





2.  $f(x) = ax^3 + bx^2 - 4x - 3$ , where  $a$  and  $b$  are constants.

Given that  $(x - 1)$  is a factor of  $f(x)$ ,

(a) show that

$$a + b = 7$$

(2)

Given also that, when  $f(x)$  is divided by  $(x + 2)$ , the remainder is 9,

(b) find the value of  $a$  and the value of  $b$ , showing each step in your working.

(4)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---





4. Solve, for  $0 \leq x < 180^\circ$ ,

$$\cos(3x - 10^\circ) = -0.4$$

giving your answers to 1 decimal place. You should show each step in your working.

**(7)**

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---



5. The circle  $C$  has equation

$$x^2 + y^2 - 20x - 24y + 195 = 0$$

The centre of  $C$  is at the point  $M$ .

(a) Find

(i) the coordinates of the point  $M$ ,

(ii) the radius of the circle  $C$ .

**(5)**

$N$  is the point with coordinates  $(25, 32)$ .

(b) Find the length of the line  $MN$ .

**(2)**

The tangent to  $C$  at a point  $P$  on the circle passes through point  $N$ .

(c) Find the length of the line  $NP$ .

**(2)**

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---



**Question 5 continued**

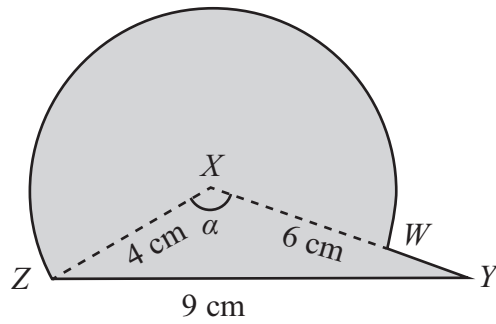
Lined area for writing the answer to Question 5 continued.







7.



**Figure 1**

The triangle  $XYZ$  in Figure 1 has  $XY = 6$  cm,  $YZ = 9$  cm,  $ZX = 4$  cm and angle  $ZXY = \alpha$ . The point  $W$  lies on the line  $XY$ .

The circular arc  $ZW$ , in Figure 1 is a major arc of the circle with centre  $X$  and radius 4 cm.

(a) Show that, to 3 significant figures,  $\alpha = 2.22$  radians. (2)

(b) Find the area, in  $\text{cm}^2$ , of the major sector  $XZWX$ . (3)

The region enclosed by the major arc  $ZW$  of the circle and the lines  $WY$  and  $YZ$  is shown shaded in Figure 1.

Calculate

(c) the area of this shaded region, (3)

(d) the perimeter  $ZWYZ$  of this shaded region. (4)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

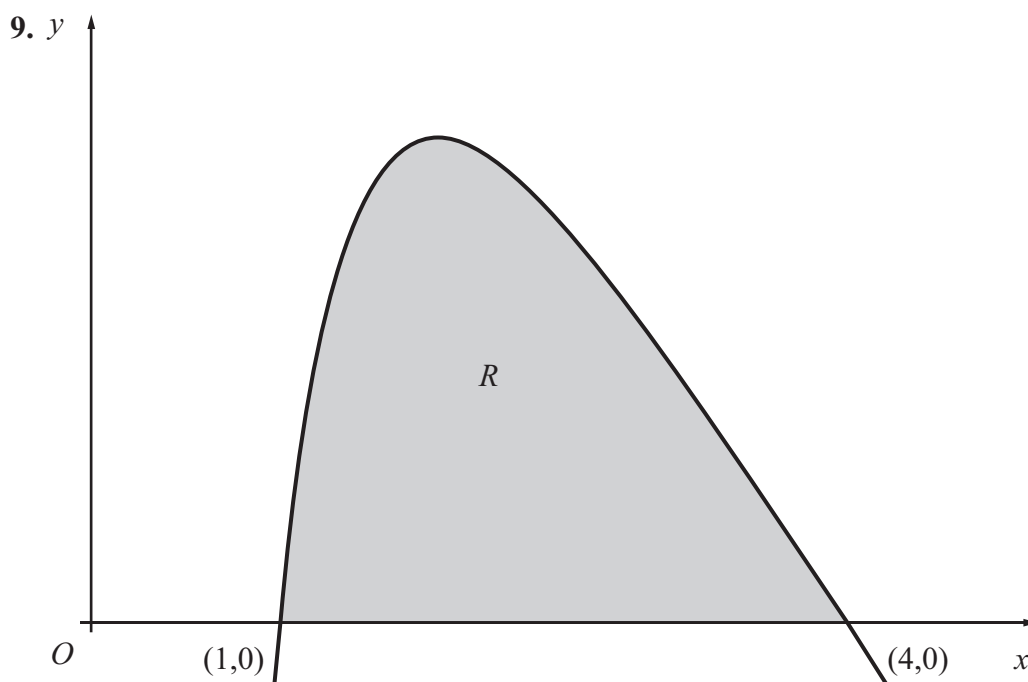
---











**Figure 2**

The finite region  $R$ , as shown in Figure 2, is bounded by the  $x$ -axis and the curve with equation

$$y = 27 - 2x - 9\sqrt{x} - \frac{16}{x^2}, \quad x > 0$$

The curve crosses the  $x$ -axis at the points  $(1, 0)$  and  $(4, 0)$ .

(a) Complete the table below, by giving your values of  $y$  to 3 decimal places.

$x$	1	1.5	2	2.5	3	3.5	4
$y$	0	5.866		5.210		1.856	0

**(2)**

(b) Use the trapezium rule with all the values in the completed table to find an approximate value for the area of  $R$ , giving your answer to 2 decimal places.

**(4)**

(c) Use integration to find the exact value for the area of  $R$ .

**(6)**

---



---



---



---



---



