

2. (a) Find the first 3 terms, in ascending powers of x , of the binomial expansion of

$$(3 + bx)^5$$

where b is a non-zero constant. Give each term in its simplest form.

(4)

Given that, in this expansion, the coefficient of x^2 is twice the coefficient of x ,

- (b) find the value of b .

(2)



4. The circle C has equation $x^2 + y^2 + 4x - 2y - 11 = 0$

Find

(a) the coordinates of the centre of C , (2)

(b) the radius of C , (2)

(c) the coordinates of the points where C crosses the y -axis, giving your answers as simplified surds. (4)



5.

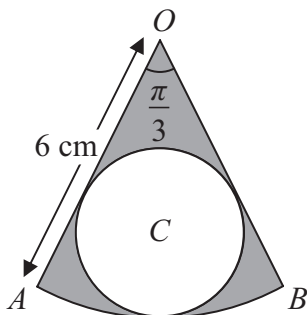


Figure 1

The shape shown in Figure 1 is a pattern for a pendant. It consists of a sector OAB of a circle centre O , of radius 6 cm, and angle $AOB = \frac{\pi}{3}$. The circle C , inside the sector, touches the two straight edges, OA and OB , and the arc AB as shown.

Find

(a) the area of the sector OAB , (2)

(b) the radius of the circle C . (3)

The region outside the circle C and inside the sector OAB is shown shaded in Figure 1.

(c) Find the area of the shaded region. (2)



7. (a) Solve for $0 \leq x < 360^\circ$, giving your answers in degrees to 1 decimal place,

$$3 \sin(x + 45^\circ) = 2$$

(4)

(b) Find, for $0 \leq x < 2\pi$, all the solutions of

$$2 \sin^2 x + 2 = 7 \cos x$$

giving your answers in radians.

You must show clearly how you obtained your answers.

(6)



8.

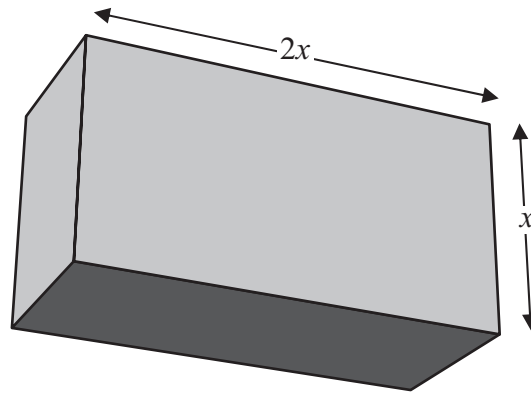


Figure 2

A cuboid has a rectangular cross-section where the length of the rectangle is equal to twice its width, x cm, as shown in Figure 2.

The volume of the cuboid is 81 cubic centimetres.

- (a) Show that the total length, L cm, of the twelve edges of the cuboid is given by

$$L = 12x + \frac{162}{x^2} \tag{3}$$

- (b) Use calculus to find the minimum value of L . (6)

- (c) Justify, by further differentiation, that the value of L that you have found is a minimum. (2)



9.

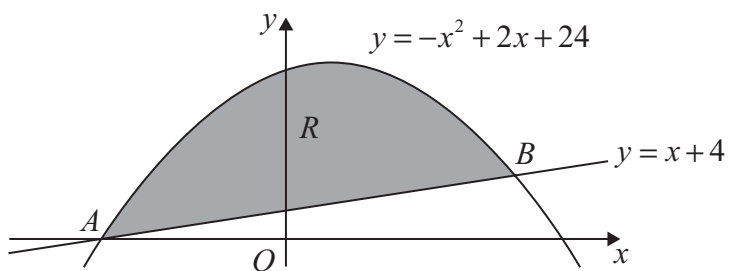


Figure 3

The straight line with equation $y = x + 4$ cuts the curve with equation $y = -x^2 + 2x + 24$ at the points A and B , as shown in Figure 3.

(a) Use algebra to find the coordinates of the points A and B . (4)

The finite region R is bounded by the straight line and the curve and is shown shaded in Figure 3.

(b) Use calculus to find the exact area of R . (7)



