

Mark Scheme (Results)

Summer 2013

GCE Statistics 1 (6683/01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.
- 8. In some instances, the mark distributions (e.g. M1, B1 and A1) printed on the candidate's response may differ from the final mark scheme.

Question		Scheme			
1.	(a)	$(S_{th}) = 64980 - \frac{7150 \times 110}{9} = -22408.9$ -22400 $(S_{hh}) = 7171500 - \frac{7150^2}{9} = 1491222.2$ 1490000	M1 A1		
		$(S_{hh}) = 7171500 - \frac{7150^2}{9} = 1491222.2$ <u>1 490 000</u>	A1		
	<i>a</i> >	22 400 0	(3)		
	(b)	$r = \frac{-22408.9}{\sqrt{1491222 \times 371.56}} = -0.95200068$ awrt $-$ 0.952	M1A1		
	(c)	Yes as r is close to -1 (if $-1 < r < -0.5$) or Yes as r is close to 1 (if $1 > r > 0.5$) [If $-0.5 \le r \le 0.5$ allow "no since r is close to 0"] [If $ r > 1$ award B0]	B1ft (1)		
	(d)	$b = \frac{-22408.9}{1491222.2} = -0.015027 \qquad \text{(allow } \frac{-56}{3725}\text{)} \qquad \text{awrt} - 0.015027$ $a = \frac{110}{9} \text{-"their } b \text{"} \times \frac{7150}{9} = (12.20.015 \times 794.4), = 24.1604 \text{ so } t = 24.2 - 0.0015 \times 794.4$			
		$u = \frac{1}{9} - \text{then } b \times \frac{1}{9} = (12.2 - 0.013 \times 794.4) = 24.1004 \text{ so } t = 24.2 - 0.004$	$\begin{array}{c c} \mathbf{015h} & \mathbf{M1, A1} \\ & \mathbf{(4)} \end{array}$		
	(e)	0.015 is the <u>drop</u> in temp, (in 0 C), for every 1(m) <u>increase</u> in height above sea level.			
	(f)	Change = $("24.2 - 0.015" \times 500) - ("24.2 - 0.015" \times 1000) \text{ or } 500 \times "0.015"$ = ± 7.5 (awrt ± 7.5) (only ft a value < 1)	100) M1 A1ft (2) (13 marks)		
		Notes			
	(a)	M1 for at least one correct expression (condone transcription error) $1^{\text{st}} \text{ A1 for } S_{hh} = \text{awrt } 1 \text{ 490 000 or } S_{th} = \text{awrt } -22 \text{ 400 (Condone } S_{xx} \text{ or } S_{xy} = \dots \text{ or even } S_{yy} = \dots)$			
	2^{nd} A1 for $S_{th} = -22\ 400\ \text{and}\ S_{hh} = 1\ 490\ 000\ \text{only}$. [This mark is assessing correct roots]				
		(Allow no labels but mis-labelling S_{th} as S_{hh} etc loses the final A1)			
	(b)	M1 for attempt at correct formula. Allow minor transcription errors of 2 or 3 digits. Must have their S_{hh} , S_{th} and given S_{tt} (3sf or better) in the correct places. Condone missing "–"			
		Award M1A0 for awrt -0.95 with no expression seen. M0 for $\frac{64980}{\sqrt{7171500 \times 7.864}}$			
	(c)	B1ft must comment on supporting and state: high/strong/clear (negative or positive) correlation "points lie close to a straight line" is B0 since there is no evidence of this.			
	(d)	1^{st} M1 for a correct expression for b. Follow through their S_{hh} & S_{th} . Cond.	done missing "-"		
		$1^{\text{st}} \text{ A}1$ for awrt -0.015 or allow exact fraction from rounded values. $2^{\text{nd}} \text{ M}1$ for a correct method for a . Follow through their value of b	0.015 N. 6		
		for a correct equation for t and h with $a = \text{awrt } 24.2$ and $b = \text{awrt } -0.2$	U.U15 INO Iractions		
	(e)	B1 Must mention h (or height) and t (or temperature) and their (1 sf) value of b in a correct comment			
	(f)	M1 for a correct expression seen based on their equation. Allow transcription If answer is $500 \times$ their b to 2sf and < 100 (M1A1), If answer is $500 \times$ their b to 2sf and			

Question	Scheme	Marks		
2. (a)	25 (allow any x where $24 < x < 26$)	B1		
(b)	$\mathbf{Q_2}$ (or median or m) = 51	B1 (1)		
	$IQR = 63 - 46 = 17$ (or $Q_3 - Q_1 = 17$)	M1, A1		
(c)	Outliers given by $46 - 1.5 \times 17 = 20.5$ or $63 + 1.5 \times 17 = 88.5$ Outliers limits are 20.5 and 88.5	(3) M1 A1		
	Females Allow lower whisker to 20.5 and upper whisker to 88.5	M1		
	Males * Do not allow a mix of whiskers e.g 20.5 and 85 Do not allow both sets of	A1ft		
	10 20 30 40 50 60 70 80 90 100 whiskers Mark	B1 (5)		
(d)	Medians: Median for females lower than males	(5)		
	IQR: IQR for females smaller than males. Allow "lower/higher" but not "wider" Pange: Pange of females is less than males.	B1ft B1ft		
	Skewness: Male and female marks are both positively skew Ignore other statements about average, spread, mean, st. Dev, variation, outliers etc			
	Ignore other statements about average, spread, mean, st. Dev, variation, outliers etc Notes (11)			
	Mark (b) and (c) together BUT must see clear statement that median (or m or Q_2) = 51 and	d IQR = 17		
(b)	-			
(c)	A fully correct box-plot (either version) with no supporting work scores 5/5. Otherwise: 1 st M1 for correct attempt to calc' at least one limit for outliers, ft their quartiles or IQR or award for sight of 20.5 or 88.5 1 st A1 for identifying both limits of 20.5 and 88.5 2 nd M1 for a box with an upper and a lower whisker(s) with at least 2 correct values (or correct ft) (condone no median marked) (condone 2 upper or 2 lower whiskers) 2 nd A1ft for their 20.5 or 26,46,51,63 and 85 or their 88.5 in appropriate places and readable off their scale. Follow through their 20.5 and their 88.5 only, other values need to be correct If there are 2 upper or 2 lower whiskers A0 B1 for only 2 outliers appropriately marked at 14 and 90 Do not award if whiskers go beyond these values. Apply ± 0.5 square accuracy for diagram A box plot not on the graph paper can only score the 1 st M1A1			
(d)	In (d) ft from their diagrams (if no diagram then use their values) 1 st B1ft 2 nd B1ft for one correct comment comparing median, IQR, range or skewness for a second correct comment comparing median, IQR, range or skewness Do not allow contradictory statements	s		

Question	Scheme		Marks
3. (a)	$\frac{35+75}{200} = 0.55$		M1 A1
	200		
(b)	200-2		(2)
	$\frac{200-2}{200} = 0.99$		M1 A1
			(2)
(c)	(c) $\left[P(W \mid C)\right] = \frac{P(W \cap C)}{P(C)} = \frac{30/200}{80/200} = \frac{30}{80} = 0.375$		
	$[\Gamma(W \mid C)] = \frac{1}{P(C)} = \frac{1}{80} = \frac{1}{$		M1 A1
	, 200		(2)
(d)	C_{64} g F	Allow diagrams with intersections between <i>F</i> ,	M1
	$\langle 16 \rangle \langle 1 \rangle \rangle$	C and H provided these	B1 for 9, 1
	(0)	are marked with 0.	B1 for 77,33
	33 B (0)	If their diagram indicates	B1 for 64,16
	77	extra empty regions do not	
	H	treat a blank as 0.	(4)
	1+16+33		
(e)	$\frac{1+16+33}{200} = 0.25$		M1 A1 (2)
			(12 marks)
	Notes		
	Correct answers only score full 1 If a probability is not in [0,	-	
(a)	M1 for denominator of 200 and attempt to add $2 + 8$		
A1 for 0.55 or exact equivalent fraction e.g. $\frac{11}{20}$			
(b)	M1 for a fully appropriate expression (e.g. 1, 0.01)		
(0)	(b) M1 for a fully correct expression (e.g. 1–0.01) A1 for 0.99 or an exact equivalent fraction		
	-		
(c)	M1 for a correct ratio or a correct formula and at least denom. BLIT award M0 if num is $P(W) \times P(C) = 0$	± ``	et num or
denom). BUT award M0 if num is $P(W) \times P(C) = \frac{67}{200} \times \frac{80}{200}$ or if num>denom A1 for 0.375 or 3/8 or any exact equivalent.			
	711 101 0.575 of 576 of any exact equivalent.		
(d)	(d) M1 for a box and the 3 regions F , C and H labelled or <u>implied</u> and single set B labelled. There should be no intersections between F , C and H unless marked by zeros. They may have 3 circles for F , C and B with $H = F' \cap C'$ etc. Condone lack of zero in the <u>given</u> diagram.		
F	1^{st} B1 for the 9 and 1 or 0.045 and 0.005 (o.e.) in the correct regions May have B in 3		
Н	2^{nd} B1 for the 77 and 33 or 0.385 and 0.165 (o.e.) in the correct regions bits that are		
C	$C = 3^{rd} B1$ for the 64 and 16 or 0.32 and 0.08 (o.e.) in the correct regions. disconnected.		
(e)	M1 for a numerator made up of their $1 + \text{their } 16 + \text{their } 33 \text{ and a denom of } 200 \text{ and } \text{num} < 200 \text{ and } 100 and$		l num < 200
	Also allow sum of their probabilities (provided sur	m < 1)	
	A1 for 0.25 or any exact equivalent		

Question	Scheme			
4. (a)	$\sum ft = 4837.5$ (allow 4838 or 4840)	B1		
	Mean = $\frac{"4837.5"}{200}$ = 24.1875 awrt $\frac{24.2}{16}$ or $\frac{387}{16}$	M1 A1		
	$\sigma = \sqrt{\frac{134281.25}{200} - \left(\frac{4837.5}{200}\right)^2}$	M1		
	= 9.293 (accept $s = 9.32$) awrt 9.29	A1 (5)		
(b)	$Q_2 = [20.5] + \frac{(100/100.5 - 62)}{88} \times 5 = 22.659$ awrt <u>22.7</u>	M1 A1 (2)		
(c)	$Q_1 = 10.5 + \frac{(50/50.25)}{62} \times 10[=18.56]$ (*) $(n + 1 \text{ gives } 18.604)$	B1 cso		
(d)	$Q_3 = 25.5$ (Use of $n + 1$ gives 25.734) IQR = 6.9 (Use of $n + 1$ gives 7.1)	B1 B1 ft		
(e)	The data is skewed (condone "negative skew")	B1 (2) (1)		
(f)	Mean decreases and st. dev. remains the same. [Must mention mean and st. dev.] (from(a)) The median and quartiles would decrease. [Must refer to median and at least Q_1 .] ((b)(c)) The IQR would remain unchanged (from (d))			
	Notes			
(a)	Correct answers only score full marks in each part except (c) B1 for 4837.5 or 4838 or 4840 seen. If no $\sum ft$ seen (or attempt at $\sum ft$ seen), B1 can be implied by a correct mean of awrt 24.2			
	1 st M1 for attempt at their $\frac{\sum_{f}^{ft}}{\sum_{f}}$ allow 1sf so $\sum_{f} f = \text{awrt } 200$ and $\sum_{f} ft = \text{awrt } 5000$.			
	Or award M1 for a clear attempt at mean where at least 4 correct products of $\sum ft$ are seen 2^{nd} M1 for correct expression including square root seen. Follow through their mean. Allow a transcription error in 134281.25 but not an incorrect re-calculation.			
(b)	M1 for a correct fraction $\times 5$. Ignore end point but must be +. Allow use of $(n + 1)$ giving 100.5			
(c)	B1cso for a fully correct expression including end point. NB Answer is given. Allow use of $(n + 1)$ giving 50.25but use of 50.5 scores B0			
(d)	$1^{\text{st}} B1$ for 25.5 (or awrt 25.7 using $n+1$) $2^{\text{nd}} B1 \text{ft}$ for their Q_3 – their Q_1 (or 18.6) (provided > 0) Accept awrt 2sf. Correct ans. on	ly scores 2/2		
(e)	B1 Must mention that the data is skewed or not symmetrical. Do not award for "outliers"			
(f)	1 st B1 for one correct comment from the above. May refer to parts (a), (b), (c) or (c 2 nd B1 for two correct comments from the above for all 3 correct comments from the above	d)		

Question	Scheme			
5. (a)	3a + 2b = 0.7	M1		
	a + 2a + 3a + 4b + 5b + 1.8 = 4.2 or $6a + 9b = 2.4$	M1		
	5b = 1 Attempt to solve	M1		
	b = 0.2 cao	B1		
	$a = \overline{0.1}$ cao	B1		
		(5)		
(b)	$E(X^{2}) = 1 \times 0.1 + 2^{2} \times 0.1 + 3^{2} \times 0.1 + 4^{2} \times 0.2 + 5^{2} \times 0.2 + 6^{2} \times 0.3 \ (= 20.4) $ (*)	B1cso		
	$E(X_i) = 1 \times 0.1 + 2 \times 0.1 + 3 \times 0.1 + 4 \times 0.2 + 3 \times 0.2 + 6 \times 0.3 (= 20.4)$			
(a)	$[V_{cr}(V) \ 1\ 20\ 4\ 4\ 2^2\ [\ 2.76]$	(1) M1		
(c)				
	Var(5-3X) = 9 Var(X)			
	$=$ <u>24.84</u> or <u>24.8</u> (allow $\frac{621}{25}$) cao	A1		
		(3)		
(d)	[5k = 1 so] k = 0.2	B1		
		(1)		
(e)	P(Y = 1) = 0.1	B1		
	e.g. $P(Y = 2) = F(2) - F(1) = 0.1$	M1		
	$\begin{vmatrix} y & 1 & 2 & 3 & 4 & 5 \end{vmatrix}$			
	Condone use of $X(x)$ instead of $Y(y)$	A1		
	$P(Y = y) \mid 0.1 \mid 0.1 \mid 0.4 \mid 0.2 \mid 0.2$ Ignore incorrect or no label if table fully correct			
		(3)		
(f)	$P(X = 1) \times P(Y = 1) = 0.01$ cao	M1, A1 (2)		
		(15 marks)		
	Notes			
	Probabilities outside [0, 1] should be awarded M0			
(a)	1^{st} M1 for an attempt at a linear equation in a and b based on sum of probs. = 1			
	2^{nd} M1 for an attempt at a second linear equation in a and b based on $E(X) = 4.2$ Allow one slip.			
	3^{rd} M1 for an attempt to solve their 2 linear equations based on sum of probs and E(X). Must reduce to			
	a linear equation in one variable. 1^{st} B1 for b and 2^{nd} B1 for a . Answers only score B1B1 only			
	The 3 rd M1 may be implied if M2 is scored and both correct answers are given.			
ALT				
	1^{st} M1 for showing that sum of probs. = 1			
	2^{nd} M1 for showing that E(X) = 4.2			
	3^{rd} M1 for an overall comment "(therefore) $a = \dots$ and $b = \dots$ " No comment loses this mark.			
(b)	B1cso for a fully correct expression (no incorrect work seen). E.g. allow $14 \times 0.1 + 41 \times 0$	$.2 + 36 \times 0.3$		
	Or $0.1+0.4+0.9+3.2+5+10.8$. Allow in a table (with 20.4) but without "+" ex	plicitly seen.		
(c)	1^{st} M1 for a correct expression for Var(X). Must see -4.2^2			
	2^{nd} M1 for $(-3)^2$ Var(X) or better, no need for a value. Accept -3^2 if it clearly is used as +9 later.			
	2 Wil for (3) var(1) of better, no need for a variet. Therefor 3 in it clearly is used	as 19 later.		
(e)	B1 for $P(Y=1) = 0.1$			
(6)	B1 for $P(Y = 1) = 0.1$ M1 for correct use of $F(y)$ to find one other prob. Can ft their k if finding $P(Y = y)$ for $y > 2$			
	Can be implied by one other prob. correct fr Look out for $P(3) = 3k - 0.2$ or $P(4) = P(5) = k$.			
	Can be implied by one other prob. correct or correct it. Look out for $P(3) = 3k - 0.2$ of $P(4) = P(3) = k$. A1 for a fully correct probability distribution. Correct table only is $3/3$			
	AT 101 a fully correct probability distribution. Correct table only is 3/3			
(f)	M1 for a correct expression or answer ft their $P(Y = 1)$ and their $P(X = 1)$			
	M1 for a correct expression or answer ft their $P(Y = 1)$ and their $P(X = 1)$ A1 for 0.01 or exact equivalent only			
	1			
	Don't ISW here e.g. $0.1 \times 0.1 + 0.1 \times 0.1$ or $2 \times 0.1 \times 0.1$ are M0A0			

Ques	tion	Scheme	
6.	(a)	[Let X be the amount of beans in a tin. $P(X < 200) = 0.1$]	
		$\frac{200 - \mu}{7.8} = -1.2816$ [calc gives 1.28155156]	M1 B1
		$\mu = 209.996$ awrt 210	A1
			(3)
	(b)	$P(X > 225) = P\left(Z > \frac{225 - "210"}{7.8}\right)$	M1
		$= P(Z > 1.92) \underline{\text{or}} 1 - P(Z < 1.92) $ (allow 1.93)	A1
		= 1 - 0.9726 = 0.0274 (or better) [calc gives 0.0272037] = 0.0274	
		= awrt 2.7% allow 0.027	A1
	(c)	[Let Y be the new amount of beans in a tin]	(3)
	(C)	$\frac{210 - 205}{\sigma} = 2.3263 \text{or} \frac{200 - 205}{\sigma} = -2.3263 \text{[calc gives 2.3263478]}$ $\sigma = \frac{5}{2.3263}$	M1 B1
		$\sigma = \frac{5}{}$	dM1
		2.3263	
		$\sigma = 2.15 (2.14933)$	A1 (4)
			(10 marks)
		Notes	
		Condone poor handling of notation if answers are correct but A marks must have corre	_
	(a)	M1 for an attempt to standardise (allow \pm) with 200 and 7.8 and set = \pm any z value.	
		for $z = \pm 1.2816$ (or better used as a z)[May be implied by 209.996(102) or for awrt 210 (can be scored for using 1.28 but then they get M1B0A1)	better seen]
		The 210 must follow from correct working – sign scores A0	
		If answer is awrt 210 and 209.996 or better seen then award M1B1A1	
		z = 1.28 gives 209.984 and $z = 1.282$ gives 209.9996 and both score M1B0A1	
		If answer is awrt 210 or awrt 209.996 then award M1B0A1 (unless of course $z = 1.2$	2816 is seen)
	(b)	M1 for attempting to standardise with 225, their mean and 7.8. Allow \pm	
	` /	1^{st} A1 for $Z > \text{awrt } 1.92/3$. Allow a diagram but must have $1.92/3$ and correct area in	ndicated.
		Must have the Z so $P(X > 225)$ with or without a diagram is not sufficient.	
		Award for $1 - 0.9726$ or $1 - 0.9732$	2/2
		2 nd A1 for 2.7 % or better (calculator gives 2.72) Allow awrt 0.027. Correct ans s	cores 3/3
	(c)	1 st M1 for an attempt to standardise with 200 or 210, 205 and σ and set = \pm any z val	ue $(z > 2)$
		B1 for $z = 2.3263$ (or better) and compatible signs.	22.1
		If B0 in (a) for using a value in [1.28, 1.29) but not using 1.2816: allow awrt 2. 2^{nd} dM1 Dependent on the first M1 for correctly rearranging to make $\sigma =$ May b	
		e.g. $\frac{5}{\sigma} = 2.32 \rightarrow \sigma = 2.16$ (M1A0) BUT must have $\sigma > 0$	c mipheu
		A1 for awrt 2.15. Must follow from correct working but a range of possible z va	lues will do
		NB $2.320 < z \le 2.331$ will give an answer of awrt 2.15	

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