Mark Scheme 4722 June 2006

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1	(i)	$(3x-2)^{4} = 81x^{4} - 216x^{3} + 216x^{2} - 96x + 16$ $u_{2} = -1, u_{3} = 2, u_{4} = -1$	M1 A1 A1 A1 B1 B1	4 4 2	Attempt binomial expansion, including attempt at coeffs. Obtain one correct, simplified, term Obtain a further two, simplified, terms Obtain a completely correct expansion For correct value -1 for u_2 For correct values for both u_3 and u_4
	(ii)	Sum is $(2+(-1))+(2+(-1))++(2+(-1))$ i.e. $50\times(2+(-1))=50$	M1 M1 A1	3	For correct interpretation of Σ notation For pairing, or $50 \times 2 - 50 \times 1$ For correct answer 50
3		$y = 4x^{\frac{1}{2}} + c$ Hence $5 = 4 \times 4^{\frac{1}{2}} + c \Longrightarrow c = -3$	M1 A1 A1 M1	<u> </u>	For attempt to integrate For integral of the form $kx^{\frac{1}{2}}$ For $4x^{\frac{1}{2}}$, with or without + <i>c</i> For relevant use of (4, 5) to evaluate <i>c</i> For correct value -3 (or follow through on integral
	(i)	So equation of the curve is $y = 4x^{\frac{1}{2}} - 3$	A1√ A1	6 <u>6</u>	of form $kx^{\frac{1}{2}}$) For correct statement of the equation in full (aef)
4	(i) (ii)	Area under curve is $\left[4x - \frac{1}{3}x^3\right]_{-2}^{1}$	M1 M1 M1	2	For both values correct For integration attempt with any one term correct For use of limits – subtraction and correct order
		i.e. $\left(4-\frac{1}{3}\right)-\left(-8+\frac{8}{3}\right)=9$ Area of triangle is $4\frac{1}{2}$ Hence shaded area is $9-4\frac{1}{2}=4\frac{1}{2}$	A1 M1 A1 A1	6	For correct area of 9 Attempt area of triangle (½ <i>bh</i> or integration) Obtain area of triangle as 4 ½ Obtain correct final area of 4 ½
		OR Area under curve is $\int_{-2}^{1} (2 - x - x^2) dx$ = $\left[-\frac{1}{3}x^3 - \frac{1}{2}x^2 + 2x \right]_{-2}^{1}$	M1 M1 A1		Attempt subtraction – either order For integration attempt with any one term correct Obtain $\pm \left[-\frac{1}{3}x^3 - \frac{1}{2}x^2 + 2x\right]$
		$= (-\frac{3}{3} - \frac{3}{2} + 2) - (\frac{3}{3} - 2 - 4)$ $= 4\frac{1}{2}$	M1 A1 A1	<u>8</u>	Obtain $\pm 4 \frac{1}{2}$ - consistent with their order of subtraction Obtain 4 $\frac{1}{2}$ only, following correct method only

5	(i)	$\sin^2 x = 1 - \cos^2 x \Longrightarrow 2\cos^2 x + \cos x - 1 = 0$	M1		For transforming to a quadratic in $\cos x$
		$Hence (2\cos x - 1)(\cos x + 1) = 0$	M1		For solution of a quadratic in cos x
		$\cos x = \frac{1}{2} \Longrightarrow x = 60^{\circ}$	A1		For correct answer 60°
		$\cos x = -1 \Longrightarrow x = 180^{\circ}$	A1	4	For correct answer 180° [Max 3 out of 4 if any extra answers present in range, or in radians] SR answer only is B1, B1 justification – ie graph or substitution is B2, B2
	(ii)	$\tan 2x = -1 \Longrightarrow 2x = 135 \text{ or } 315$	M1 M1		For transforming to an equation of form $tan 2x = k$ For correct solution method, i.e. inverse tan followed by division by 2
		Hence $x = 67.5^{\circ}$ or 157.5°	A1		For correct value 67.5
			A1	4	For correct value 157.5
		OR $\sin^2 2x = \cos^2 2x$ $2\sin^2 2x = 1$ $2\cos^2 2x = 1$ $\sin 2x = \pm \frac{1}{2}\sqrt{2}$ $\cos 2x = \pm \frac{1}{2}\sqrt{2}$ Hence $x = 67.5^\circ$ or 157.5°	M1 M1 A1 A1	8	Obtain linear equation in cos 2 <i>x</i> or sin 2 <i>x</i> Use correct solution method For correct value 67.5 For correct value 157.5 [Max 3 out of 4 if any extra answers present in range, or in radians] SR answer only is B1, B1 justification – ie graph or substitution is B2, B2
6	(i)	(a) $100 + 239 \times 5 = \pounds 1295$	M1	•	For relevant use of $a + (n - 1)d$
			A1	.2	For correct value 1295
		(b) $\frac{1}{2} \times 240 \times (100 + 1295) = \pounds 167400$	M1		For relevant use of $\frac{1}{2}n(a+l)$ or equivalent
	<u></u>		A1	.2	For correct value 167400
	(ii)	$100r^{239} = 1500 \implies r = 1.01139$ Hence total is $\frac{100(1.01139^{240} - 1)}{1.01139 - 1} = \pounds 124359$	B1 M1 A1 M1 A1	5	For correct statement of $100r^{239} = 1500$ Attempt to find <i>r</i> For correct value 1.01 For relevant use of GP sum formula For correct value 124359 (3 s.f. or better)
				<u>9</u>	

7	(i)	$AC^2 = 11^2 + 8^2 - 2 \times 11 \times 8 \times \cos 0.8$ = 62.3796 Hence AC=7.90 cm	M1 A1 A1	3	Attempt to use the cosine formula Correct unsimplified expression Show the given answer correctly
	(ii)	Area of sector = $\frac{1}{2} \times 7.90^2 \times 1.7 = 53.0$	M1		Attempt area of sector using $\left(\frac{1}{2}\right)r^2\theta$
		Area of triangle = $\frac{1}{2} \times 7.90^2 \times \sin 1.7 = 30.9$	M1		Attempt area of $\triangle ACD$, using $(\frac{1}{2})r^2 \sin \theta$, or equiv
		Hence shaded area = 22.1 cm^2	A1	3	Obtain 22.1
	(iii)	(arc) $DC = 7.90 \times 1.7 = 13.4$	M1		Use $r\theta$ to attempt arc length
			A1		Obtain 13.4
		(line) $DC^{2} = 7.90^{2} + 7.90^{2} - 2 \times 7.90 \times 7.90 \times \cos 1.7$ DC = 11.9 Hence perimeter = 25.3cm	M1 A1	4	Attempt length of line <i>DC</i> using cosine rule or equiv. Obtain 25.3
8	(i)	$f(2) = 12 \Longrightarrow 4a + 2b = 6$	M1	<u>10</u>	For equating f(2) to 12
	()		A1		For correct equation $4a + 2b = 6$
		$f(-1) = 0 \Longrightarrow a - b = 12$	M1		For equating f(-1) to 0
		Hence $a = 5$. $b = -7$	A1		For correct equation $a - b = 12$
			A1	6	For both values correct
	(ii)	Quotient is $2x^2 + x - 9$	B1		For correct lead term of $2x^2$
			M1		For complete division attempt or equiv
			A1		For completely correct quotient
		Remainder is 8		5	For attempt at remainder – either division or f(–2)
				<u>11</u>	

1

			r	r	
9	(i)				
		1	M1		Attempt sketch of any exponential graph, in at least first quadrant
		· · · · · · · · · · · · · · · · · · ·	A1		Correct graph – must be in both quadrants
			B1	3	For identification of (0, 1)
	(ii)	$A \approx \frac{1}{2} \times 0.5 \times \left\{ 1 + 2 \left(0.5^{\frac{1}{2}} + 0.5 + 0.5^{\frac{3}{2}} \right) + 0.5^{2} \right\}$	B1		State, or imply, at least three correct <i>y</i> -values
		² (()) ≈1.09	A1		For correct use of trapezium rule, inc correct <i>n</i> For correct unsimplified expression
		~ 1.07	A1	4	For the correct value 1.09, or better
	(111)	$\left(\frac{1}{2}\right)^x = \frac{1}{6} \Longrightarrow x \log_{10} \frac{1}{2} = \log_{10} \frac{1}{6}$	M1		For equation $\left(\frac{1}{2}\right)^x = \frac{1}{6}$ and attempt at logs
		$x = \frac{\log_{10} \frac{1}{6}}{\log_{10} \frac{1}{6}} = \frac{-\log_{10} 6}{\log_{10} \frac{1}{6}}$	A1		Obtain $x \log(\frac{1}{2}) = \log(\frac{1}{6})$, or equivalent
		$\log_{10} \frac{1}{2} - \log_{10} 2$			
		Hence $=\frac{\log_{10} 2 + \log_{10} 3}{\log_{10} 2}$	M1		For use of log $6 = \log 2 + \log 3$
		$\log_{10} 2$		4	For showing the given answer correctly
		$=1+\frac{\log_{10} 5}{\log_{10} 2}$	A1		
		OR			
		$\left(\frac{1}{2}\right)^x = \frac{1}{6} \Longrightarrow 2^x = 6$			
		$\Rightarrow x \log_{10} 2 = \log_{10} 6$	M1		For equation $2 = 6$ and attempt at logs
		$x = \frac{\log_{10} 6}{100}$	A1		Obtain $x \log 2 = \log 6$, or equivalent
		$\log_{10} 2$			
		$=\frac{\log_{10} 2 + \log_{10} 5}{\log_{10} 2}$	M1		For use of log $6 = \log 2 + \log 3$
		$\log_{10} 2$	A 4		For showing the given answer correctly
		$=1+\frac{-100}{\log_{10} 2}$	AI		
		OR			
		$\left(\frac{1}{2}\right)^x = \frac{1}{6} \Longrightarrow 2^x = 6$	M1		Attempt to rearrange equation to $2^n = 3$
		$2^{x-1} = 3$ $(x-1)\log_{10} 2 = \log_{10} 3$	A1		Obtain $2^{x-1} = 3$
		$\log_{10} 3$	M1		For attempt at logs
		$x = 1 + \frac{1}{\log_{10} 2}$	A1		For showing the given answer correctly
		OR			
		$\mathbf{X} = \frac{\log_{10} 2 + \log_{10} 3}{\log_{10} 2}$			
		$= \log_{10} 6$	M1		Use $\log 2 + \log 3 = \log 6$
		$\overline{\log_{10} 2}$	A1		Obtain <i>x</i> log 2 = log 6
		$x \log_{10} 2 = \log_{10} 6$	N/1		Attempt to remove logarithms
		$\log_{10} 2^{\circ} = \log_{10} 6$			
		$\mathcal{L} = 0$			
		$\left(\frac{1}{2}\right) = \frac{1}{6}$	A1		Show $\left(\frac{1}{2}\right)^x = \frac{1}{6}$ correctly
				<u>11</u>	