mark

**M**1

mark

A1

B1

M1

## June 2006

Q 1

$0 = u - 9.8 \times 3$ u = 29.4 so 29.4 m s <sup>-1</sup>	
$s = 0.5 \times 9.8 \times 9 = 44.1$ so 44.1 m	

*uvast* leading to u with t = 3 or t = 6

Signs consistent A1 **M**1 *uvast* leading to *s* with t = 3 or t = 6 or **their** *u* FT their *u* if used with t = 3. Signs consistent. F1

# Award for 44.1, 132.3 or 176.4 seen. [Award maximum of 3 if one answer wrong]

4

Sub

4

Sub

2

# Q 2 (i) $\sqrt{\left(-6\right)^2 + 13^2} = 14.31782...$ so 14.3 N (3 s. f.)

(ii) Resultant is  $\begin{pmatrix} -6\\13 \end{pmatrix} - \begin{pmatrix} -3\\5 \end{pmatrix} = \begin{pmatrix} -3\\8 \end{pmatrix}$ 

Require 
$$270 + \arctan\frac{8}{3}$$

so 339.4439...° so 339°

(iii) 
$$\begin{pmatrix} -3\\5 \end{pmatrix} = 5a$$
  
so  $(-0.6i + i) \text{ m s}^{-2}$ 

change in velocity is 
$$(-6\mathbf{i} + 10\mathbf{j}) \text{ m s}^{-1}$$

M

1 Accept 
$$\sqrt{-6^2+13^2}$$

- May not be explicit. If diagram used it must have correct orientation. Give if final angle correct. Use of  $\arctan\left(\pm\frac{8}{3}\right)$  or  $\arctan\left(\pm\frac{3}{8}\right)$  ( $\pm 20.6^{\circ}$  or  $\pm 69.4^{\circ}$ ) or equivalent on **their** resultant
- A1 cao. Do not accept -21°.
- **M**1 Use of N2L with accn used in vector form
- Any form. Units not required. isw. A1 F1 10a seen. Units not required. Must be a vector. [SC1 for  $a = \sqrt{3^2 + 5^2} / 5 = 1.17$ ]

3 8

3

476	51
-----	----

**Mark Scheme** 

Q 3		mark		Sub
(i)	$F = 14000 \times 0.25$	M1	Use of N2L . Allow $F = mga$ and wrong mass. No	
	so 3500 N	A1	extra forces.	2
(ii)	4000 - R = 3500 so 500 N	<b>B</b> 1	FT $F$ from (i). Condone negative answer.	1
(iii)	$1150 - R_{\rm T} = 4000 \times 0.25$	M1	N2L applied to truck (or engine) using all forces required. No extras. Correct mass. Do not allow use	
	so 150 N	A1	of $F = mga$ . Allow sign errors. cao	2
(iv)	either Component of weight down slope is	M1	Attempt to find cpt of <i>weight</i> (allow wrong mass). Accept $\sin \leftrightarrow \cos$ . Accept use of $m \sin \theta$ .	
	Extra driving force is cpt of mg down slope	M1	May be implied. Correct mass. No extra forces. Must have resolved weight component. Allow $\sin \leftrightarrow \cos$	
	14000 <i>g</i> sin 3°			
	= 14000×9.8×0.0523359 = 7180.49 so 7180 N (3 s. f.)	A1		
	or	M1	Attempt to find cpt of <i>weight</i> (allow wrong mass). Accept $sin \leftrightarrow cos$ . Accept use of $m sin \theta$ .	
	$D - 500 - 14000g\sin 3 = 14000 \times 0.25$	M1	N2L with all terms present with correct signs and mass. No extras. FT 500 N. Accept <b>their</b> $500 + 150$ for resistance. Must have resolved weight component.	
	<i>D</i> = 11180.49 so extra is 7180 N (3 s. f.)	A1	Allow $\sin \leftrightarrow \cos s$ . Must be the extra force.	3 8

Mark Scheme

	mark		Sub
either Need i opt 0 so $18t^2 - 1 = 0$	M1	Need not solve	
$\Rightarrow t^2 - \frac{1}{2}$ Only one root as $t > 0$	E1	Must astablish only one of the two roots is valid	
$r = \frac{1}{18}$ . Only one root as $r > 0$	LI	Must establish only one of the two roots is vanu	
Establish sign change in <b>j</b> cpt	B1		
Establish only one root	B1		2
$\mathbf{v} = 3 \mathbf{i} + 36t \mathbf{j}$	M1	Differentiate. Allow i or j omitted	
	A1		
Need I cpt 0 and this never happens	EI	Clear explanation. Accept '1 cpt always there' or equiv	3
$x = 3t$ and $y = 18t^2 - 1$	B1	Award for these two expressions seen.	
Eliminate <i>t</i> to give		-	
$y = 18\left(\frac{x}{3}\right)^2 - 1$	M1	<i>t</i> properly eliminated. Accept any form and brackets missing	
so $y = 2x^2 - 1$	A1	сао	
			3 8
			0
	mark		Sub
$0^2 = V^2 - 2 \times 9.8 \times 22.5$	M1	Use of appropriate <i>uvast</i> . Give for correct expression	
V = 21 so $21$ m s <sup>-1</sup>	E1	Clearly shown. Do not allow $v^2 = 0 + 2gs$ without	
		explanation. Accept using $V = 21$ to show $s = 22.5$ .	2
28 : 4 21	N/1		2
$28\sin\theta = 21$	NI I	Attempt to find angle of projection $A \parallel ow \sin \Theta = \cos \Theta$	
so $\theta = 48.59037$	A1	Attempt to find angle of projection. Anow sin ( ) cos.	
so $\theta = 48.59037$	A1	Attempt to find angle of projection. Attow sin (7 cos.	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{0.8} = \frac{15}{7}$	A1 B1	Or equivalent (time of whole flight)	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{2} \times 28 \times \cos(\text{their }\theta)$	A1 B1 M1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept <sup>1</sup> / <sub>2</sub> time.	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$	A1 B1 M1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept ½ time.	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$	A1 B1 M1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept ½ time. Do not accept 28 used for horizontal speed or vertical speed when calculating time.	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$	A1 B1 M1 B1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept ½ time. Do not accept 28 used for horizontal speed or vertical speed when calculating time. Horizontal speed correct	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$ 79.3725 so 79.4 m (3 s. f.)	A1 B1 M1 B1 A1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept <sup>1</sup> / <sub>2</sub> time. Do not accept 28 used for horizontal speed or vertical speed when calculating time. Horizontal speed correct cao. Accept answers rounding to 79 or 80. [If angle with vertical found in (ii) allow up to full	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$ 79.3725 so 79.4 m (3 s. f.)	A1 B1 M1 B1 A1	<ul> <li>Or equivalent (time of whole flight)</li> <li>Valid method for horizontal distance. Accept ½ time.</li> <li>Do not accept 28 used for horizontal speed or vertical speed when calculating time.</li> <li>Horizontal speed correct</li> <li>cao. Accept answers rounding to 79 or 80.</li> <li>[If angle with vertical found in (ii) allow up to full marks in (iii). If sin ↔ cos allow up to B1 B1 M0 A1]</li> </ul>	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$ 79.3725 so 79.4 m (3 s. f.)	A1 B1 M1 B1 A1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept $\frac{1}{2}$ time. Do not accept 28 used for horizontal speed or vertical speed when calculating time. Horizontal speed correct cao. Accept answers rounding to 79 or 80. [If angle with vertical found in (ii) allow up to full marks in (iii). If sin $\leftrightarrow$ cos allow up to B1 B1 M0 A1] [If $u^2 \sin 2\theta/g$ used then	2
so $\theta = 48.59037$ Time to highest point is $\frac{21}{9.8} = \frac{15}{7}$ Distance is $2 \times \frac{15}{7} \times 28 \times \cos(\text{their }\theta)$ 79.3725 so 79.4 m (3 s. f.)	A1 B1 M1 B1 A1	Or equivalent (time of whole flight) Valid method for horizontal distance. Accept $\frac{1}{2}$ time. Do not accept 28 used for horizontal speed or vertical speed when calculating time. Horizontal speed correct cao. Accept answers rounding to 79 or 80. [If angle with vertical found in (ii) allow up to full marks in (iii). If sin $\leftrightarrow$ cos allow up to B1 B1 M0 A1] [If $u^2 \sin 2\theta/g$ used then M1* Correct formula used. FT their angle.	2
	either Need j cpt 0 so $18t^2 - 1 = 0$ $\Rightarrow t^2 = \frac{1}{18}$ . Only one root as $t > 0$ or Establish sign change in j cpt Establish only one root $\mathbf{v} = 3 \mathbf{i} + 36t \mathbf{j}$ Need i cpt 0 and this never happens $x = 3t$ and $y = 18t^2 - 1$ Eliminate t to give $y = 18\left(\frac{x}{3}\right)^2 - 1$ so $y = 2x^2 - 1$ $0^2 = V^2 - 2 \times 9.8 \times 22.5$ V = 21 so $21$ m s <sup>-1</sup> $28\sin\theta = 21$	either Need j cpt 0 so $18t^2 - 1 = 0$ M1 $\Rightarrow t^2 = \frac{1}{18}$ . Only one root as $t > 0$ E1 or Establish sign change in j cpt B1 Establish only one root B1 $\mathbf{v} = 3 \mathbf{i} + 36t \mathbf{j}$ M1 Need i cpt 0 and this never happens E1 $x = 3t$ and $y = 18t^2 - 1$ B1 Eliminate t to give $y = 18\left(\frac{x}{3}\right)^2 - 1$ M1 so $y = 2x^2 - 1$ A1 $0^2 = V^2 - 2 \times 9.8 \times 22.5$ M1 V = 21 so $21$ m s <sup>-1</sup> E1	markeitherNeed j cpt 0 so $18t^2 - 1 = 0$ M1Need not solve $\Rightarrow t^2 = \frac{1}{18}$ . Only one root as $t > 0$ E1Must establish only one of the two roots is validorEstablish sign change in j cptB1Establish only one rootB1 $\mathbf{v} = 3 \mathbf{i} + 36t \mathbf{j}$ M1Differentiate. Allow i or j omittedA1Clear explanation. Accept 'i cpt always there' or equiv $x = 3t$ and $y = 18t^2 - 1$ B1Eliminate t to give $t$ properly eliminated. Accept any form and brackets $y = 18\left(\frac{x}{3}\right)^2 - 1$ M1 $correct y = 2x^2 - 1$ M1Use of appropriate <i>uvast</i> . Give for correct expression $e^2 = V^2 - 2 \times 9.8 \times 22.5$ M1 $V = 21$ so $21$ m s <sup>-1</sup> M1Attempt to find angle of projection. Allow sin $\epsilon \ge 0.5$ $28in \theta = 21$ M1

4 8

### 4761

### **Mark Scheme**

mark

**M**1

A1

**B**1

M1

**B**1

M1

A1

M1

A1

A1

### Q 6

(i)  $0.5 \times 2 \times 12 + 0.5 \times 4 \times 12$ so 36 m

(ii) 
$$8 - \frac{36}{12} = 5$$
 seconds

(iii) 
$$-6 \text{ m s}^{-2}$$

(iv) 
$$58.5 = 12 \times 6 + 0.5 \times a \times 36$$
  
so  $a = -0.75$ 

(v) 
$$a = -10 + \frac{9}{2}t - \frac{3}{8}t^2$$

$$a(1) = -10 + \frac{9}{2} - \frac{3}{8} = -5.875$$

(vi) 
$$s = \int \left( 12 - 10t + \frac{9}{4}t^2 - \frac{1}{8}t^3 \right) dt$$

$$= 12t - 5t^{2} + \frac{3}{4}t^{3} - \frac{1}{32}t^{4} + C$$
  
s = 0 when t = 0 so C = 0

s(8) = 32

### either

(vii) s(2) = 9.5 and s(4) = 8

Displacement is negative Car going backwards or Evaluate v(t) where 2 < t < 4 or appeal to shape of the graph Velocity is negative

# SubAttempt at sum of areas or equivalent. No extra areas.2cao1Attempt at accn for $0 \le t \le 2$ <br/>must be - ve or equivalent2Use of uvast with 12 and 58.52Differentiationcao3

- M1Attempt to integrate A1 At least one term correct A1 All correct. Accept + C omitted A1\* Clearly shown cao (award even if A1\* is not given) A1 B1 Both calculated correctly from **their** *s*. No further marks if **their**  $s(2) \le s(4)$ E1 Do not need car going backwards throughout the E1 interval. **B**1 e.g. v(3) = -1.125No further marks if **their**  $v \ge 0$ E1
- E1 Do not need car going backwards throughout the interval
   [Award WW2 for 'car going backwards'; WW1 for velocity or displacement negative]

5

Q 7

(i)  $T_{AB} \sin \alpha = 147$ 

so 
$$T_{AB} = \frac{147}{0.6}$$

$$= 245 \text{ so } 245 \text{ N}$$

(ii) 
$$T_{\rm BC} = 245\cos\alpha$$

$$= 245 \times 0.8 = 196$$

- (iii) Geometry of A, B and C and weight of B the
  - same and these determine the tension

(iv)

## either

Realise that 196 N and 90 N are horiz and vert M forces where resultant has magnitude and line of action of the tension  $\tan \beta = 90/196$  H  $\beta = 24.6638...$  so 24.7 (3 s. f.) M  $T = \sqrt{196^2 + 90^2}$  M T = 215.675... so 216 N (3 s. f.) H or  $\uparrow T \sin \beta - 90 = 0$  H  $\rightarrow T \cos \beta - 196 = 0$  H Solving  $\tan \beta = \frac{90}{196} = 0.45918...$  M  $\beta = 24.6638...$  so 24.7 (3 s. f.) A

- T = 215.675... so 216 N (3 s. f.)
- (v) Tension on block is 215.675.. N (pulley is smooth and string is light)  $M \times 9.8 \times \sin 40 = 215.675... + 20$

$$M = 37.4128...$$
 so 37.4 (3 s. f.)

mark		Sub
M1	Attempt at resolving. Accept $sin \leftrightarrow cos$ . Must have <i>T</i> resolved and equated to 147.	
B1	Use of 0.6. Accept correct subst for angle in wrong	
A1	expression. Only accept answers agreeing to 3 s. f. [Lami: M1 pair of ratios attempted; B1 correct sub;A1]	3
M1	Attempt to resolve 245 and equate to <i>T</i> , or equiv Accept $\sin \leftrightarrow \cos$	
E1	Substitution of 0.8 clearly shown [SC1 $245 \times 0.8 = 196$ ] [Lami: M1 pair of ratios attempted; E1]	2
E1	Mention of two of: same weight: same direction AB:	
E1	same direction BC Specific mention of same geometry & weight or recognition of same force diagram	2
B1 B1	No extra forces. Correct orientation and arrows ' <i>T</i> ' 196 and 90 labelled. Accept 'tension' written out.	
M1	Allow for only $\beta$ or <i>T</i> attempted	
B1 A1	Use of arctan (196/90) or arctan (90/196) or equiv	
M1 E1	Use of Pythagoras	
B1 B1	Allow if $T = 216$ assumed Allow if $T = 216$ assumed	
M1	Eliminating <i>T</i> , or	
A1 E1	[If $T = 216$ assumed, B1 for $\beta$ ; B1 for check in 2 <sup>nd</sup> equation; E0]	7
B1	May be implied. Reasons not required.	
M1 A1	<i>Equating</i> their tension on the block unresolved $\pm 20$ to weight component. If equation in any other direction, normal reaction must be present. Correct	

A1 Accept answers rounding to 37 and 38