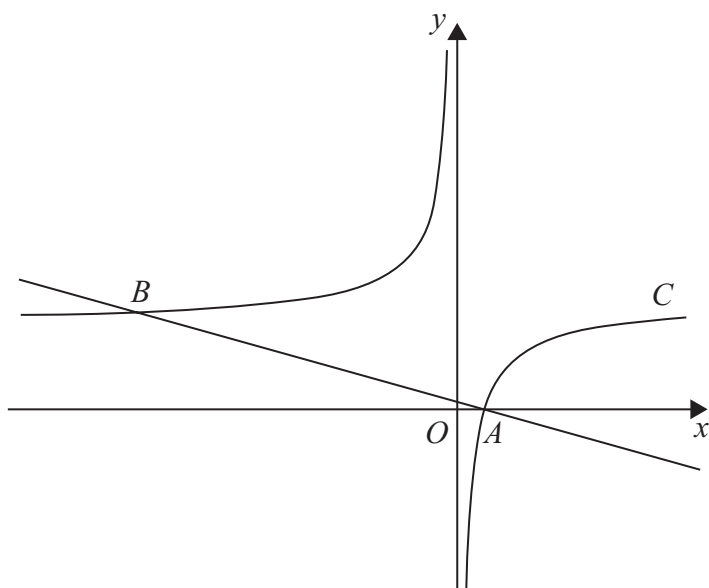


Figure 2

Figure 2 shows a sketch of the curve C with equation

$$y = 2 - \frac{1}{x}, \quad x \neq 0$$

The curve crosses the x -axis at the point A .

(a) Find the coordinates of A . (1)

(b) Show that the equation of the normal to C at A can be written as

$$2x + 8y - 1 = 0 \quad (6)$$

The normal to C at A meets C again at the point B , as shown in Figure 2.

(c) Find the coordinates of B . (4)



