

OXFORD CAMBRIDGE AND RSA EXAMINATIONS

Advanced Subsidiary General Certificate of Education Advanced General Certificate of Education

MEI STRUCTURED MATHEMATICS

4752

Concepts for Advanced Mathematics (C2)

6 JUNE 2006

Tuesday

Afternoon

1 hour 30 minutes

Additional materials: 8 page answer booklet Graph paper MEI Examination Formulae and Tables (MF2)

TIME 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet.
- Answer **all** the questions.
- There is an **insert** for use in Question **12**.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are advised that an answer may receive **no marks** unless you show sufficient detail of the working to indicate that a correct method is being used.
- The total number of marks for this paper is 72.

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Section A (36 marks)

- 1 Write down the values of $\log_a a$ and $\log_a (a^3)$. [2]
- 2 The first term of a geometric series is 8. The sum to infinity of the series is 10.Find the common ratio.

[3]

3 θ is an acute angle and $\sin \theta = \frac{1}{4}$. Find the exact value of $\tan \theta$. [3]

4 Find
$$\int_{1}^{2} \left(x^4 - \frac{3}{x^2} + 1 \right) dx$$
, showing your working. [5]

- 5 The gradient of a curve is given by $\frac{dy}{dx} = 3 x^2$. The curve passes through the point (6, 1). Find the equation of the curve. [4]
- 6 A sequence is given by the following.

$$u_1 = 3$$
$$u_{n+1} = u_n + 5$$

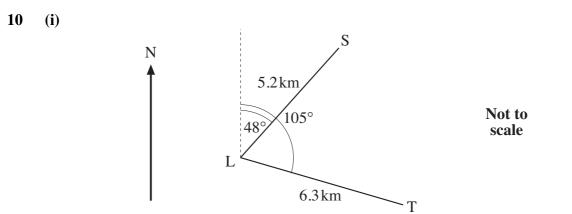
- (i) Write down the first 4 terms of this sequence. [1]
- (ii) Find the sum of the 51st to the 100th terms, inclusive, of the sequence. [4]
- 7 (i) Sketch the graph of $y = \cos x$ for $0^\circ \le x \le 360^\circ$.

On the same axes, sketch the graph of $y = \cos 2x$ for $0^{\circ} \le x \le 360^{\circ}$. Label each graph clearly. [3]

- (ii) Solve the equation $\cos 2x = 0.5$ for $0^{\circ} \le x \le 360^{\circ}$. [2]
- 8 Given that $y = 6x^3 + \sqrt{x} + 3$, find $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$. [5]
- 9 Use logarithms to solve the equation $5^{3x} = 100$. Give your answer correct to 3 decimal places. [4]



Section B (36 marks)





At a certain time, ship S is 5.2 km from lighthouse L on a bearing of 048°. At the same time, ship T is 6.3 km from L on a bearing of 105°, as shown in Fig. 10.1.

For these positions, calculate

- (*A*) the distance between ships S and T,
- (B) the bearing of S from T.

(ii)

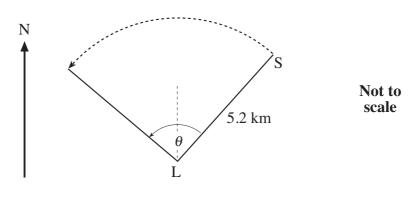


Fig. 10.2

Ship S then travels at 24 km h^{-1} anticlockwise along the arc of a circle, keeping 5.2 km from the lighthouse L, as shown in Fig. 10.2.

Find, in radians, the angle θ that the line LS has turned through in 26 minutes.

Hence find, in degrees, the bearing of ship S from the lighthouse at this time. [5]

[3]

[3]

- 11 A cubic curve has equation $y = x^3 3x^2 + 1$.
 - (i) Use calculus to find the coordinates of the turning points on this curve. Determine the nature of these turning points. [5]
 - (ii) Show that the tangent to the curve at the point where x = -1 has gradient 9.

Find the coordinates of the other point, P, on the curve at which the tangent has gradient 9 and find the equation of the normal to the curve at P.

Show that the area of the triangle bounded by the normal at P and the *x*- and *y*-axes is 8 square units. [8]

12 Answer the whole of this question on the insert provided.

A colony of bats is increasing. The population, P, is modelled by $P = a \times 10^{bt}$, where t is the time in years after 2000.

- (i) Show that, according to this model, the graph of $\log_{10} P$ against *t* should be a straight line of gradient *b*. State, in terms of *a*, the intercept on the vertical axis. [3]
- (ii) The table gives the data for the population from 2001 to 2005.

Year	2001	2002	2003	2004	2005
t	1	2	3	4	5
Р	7900	8800	10000	11 300	12800

Complete the table of values on the insert, and plot $\log_{10} P$ against *t*. Draw a line of best fit for the data. [3]

[2]

- (iii) Use your graph to find the equation for *P* in terms of *t*. [4]
- (iv) Predict the population in 2008 according to this model.