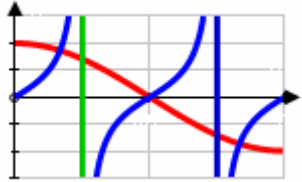


Mark Scheme 4722
June 2005

1 (i) $u_1 = 2, u_2 = 5, u_3 = 8$ The sequence is an Arithmetic Progression	B1 B1 B1 3	For the correct value of u_1 For both correct values of u_2 and u_3 For a correct statement (any mention of arithmetic)
(ii) $\frac{1}{2} \times 100 \times (2 \times 2 + 99 \times 3) = 15050$	M1 M1 A1 3 6	For correct interpretation of Sigma notation – ie finding the sum of an AP or GP For use of correct $\frac{1}{2}n(2a + (n-1)d)$, or equiv, with $n=100$ and a & d not both =1 For correct value 15050
2 (i) $r\theta = 12, \frac{1}{2}r^2\theta = 36$ (ii) $\frac{1}{2}r \times 12 = 36 \Rightarrow r = 6$ Hence $\theta = 2$ (iii) Segment area is $36 - \frac{1}{2} \times 6^2 \times \sin 2 = 19.6 \text{ cm}^2$	B1 B1 2 B1 B1 2 M1* M1dep* A1 3 7	For $r\theta = 12$ stated correctly at any point For $\frac{1}{2}r^2\theta = 36$ stated correctly at any point For showing given value correctly For correct value 2 (or 0.637π) For use of $\Delta = \frac{1}{2}ab \sin C$, or equivalent For attempt at $36 - \Delta$ For correct value (rounding to) 19.6
3 (i) $\int (2x^2 + 7x + 3) dx$ $= \frac{2}{3}x^3 + \frac{7}{2}x^2 + 3x + c$ (ii) $\left[2x^{\frac{1}{2}} \right]_0^9$ $= 6$	M1 A1 A1 B1 4 M1 M1 A1 3 7	For expanding and integration attempt For at least one term correct For all three terms correct For addition of arbitrary constant, and no \int or dx For integral of the form $kx^{\frac{1}{2}}$ For evaluating at least $F(9)$, following attempt at integration For final answer of 6 only
4 (i) $\cos BCA = \frac{5^2 + 6^2 - 9^2}{2 \times 5 \times 6} = -\frac{1}{3}$ So $\sin BCA = \frac{2}{3}\sqrt{2} \approx 0.9428 \dots$ (ii) Angles BCA and CAD are equal So $\sin ADC = \frac{5}{15} \sin CAD = \frac{1}{3} \times \frac{1}{3} \sqrt{8} = \frac{2}{9} \sqrt{2}$ $\Rightarrow ADC = 18.3^\circ$	M1 M1 A1 B1 M1 M1 A1 B1 4 B1 M1 A1√ A1 4 8	For relevant use of the correct cosine formula For attempt to rearrange correct formula For obtaining the given value correctly For correct answer for $\sin BCA$ in any form OR For substituting $\cos BCA = -\frac{1}{3}$ For attempt at evaluation For full verification For correct answer for $\sin BCA$ in any form For stating, using or implying the equal angles For correct use of the sine rule in ΔADC (sides must be numerical, angles may still be in letters) For a correct equation from their value in (i) For correct answer, from correct working
5 (i) $f(-1) = 0 \Rightarrow -1 - a + b = 0$ $f(3) = 16 \Rightarrow 27 + 3a + b = 16$ Hence $a = -3, b = -2$ (ii) $f(2) = 8 - 6 - 2 = 0$	M1 A1 M1 A1 A1 5 B1	For equating their attempt at $f(-1)$ to 0, or equiv For the correct (unsimplified) equation For equating their attempt at $f(3)$ to 16, or equiv For the correct (unsimplified) equation For both correct values – must follow two correct equations For the correct verification (from correct a &

	Hence $f(x) = (x + 1)^2(x - 2)$	M1 A1 3 8	b) For recognition or use of two linear factors, or full division attempt by either $(x + 1)$ or $(x - 2)$ For correct third factor (repeated) of $(x + 1)$, and full linear factorisation stated
6 (i)	$x^6 + 3x^3 + 3 + \frac{1}{x^3}$	M1 A1 A1 A1 4	For 4 term binomial attempt or equiv For any one (unsimplified) term correct For any other (unsimplified) term correct For full, simplified, expansion correct
(ii)	$\frac{1}{7}x^7 + \frac{3}{4}x^4 + 3x - \frac{1}{2}x^{-2} + c$	M1 A1√ M1 A1√ 4 8	For any correct use of $\frac{x^{n+1}}{n+1}$ For any two terms integrated correctly For any correct use of x^{n+1} using a negative index For all terms integrated correctly (must have at least 4 terms, including at least 1 negative index) [No penalty for omission of $+c$ in this part]
7 (i)	$\log_5\left(\frac{15 \times 20}{12}\right) = \log_5 25 = 2$	M1 A1 A1 3	For any relevant combination of $\log a \pm \log b$ For $\log 25$ – must follow correct working only For correct answer 2
(ii)	Method A $\frac{1}{3}y = 10^{2x}$ Hence $2x = \log_{10}\left(\frac{1}{3}y\right)$ i.e. $x = \frac{1}{2}\log_{10}\left(\frac{1}{3}y\right)$	M1 M1 A1 A1 4	For correct division of both sides by 3 For relevant use of $a = b^c \Leftrightarrow c = \log_b a$ For correct equation involving logs to base 10 For correct answer for x
	Method B $\frac{1}{3}y = 10^{2x}$ $\log \frac{1}{3}y = \log 10^{2x}$ $\log \frac{1}{3}y = 2x \log 10$ i.e. $x = \frac{1}{2}\log_{10}\left(\frac{1}{3}y\right)$	M1 M1 A1 A1 4	For correct division of both sides by 3 For taking logs of both sides For correct linear equation involving logs For correct answer for x
	Method C $y = 3 \times 10^{2x} \Rightarrow \log y = \log 3 + \log 10^{2x}$ $\log y = \log 3 + \log 10^{2x}$ $\log y = \log 3 + 2x \log 10$ i.e. $x = \frac{1}{2}\log_{10}\left(\frac{1}{3}y\right)$	M1 A1 M1 A1 4	For introducing logs throughout For correct RHS $\log 3 + \log 10^{2x}$ For correct use of $\log a^b = b \log a$ For correct answer for x
	Method D $x = a \log(b \times 3 \times 10^{2x})$ $x = a \log 3b + a \log 10^{2x}$ $x = 2ax \log 10 \Rightarrow 2a = 1 \Rightarrow a = \frac{1}{2}$ $a \log 3b = 0 \Rightarrow 3b = 1 \Rightarrow b = \frac{1}{3}$	M1 M1 A1 A1 4 7	For substituting for y , and separating RHS into at least 2 terms For attempting values for a and b For obtaining $a = \frac{1}{2}$ For obtaining $b = \frac{1}{3}$
8 (i)	$100\,000 \times 0.9^3 = 72900$	M1 A1 2	For relevant use of ar^3 or equiv For the correct answer 72900
(ii)	$100\,000 \times 0.9^x = 5000$ Hence $x \log 0.9 = \log 0.05$ So $x = 28.4, 28$ or 29 ; or $n = 29.4, 29$ or 30 i.e. 30 th year / 30 years / year is 2030	B1 M1 A1 A1√ 4	For a correct equation or inequality For complete solution method by logs or trial For correct solution for their index – allow integer values either side For correctly linking their index to date or

<p>(iii) Total is $\frac{100000(1-0.9^{30})}{1-0.9} = 957609$</p>	<p>M1 A1√ A1 3 9</p>	<p>number of years For relevant use of $\frac{a(1-r^n)}{1-r}$ For correct (unsimplified) statement for their integer n (if no n stated then use their year – 2000) For answer 958000 or better, including decimal</p>
<p>9 (a) (i) $\cos \frac{1}{6}\pi = \frac{1}{2}\sqrt{3}$ $\tan \frac{1}{3}\pi = \sqrt{3}$ Hence $2 \cos \frac{1}{6}\pi = 2 \times \frac{1}{2}\sqrt{3} = \tan \frac{1}{3}\pi$</p> <p>(ii) </p> <p>Other roots are $\pi/2$ and $5\pi/6$</p>	<p>B1 B1 B1 3 B1 B1 B1 4</p>	<p>For any correct exact value For any correct exact value For correct verification (allow via decimals) For correct sketch of either $y = \tan 2x$ or $y = 2\cos x$ For second correct sketch, with both graphs in proportion (ie 3 points of intersection) For one of $\pi/2$ or $5\pi/6$ (or equiv in degrees) For second correct value, and no others in range $0 \leq x \leq \pi$</p>
<p>(b) (i) $0.05(0.1003 + 2(0.2027 + 0.3093) + 0.4228) = 0.0774$</p> <p>(ii) Overestimate; tops of trapezia above the curve or equiv</p>	<p>M1 M1 A1 A1 4 B1 1 12</p>	<p>State at least three of $\tan 0.1$, $\tan 0.2$, $\tan 0.3$, $\tan 0.4$ Substitute numerical values (must be attempt at y-coords, not x-coords) into correct trapezium rule, with h consistent with number of strips Obtain $0.05(\tan 0.1 + 2(\tan 0.2 + \tan 0.3) + \tan 0.4)$ or equiv in decimals (SC – award A1 if values are now decimals from using degrees – gives final answer of 0.00131) Obtain 0.077 or better For correct statement and justification</p>