

GCE

Mathematics

Advanced Subsidiary GCE

Unit 4732: Probability and Statistics 1

Mark Scheme for January 2013

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations and abbreviations

Annotation in scoris	Meaning
√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
٨	Omission sign
MR	Misread
Highlighting	

Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Subject-specific Marking Instructions for GCE Mathematics (OCR) Statistics strand

a. Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c. The following types of marks are available.

М

A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Δ

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Ε

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results.

 Otherwise A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f. Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

Candidates are expected to give numerical answers to an appropriate degree of accuracy. 3 significant figures may often be the norm for this, but this always needs to be considered in the context of the problem in hand. For example, in quoting probabilities from Normal tables, we generally expect some evidence of interpolation and so quotation to 4 decimal places will often be appropriate. But even this does not always apply – quotations of the standard critical points for significance tests such as 1.96, 1.645, 2.576 (maybe even 2.58 – but not 2.57) will commonly suffice, especially if the calculated value of a test statistic is nowhere near any of these values. Sensible discretion must be exercised in such cases.

Discretion must also be exercised in the case of small variations in the degree of accuracy to which an answer is given. For example, if 3 significant figures are expected (either because of an explicit instruction or because the general context of a problem demands it) but only 2 are given, loss of an accuracy ("A") mark is likely to be appropriate; but if 4 significant figures are given, this should not normally be penalised. Likewise, answers which are slightly deviant from what is expected in a very minor manner (for example a Normal probability given, after an attempt at interpolation, as 0.6418 whereas 0.6417 was expected) should not be penalised. However, answers which are grossly over- or under-specified should normally result in the loss of a mark. This includes cases such as, for example, insistence that the

value of a test statistic is (say) 2.128888446667 merely because that is the value that happened to come off the candidate's calculator. Note that this applies to answers that are given as final stages of calculations; intermediate working should usually be carried out, and quoted, to a greater degree of accuracy to avoid the danger of premature approximation.

The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

g. Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h. Genuine misreading (of numbers or symbols, occasionally even of text) occurs. If this results in the object and/or difficulty of the question being considerably changed, it is likely that all the marks for that question, or section of the question, will be lost. However, misreads are often such that the object and/or difficulty remain substantially unaltered; these cases are considered below.

The simple rule is that all method ("M") marks [and of course all independent ("B") marks] remain accessible but at least some accuracy ("A") marks do not. It is difficult to legislate in an overall sense beyond this global statement because misreads, even when the object and/or difficulty remains unchanged, can vary greatly in their effects. For example, a misread of 1.02 as 10.2 (perhaps as a quoted value of a sample mean) may well be catastrophic; whereas a misread of 1.6748 as 1.6746 may have so slight an effect as to be almost unnoticeable in the candidate's work.

A misread should normally attract some penalty, though this would often be only 1 mark and should rarely if ever be more than 2. Commonly in sections of questions where there is a numerical answer either at the end of the section or to be obtained and commented on (eg the value of a test statistic), this answer will have an "A" mark that may actually be designated as "cao" [correct answer only]. This should be interpreted strictly – if the misread has led to failure to obtain this value, then this "A" mark must be withheld even if all method marks have been earned. It will also often be the case that such a mark is implicitly "cao" even if not explicitly designated as such.

On the other hand, we commonly allow "fresh starts" within a question or part of question. For example, a follow-through of the candidate's value of a test statistic is generally allowed (and often explicitly stated as such within the marking scheme), so that the candidate may exhibit knowledge of how to compare it with a critical value and draw conclusions. Such "fresh starts" are not affected by any earlier misreads.

A misread may be of a symbol rather than a number – for example, an algebraic symbol in a mathematical expression. Such misreads are more likely to bring about a considerable change in the object and/or difficulty of the question; but, if they do not, they should be treated as far as possible in the same way as numerical misreads, mutatis mutandis. This also applied to misreads of text, which are fairly rare but can cause major problems in fair marking.

The situation regarding any particular cases that arise while you are marking for which you feel you need detailed guidance should be discussed with your Team Leader.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

"3 sf" means "answer which rounds to ... to 3 sf". Penalise over–rounding if no better answer is seen and penalise only once in the paper.

	Questic	n	Answer	Marks	Guidan	ce
1	(i)		2k + 4k + 6k + 8k = 1	M1	or $2 + 4 + 6 + 8 = 20$ M1	Must see correct wk'g for $k = \frac{1}{20}$,
			$k = \frac{1}{20}$ AND $6 \times \frac{1}{20} = \frac{3}{10}$ AG	A1	Must see both for A1	otherwise M0A0
			10	AI	Wust see both for A1	NB $k \times 6 = \frac{3}{10} \implies k = \frac{1}{20} \text{ M0A0}$
					or $2k + 4k + 6k + 8k = 20k$ M1	
					$P(X=6) = \frac{6k}{20k} = \frac{3}{10}$ A1	(even if tested by showing that $k = \frac{1}{20}$
						gives $\Sigma p=1$)
						Just showing $\frac{1}{10} + \frac{2}{10} + \frac{3}{10} + \frac{4}{10} = 1$
	(**)			[2]		M0A0
1	(ii)		$2 \times \frac{1}{10} + 4 \times \frac{2}{10} + 6 \times \frac{3}{10} + 8 \times \frac{4}{10}$ oe	M1	≥ 3 terms correct ft their values of p , dep $\sum p = 1$	Allow i.t.o. k for M1 $\div 4$ M0
			= 6	A1	cao	
			$2^2 \times \frac{1}{10} + 4^2 \times \frac{2}{10} + 6^2 \times \frac{3}{10} + 8^2 \times \frac{4}{10}$ oe (= 10)	M1	\geq 3 terms correct; ft their values of p;	Allow ito k for M1M1 $\div 4$ M0
				IVII	dep $\Sigma p = 1$	NOT $- m^2 \div 4$
			- '6' ²	M1	ft their values of p; dep +ve result & $\Sigma p = 1$	$\sqrt{4} = 2$ lose final A1, not ISW, unless
			= 4		cao	labelled sd
			= 4	A1		
2	(i)		3 1 3	[5] M1	1513 (650.127)	
	(1)		$\frac{3}{4} + \frac{1}{4} \times \frac{3}{8}$	IVII	$\frac{1}{4} \times \frac{5}{8} \times \frac{13}{16}$ (= $\frac{65}{512}$ or 0.127)	
			$+\frac{1}{4} \times \frac{5}{8} \times \frac{3}{16}$	M1	$1 - \frac{1}{4} \times \frac{5}{8} \times \frac{13}{16}$	
			$=\frac{447}{512}$ or 0.873 (3 sf)	A1		
			312	[3]		
2	(ii)		0.6 <i>p</i> or equiv seen	B1	Tree diag alone insufficient for mark.	NB $0.6 \times 0.3 = 0.18$ seen at the end is
			0.4 + 0.6p = 0.58	M1	Or $0.6p = 0.18$. "0.18" alone insufficient	probably a check, not an answer.
			p = 0.3	A1		But if 0.3 seen and 0.18 is very clearly
				[3]		indicated as the ans then B1M1A0

	Question	Answer	Marks	Guidan	ce
3	(i)	$S_{xx} = 8700000 - \frac{7000^2}{6} \qquad (= 533333)$			
		$S_{xy} = 509900 - \frac{7000 \times 456}{6} \qquad (= -22100)$	M1	Correct subst'n in any correct S formula	
		$b = -\frac{"22100"}{"533333"}$ or $-\frac{663}{16000}$ (= -0.0414)	M1	Correct subst'n in any correct b formula from two correct S formulae	
		$y - \frac{456}{6} = \text{``-0.0414''}(x - \frac{7000}{6})$	M1	ft their b except if using r	or $a = \frac{456}{6} - ("-0.0414") \times \frac{7000}{6}$ oe ft "b"
		y = -0.0414x + 124 (3 sf)	A1 [4]	or $y = -\frac{663}{16000} x + \frac{3979}{32}$ or $y = -0.041x + 124$	Allow $y=-0.04x+124$ if -0.041 seen above
3	(ii)	70 to 72	B1 [1]	or 71 per thousand, NOT 71000	No ft from (i) Ignore method
3	(iii)	Extrapolation oe	B1	Allow "2400 is beyond graph" } "Not shown on the graph" or "Line drops low, or below 0" } "Outlier" }	"Line only allows for countries poorer than Nigeria" 1 st B1 Allow "Value for Nigeria is –ve 1 st B1
		Corr'n not high or small sample	B1	Poor corr'n oe, or pts not close to line oe 2 nd B1	NOT "Other factors may apply" oe
			[2]		Ignore all else
3	(iv)	$S_{xx} = 8700000 + 1300^2 - \frac{(7000 + 1300)^2}{7}$		or $10390000 - \frac{(8300)^2}{7} = \frac{3840000}{7}$ or 548571	
		$S_{yy} = 36262 + 96^{2} - \frac{(456+96)^{2}}{7}$ $S_{xy} = 509900 + 1300 \times 96 - \frac{8300 \times 552}{7}$	M1 A1	or $45478 - \frac{552^2}{7} = \frac{13642}{7}$ or 1948.86 or $634700 - \frac{8300 \times 552}{7} = -\frac{138700}{7}$ or -19814.3	Correct sub in any correct <i>S</i> formula M1 Correct value of any <i>S</i> seen or implied by <i>r</i> A1
		$r = \frac{\text{"-}19814.3\text{"}}{\sqrt{\text{"548571"}\times\text{"1948.86"}}}$	M1	Correct subst'n in any correct <i>r</i> formula from 3 correct subst in 3 correct <i>S</i> formulae, ie all correct method	SC If $n = 6$, but otherwise correct allow M1A0M1A0 (ans $r = -0.574$, must see wking)
		=-0.606 (3 sf)	A1 [4]		

	Questi	on	Answer	Marks	Guida	nce
3	(v)		No effect oe	B1 [1]	Stay the same oe Allow just "No"	Ignore all else
4	(i)	(a)	6	B1 [1]		
4	(i)	(b)	3×3×3 = 27	M1 A1 [2]	3! + 7×3 3 + 3×6 + 6 3! × 4 + 3 Complete correct method. Allow methods equiv to these. Only allow other methods if they appear correct	(Explanation for 3! × 4 + 3: 123: 3!, 112 & 122: 3!, 223 & 233: 3!, 331 & 311: 3! 111, 222, 333: 3 Candidates need not include this)
4	(i)	(c)	(i)(b) – 3 If answer is not 24, this method must be explicitly stated in order to give M1A1ft = 24 ft their (i)(b)	M1 A1ft [2]	or $3! + 6 \times 3$ or $3! + 3! \times 3$ or $6 + 3! \times 3! \div 2!$ or $3! \times 4$ Complete correct method. Allow methods equiv to these. Only allow other methods if they appear correct	or 8 × 3 (Explanation: there are 8 possible orders starting with 1. Candidates need not include this)
4	(ii)		eg 1123: $\frac{4!}{2!} \times 3$ alone allow M1 for $\frac{4!}{2!} \times 3!$ alone eg 1122: $\frac{4!}{2!2!} \times 3$ alone allow M1 for $\frac{4!}{2!2!} \times 3!$ alone Total = 54	M2 M2 A1 [5]	$3! \times {}^{4}C_{1} \times 3 \text{ or } 3! \times 12 \text{ M1}$ $\div 2 \text{ M1dep } (=36)$ $3! \times {}^{4}C_{2} \text{ M1}$ $\div 2 \text{ M1dep } (=18)$ Allow methods equiv to these, eg correctly listing cases Only allow other methods if they appear correct. $NB \ 3 \times 3 \times 2 \times 2 = 36 \& 3 \times 3 \times 2 \times 1 = 18$ are incorrect methods unless clear justification given	This method only scores if $3\times3\times3\times3$ is used: No. with 4 rep'ns = 3 M1 No. with 3 rep'ns = $\frac{4!}{3!}$ M1 × 6 (= 24) M1 or 8 × 3 M2 81–('3'+'24') or 81–27 M1 (allow 81–3 or 81–24) 18, 36 only score if a correct method seen,, or eg: 18 orders listed starting with "1" or 18 orders listed with two repetitions

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	Duestic	'n	Answer	Marks	Guidan	00		
	uesuc)11						
5			If incorrect p used consistently in all parts of qu 5, no mks in (i)(a) & (b) but can score M-marks in (ii) and (iii).					
5	(i)	(a)	1.25 oe	B1				
				[1]				
5	(i)	(b)	0.8965 - 0.6328	M1	$^{5}C_{2}(\frac{3}{4})^{3}(\frac{1}{4})^{2}$			
			= 0.264 (3 sf)	A1 [2]	$= \frac{135}{512} \text{ or } 0.264 \text{ (3 sf)}$	Answer which rounds to 0.264		
5	(ii)			M1	$\left(\left(\frac{3}{4}\right)^{5}\right)^{2}$ or $\left(\frac{243}{1024}\right)^{2}$ or $\left(\frac{3}{4}\right)^{10}$ oe $\left(=\frac{59049}{1048576}\right)$	B(10. 0.25) seen or implied M1		
			Answer which rounds to 0.244	M1	$\left(\frac{3}{4}\right)^5 \times 5\left(\frac{3}{4}\right)^4 \left(\frac{1}{4}\right) \text{ or } \frac{243}{1024} \times \frac{405}{1024} \text{ or } 5\left(\frac{3}{4}\right)^9 \left(\frac{1}{4}\right)$	Table or formula with $n = 10$ used M1		
					$(=\frac{98415}{1048576})$	$P(X \le 1)$ from table		
				M1	$2 \times (\text{attempt P}(1, 0) \text{ alone}), \\ (\text{NOT } 2 \times (\text{P}(1, 0) + \text{P}(0, 0)))$	or $(\frac{3}{4})^{10} + 10(\frac{3}{4})^9 \times (\frac{1}{4})$ M1		
						0.244 (3 sf) A1		
					If $P(\text{sum} \le 2)$, all three M-mks are available, but for 3rd M1, must be $2 \times (P(1,0) + P(2,0))$ only	$P(X \le 2) = 0.526$ from table $n = 10$ M1M1M1A0		
				A1	Ans 0.150 probably M1M1M0A0 but check working Ans 0.188 probably M0M1M1A0 but check working	SC $P(X = 2)$ answer 0.282: B1		
				[4]				
5	(iii)		Use of 0.2637 or 0.264	M1	or their (i)(b)	SC allow ${}^{10}C_3 \times (1-'0.282')^7 \times '0.282'^3$		
			$^{10}\text{C}_3 \times (1 - \text{`}0.2637\text{'})^7 \times \text{`}0.2637\text{'}^3$	M1	ft (i)(b) allow ft their (ii) for this M1 only	M0M1		
					, ,	(0.282 comes from P(3 totals = 2))		
			=0.258 (3 sf)	A1 [3]	Correct ans, no working: M1M1A1	` <u> </u>		

Ç	Question	Answer	Marks	G	uidance
6	(i)	Attempt find total area, (even if includes a^2) eg $20 \times 1.4a + 10 \times 3.4a + 6 \times 4.6a + 4 \times 2.6a + 10 \times 3a + 30a$		eg tot $\frac{\text{area}}{800/16} = 16\text{cm}^2 \text{ or } 16a$ M1 800/16 (= 50) M1	Trial methods, eg:
		or 28a+34a+27.6a+10.4a+30a+30a or 20×1.4+10×3.4+6×4.6+4×2.6+10×3+30		$a \times 10 = 50 \ a = 5$ A1	$a = 5$ gives $7 \times 20 + 17 \times 10 + 23 \times 6 + \dots$ = 800 M1
		or 28+34+27.6+10.4+30+30		eg tot area = 400 (sqs) M1	= 800 M1 But no of apples $= 800$ M1
		or $7 \times 20 + 17 \times 10 + 23 \times 6 + \dots$		800/400 (= 2) M1	Hence $a = 5$ A1
		or 160a or 160 or 16 or 16a (if area, not ht)	M1	$1.4a \times 20 = 70 \times 2$ $a = 5$ A1	
					$a = 10$ gives $14 \times 20 + 34 \times 10 + 46 \times 6 + . =$
		800 ÷ their total (must involve area, not ht)	M1dep		1600 M1
		eg $160a = 800, 800 \div$ a = 5	Λ 1	Correct ans with nothing incorrect seen:	But no of apples = $800 \text{ M}1$
		u - S	A1	M1M1A1	Hence $a = 5$ A1
		"Box" \Rightarrow area. "Square" possibly \Rightarrow area		But where the correct answer clearly res	ults NOT "1cm = 5" (because may just
				from incorrect working, eg $a = 800/167$	
				rounded to $a = 5$, then max M1M1A0	NB total ht = 16 cm so if 16 seen, must
					clearly be area eg 800/16 may score 0
	(**)		[3]		<u>or 2</u>
6	(ii)	$\frac{1}{2}$ total area or $\frac{1}{2}$ total no. apples ft their 6(i)	B1f		Examples of correct methods:
		M 1	M1		$400 - (7 \times 20 + 17 \times 10)$ (= 90)
		Median is in 50 – 56 class stated or implied	IVII		$50 + \frac{"90"}{23\times6} \times 6 = 54$
					23×0
					$200 - (70 + 85) \ (= 45)$
		Calculate (approx) $\frac{2}{3}$ of way along class			$50 + \frac{"45"}{69} \times 6 = 54$
			3.54		
		or $\frac{1}{3}$ of way from top of class	M1		$400.5 - (7 \times 20 + 17 \times 10)$ (= 90.5)
					$50 + \frac{"90.5"}{23 \times 6} \times 6 = 54$
		Median = 53.9 to 54 Not eg 54.2	A1	Correct ans with nothing incorrect se	en:
				M1M1A1	Use of LB = 49.5 :
				But where the correct answer clearly res	eg median = 49.5 +appr $\frac{2}{3} \times 6 = 53.4$
			[4]	from incorrect working, eg $a = 800/167$	
				rounded to $a = 5$, then max M1M1A0	

Q	uestic	n	Answer	Marks	Guidan	ce
7	(i)		$\Sigma d^2 = n \text{ seen or implied}$ $1 - \frac{6 \times \text{anything}}{n(n^2 - 1)} = \frac{63}{65} \text{or } \frac{6 \times \text{anything}}{n(n^2 - 1)} = \frac{2}{65}$	M1 M1	eg $1 - \frac{6 \times \Sigma d^2}{n(n^2 - 1)}$ or $1 - \frac{6 \times n^2}{n(n^2 - 1)}$ or $1 - \frac{6 \times 1^n}{n(n^2 - 1)}$ or $1 - \frac{6 \times 6^2}{n(n^2 - 1)} = \frac{63}{65}$	Trial method: $\Sigma d^2 = 14$ M1 $1 - \frac{6 \times 14}{14(14^2 - 1)}$ oe M1 $= \frac{63}{65}$ A1 (0.969 : A0)
			$\frac{6}{(n^2-1)} = \frac{2}{65}$ or eg 390 = 2(n ² - 1)	A1 depM2	Any <u>correct</u> eqn after cancelling n or take out factor of n ; can be implied by $n = 14$	$\Rightarrow n = 14$ A1 Conclusion needed
			$n = 14$ NOT $n = \pm 14$	A1	But A0 if $n = 14$ clearly follows from incorrect working	
				[4]	If no working or unclear working, but n = 14, M1M1A1A1	
7	(ii)	(a)	$r = 1 \implies$ st line, hence true (or $r_s = 1$) oe Explanation essential Must state or imply "true"	B1	$r = 1 \implies y$ incr as x incr, so $r_s = 1$ oe Allow "True because perfect corr'n" or "True because $r = 1$ means pts ranked in order so $r_s = 1$ " " $r = 1$ means the ranks will agree" " $r = 1$ means all d 's are 0, hence $r_s = 1 - 0 = 1$ "	NOT " r incr so ranks incr" NOT " $r_s = r$ for ranks so true" NOT "True because strong corr'n"
7	(ii)	(b)	Diag, ≥ 3 pts, not on st line but with $x_{n+1} > x_n$ & $y_{n+1} > y_n$, Zig zag line or curve, moving up & right	[1] B1	Ignore explan if correct diag given Ignore any st line drawn Allow numerical example for which $r \neq 1$ but $r_s = 1$. If expl'n contradicts diag, mark diag	
			so r_s can still be 1	B1dep [2]	For 2 nd B1 must state or imply "false"	
			eg "expon'l curve gives $r \neq 1$ but $r_s = 1$ " B1B1			

8	(i)	(a)				ce
		(a)	$0.9^4 \times 0.1$	M1		
			$=\frac{6561}{100000}$ or 0.0656 (3sf)	A1		
	(8)	73. \	10000	[2]	111 0 04 1 0 05 374	1 (01 00 01 002 01
8	(i)	(b)	0.9^{5}	M1	Allow 0.9 ⁴ or 1–0.9 ⁵ :M1	$1 - (0.1 + 0.9 \times 0.1 + 0.9^2 \times 0.1 + 0.9^4 \times 0.1)$
			500.40	A1	but $1-0.9^n (n \neq 5)$ or 0.1×0.9^n :M0	$0.9^4 \times 0.1$) Allow without "1 –" OR omit last
			$=\frac{59049}{100000}$ or 0.59 (2 sf)	AI		term
				[2]		NB $0.9^5 \times 0.1 = 0.0590 \text{ M0A0}$
8	(i)	(c)	0.1×0.1 or $[0.1 \times 0.1 \times 0.9 + 0.1 \times 0.1 \times 0.1]$	oe M1		$3\times0.1^2\times0.9+0.1^3$ no incorrect multiples
	(-)	(0)	+ 0.1×0.9×0.1	oe M1	M1M1 two correct terms, no incorrect multiples	M2 for 1st term; M1 for 2nd
			$+ 0.9 \times 0.1 \times 0.1$	oe M1	M1 all correct	
						This method only scores using " $1 -$ ":
			= 0.028	A1	Ans 0.027 probably M0M1M1A0 but check	0.9^3 ; $3\times0.9^2\times0.1$ no incorrect multiples
					working	M1; M1
					SC if no M-mks scored:	1 – one or both terms with no further wking: M1(dep M1)
					SSF, SSS, FSS, SFS	eg $1 - 0.9^3$ alone M1M0M1
				[4]	or SS, FSS, SFS seen or implied: B1	eg 1 0.5 dione witwowii
8	(ii)	(a)	$0.9 \times 0.8 \times 0.1$	M1	alone or allow \times 0.8 (ie girls in wrong order)	NOT 0.9×0.8×0.1×0.2= 0.0144: M0A0
	` '		$=\frac{9}{125}$ or 0.072	A1	(= 0.0576)	NOT 0.9×0.8×0.2= 0.144: M0A0
			123	[2]		
8	(ii)	(b)	$0.9^{9 \text{ or } 10} \times 0.8^{9 \text{ or } 10} \times 0.1 \text{ (or } \times 0.2, \text{ not }$	M1	allow $0.9^{9 \text{ or } 10} \times 0.8^{9 \text{ or } 10} \times 0.1 \times {}^{18,19,20}C_1$	If ans = 0.00360 or 0.0150 see SC
			×0.1×0.2)			<u>below</u>
			$(0.9 \times 0.8)^9 \times 0.1$ oe	M1	fully correct	
			$= 5.2 \times 10^{-3} \text{ or } 0.0052 \text{ (2 sf)}$	A1		
					SC Consistent use of 0.8 for both girls: (ii)(a)	0.128 (ii)(b) 0.00360
						0.081 (ii)(b) 0.00500 0.081 (ii)(b) 0.0150 If both these ans
				[3]	seen, allow (a) 0 (b) B1	0.001 (h)(b) 0.0130 II both these ans

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