







3.

$$x^2 - 8x - 29 \equiv (x + a)^2 + b,$$

where  $a$  and  $b$  are constants.

(a) Find the value of  $a$  and the value of  $b$ .

(3)

(b) Hence, or otherwise, show that the roots of

$$x^2 - 8x - 29 = 0$$

are  $c \pm d\sqrt{5}$ , where  $c$  and  $d$  are integers to be found.

(3)

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4.

Figure 1

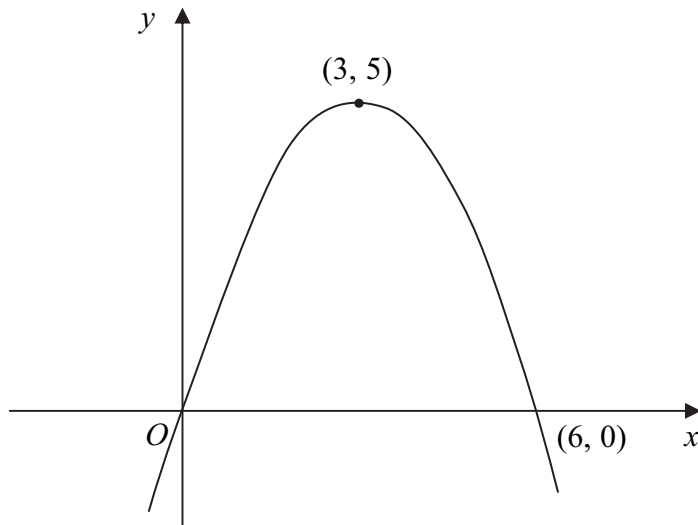


Figure 1 shows a sketch of the curve with equation  $y = f(x)$ . The curve passes through the origin  $O$  and through the point  $(6, 0)$ . The maximum point on the curve is  $(3, 5)$ .

On separate diagrams, sketch the curve with equation

(a)  $y = 3f(x)$ , (2)

(b)  $y = f(x + 2)$ . (3)

On each diagram, show clearly the coordinates of the maximum point and of each point at which the curve crosses the  $x$ -axis.











8. The line  $l_1$  passes through the point  $(9, -4)$  and has gradient  $\frac{1}{3}$ .

(a) Find an equation for  $l_1$  in the form  $ax + by + c = 0$ , where  $a$ ,  $b$  and  $c$  are integers.

(3)

The line  $l_2$  passes through the origin  $O$  and has gradient  $-2$ . The lines  $l_1$  and  $l_2$  intersect at the point  $P$ .

(b) Calculate the coordinates of  $P$ .

(4)

Given that  $l_1$  crosses the  $y$ -axis at the point  $C$ ,

(c) calculate the exact area of  $\triangle OCP$ .

(3)

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9. An arithmetic series has first term  $a$  and common difference  $d$ .

(a) Prove that the sum of the first  $n$  terms of the series is

$$\frac{1}{2}n[2a + (n-1)d]. \tag{4}$$

Sean repays a loan over a period of  $n$  months. His monthly repayments form an arithmetic sequence.

He repays £149 in the first month, £147 in the second month, £145 in the third month, and so on. He makes his final repayment in the  $n$ th month, where  $n > 21$ .

(b) Find the amount Sean repays in the 21st month. (2)

Over the  $n$  months, he repays a total of £5000.

(c) Form an equation in  $n$ , and show that your equation may be written as

$$n^2 - 150n + 5000 = 0. \tag{3}$$

(d) Solve the equation in part (c). (3)

(e) State, with a reason, which of the solutions to the equation in part (c) is **not** a sensible solution to the repayment problem. (1)

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10. The curve  $C$  has equation  $y = \frac{1}{3}x^3 - 4x^2 + 8x + 3$ .

The point  $P$  has coordinates  $(3, 0)$ .

(a) Show that  $P$  lies on  $C$ .

(1)

(b) Find the equation of the tangent to  $C$  at  $P$ , giving your answer in the form  $y = mx + c$ , where  $m$  and  $c$  are constants.

(5)

Another point  $Q$  also lies on  $C$ . The tangent to  $C$  at  $Q$  is parallel to the tangent to  $C$  at  $P$ .

(c) Find the coordinates of  $Q$ .

(5)

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