

1.

$$y = 3^x + 2x$$

(a) Complete the table below, giving the values of y to 2 decimal places.

x	0	0.2	0.4	0.6	0.8	1
y	1	1.65				5

(2)

(b) Use the trapezium rule, with all the values of y from your table, to find an approximate

value for $\int_0^1 (3^x + 2x) dx$.

(4)



6.

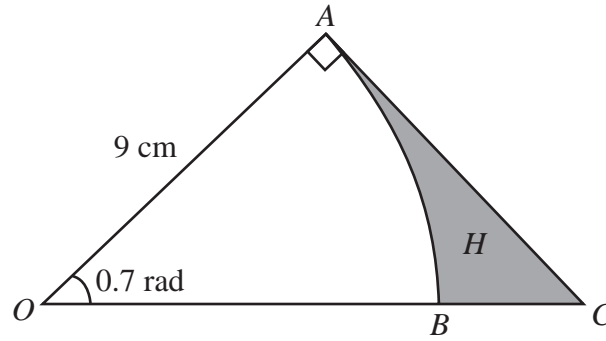


Figure 1

Figure 1 shows the sector OAB of a circle with centre O , radius 9 cm and angle 0.7 radians.

(a) Find the length of the arc AB . (2)

(b) Find the area of the sector OAB . (2)

The line AC shown in Figure 1 is perpendicular to OA , and OBC is a straight line.

(c) Find the length of AC , giving your answer to 2 decimal places. (2)

The region H is bounded by the arc AB and the lines AC and CB .

(d) Find the area of H , giving your answer to 2 decimal places. (3)



8.

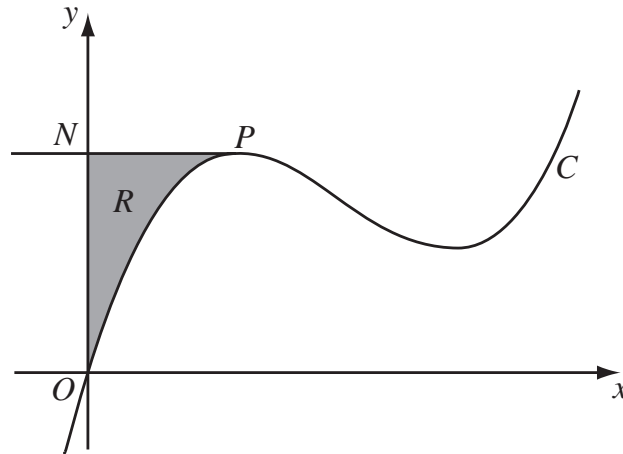


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = x^3 - 10x^2 + kx,$$

where k is a constant.

The point P on C is the maximum turning point.

Given that the x -coordinate of P is 2,

(a) show that $k = 28$. (3)

The line through P parallel to the x -axis cuts the y -axis at the point N .
 The region R is bounded by C , the y -axis and PN , as shown shaded in Figure 2.

(b) Use calculus to find the exact area of R . (6)



Question 8 continued

Blank lined area for writing the answer to Question 8.



9. The adult population of a town is 25 000 at the end of Year 1.

A model predicts that the adult population of the town will increase by 3% each year, forming a geometric sequence.

(a) Show that the predicted adult population at the end of Year 2 is 25 750. (1)

(b) Write down the common ratio of the geometric sequence. (1)

The model predicts that Year N will be the first year in which the adult population of the town exceeds 40 000.

(c) Show that

$$(N - 1)\log 1.03 > \log 1.6 \quad (3)$$

(d) Find the value of N . (2)

At the end of each year, each member of the adult population of the town will give £1 to a charity fund.

Assuming the population model,

(e) find the total amount that will be given to the charity fund for the 10 years from the end of Year 1 to the end of Year 10, giving your answer to the nearest £1000. (3)



10. The circle C has centre $A(2, 1)$ and passes through the point $B(10, 7)$.

(a) Find an equation for C . (4)

The line l_1 is the tangent to C at the point B .

(b) Find an equation for l_1 . (4)

The line l_2 is parallel to l_1 and passes through the mid-point of AB .

Given that l_2 intersects C at the points P and Q ,

(c) find the length of PQ , giving your answer in its simplest surd form. (3)

Handwriting lines for part (c)



