

| Question |  | Answer | Marks |  |  |
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| $\mathbf{3}$ | (i) |  | $\begin{array}{l}\text { graph of shape with vertices at }(-2,-3), \\ (0,0) \text { and }(2,-4)\end{array}$ | 2 | M1 for 2 vertices correct |
| $[2]$ |  |  |  |  |  |$)$


| Question |  | Answer <br> $3 a+12[=a c+5 f]$ <br> $3 a-a c=5 f-12$ or ft $a(3-c)=5 f-12$ or ft <br> $[a=] \frac{5 f-12}{3-c}$ oe or ft as final answer | MarksM1M1M1M1[4] | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5 |  |  |  | for expanding brackets correctly for collecting $a$ terms on one side, remaining terms on other <br> for factorising $a$ terms; may be implied by final answer <br> for division by their two-term factor; for all 4 marks to be earned, work must be fully correct | annotate this question if partially correct ft only if two $a$ terms <br> ft only if two $a$ terms, needing factorising may be earned before $2^{\text {nd }} \mathrm{M} 1$ |
| 6 |  | $\begin{aligned} & (3 x+1)(x+3) \\ & \\ & x<-3 \\ & {[\mathrm{or}]} \\ & x>-1 / 3 \text { oe } \end{aligned}$ | M1 <br> A1 <br> A1 <br> [3] | or $3(x+1 / 3)(x+3)$ <br> or for $-1 / 3$ and -3 found as endpoints eg by use of formula <br> mark final answers; <br> allow only A1 for $-3>x>-1 / 3$ oe as final answer or for $x \leq-3$ and $x \geq-1 / 3$ <br> if M0, allow SC1 for sketch of parabola the right way up with their solns ft their endpoints | A0 for combinations with only one part correct eg $-3>x<-1 / 3$, though this would earn M1 if not already awarded |




| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | (i) | $3 n^{2}+6 n+5$ isw | B2 <br> [2] | M1 for a correct expansion of at least one of $(n+1)^{2}$ and $(n+2)^{2}$ |  |
| 9 | (ii) | odd numbers with valid explanation | B2 <br> [2] | marks dep on 9(i) correct or starting again <br> for B2 must see at least odd $\times$ odd $=$ odd [for $3 n^{2}$ ] (or when $n$ is odd, [3] $n^{2}$ is odd) and odd $[+$ even $]+$ odd $=$ even soi, <br> condone lack of odd $\times$ even $=$ even for $6 n$; condone no consideration of $n$ being even <br> or B2 for deductive argument such as: $6 n$ is always even [and 5 is odd] so $3 n^{2}$ must be odd so $n$ is odd <br> B1 for odd numbers with a correct partial explanation or a partially correct explanation <br> or B1 for an otherwise fully correct argument for odd numbers but with conclusion positive odd numbers or conclusion negative odd numbers <br> B0 for just a few trials and conclusion | accept a full valid argument using odd and even from starting again <br> Ignore numerical trials or examples in this part - only a generalised argument can gain credit |


| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | (i) | $(7,0)$ | $\begin{gathered} 1 \\ {[1]} \end{gathered}$ | accept $x=7, y=0$ | condone 7, 0 |
| 10 | (ii) | $\sqrt{13}$ <br> $(x-4)^{2}+(y-2)^{2}=13$ or ft their evaluated $r^{2}$, isw | 2 <br> 2 <br> [4] | M1 for Pythagoras used correctly eg $\left[r^{2}=\right] 3^{2}+2^{2}$ or for subst A or their B in $(x-4)^{2}+(y-2)^{2}\left[=r^{2}\right]$ <br> or B1 for $[r=] \pm \sqrt{13}$ <br> M1 for one side correct, as part of an equation with $x$ and $y$ terms | annotate this question if partially correct <br> allow recovery if some confusion between squares and roots but correct answer found <br> do not accept $(\sqrt{13})^{2}$ instead of 13 ; allow M1 for LHS for $(x-4)^{2}+(y-2)^{2}=r^{2}$ (or worse, $\left.(x-4)^{2}+(y-2)^{2}=r\right)$ (may be seen in attempt to find radius) |
| 10 | (iii) | $(7,4)$ | 2 <br> [2] | B1 each coord accept $x=7, y=4$ <br> if B0, then M1 for a vector or coordinates approach such as ' 3 along and 2 up' to get from A to C oe <br> or M1 for $\frac{x_{D}+1}{2}=4$ and $\frac{y_{D}+0}{2}=2$ | condone 7, 4 <br> or M1 for longer method, finding the equation of the line CD as $y=2 / 3(x-1)$ oe and then attempting to find intn with their circle |


| Question |  | grad tgt $=-3 / 2$ oe | Marks M2 | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | (iv) | $\operatorname{grad} \operatorname{tgt}=-3 / 2$ oe | M2 | correctly obtained or ft their D if used <br> M1 for $\operatorname{grad} \mathrm{AD}=\frac{4-0}{7-1}$ oe isw or $2 / 3$ oe seen or used in this part or for their grad tgt $=-1 /$ their grad AD | annotate this question if partially correct may use $\mathrm{AD}, \mathrm{CD}$ or AC <br> NB grad AD etc may have been found in part (iii); allow marks if used in this part - mark the copy of part (iii) that appears below the image for part (iv) |
|  |  | $y-\text { their } 4=\text { their }(-3 / 2)(x-\text { their } 7)$ | M1 | or subst $(7,4)$ into $y=$ their $(-3 / 2) x+b$ <br> M0 if grad AD oe used or if a wrong gradient appears with no previous working |  |
|  |  | $y=-1.5 x+14.5$ oe isw | A1 |  | condone $y=\frac{-3 x+29}{2}$ |
|  |  |  | [4] |  | condone $y=-1.5 x+b$ and $b=14.5$ oe |


| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | (i) | $\begin{aligned} & x=4 \\ & (4,-3) \end{aligned}$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & {[2]} \end{aligned}$ | or $x=4, y=-3$ | condone 4, -3 |
| 11 | (ii) | $(0,13)$ isw <br> $[$ when $y=0,](x-4)^{2}=3$ <br> $[x=] 4 \pm \sqrt{3}$ or $\frac{8 \pm \sqrt{12}}{2}$ isw | 1 <br> M1 <br> A2 <br> [4] | or [when $x=0$ ], $y=13$ isw 0 for just $(13,0)$ or $(k, 13)$ where $k \neq 0$ or $x^{2}-8 x+13[=0]$ need not go on to give coordinate form <br> A1 for one root correct | annotate this question if partially correct <br> may be implied by correct value(s) for $x$ found <br> allow M1 for $y=x^{2}-8 x+13$ only if they go on to find values for $x$ as if $y$ were 0 |
| 11 | (iii) | replacement of $x$ in their eqn by $(x-2)$ <br> completion to given answer $y=x^{2}-12 x+33$, showing at least one correct interim step | M1 <br> A1 <br> [2] | $\begin{aligned} & \text { may be simplified; eg }[y=](x-6)^{2}-3 \\ & \text { or allow M1 for }(x-6-\sqrt{3})(x-6+\sqrt{3}) \\ & {[=0 \text { or } y]} \\ & \text { cao; condone using } \mathrm{f}(x-2) \text { in place of } y \end{aligned}$ | condone omission of ' $y=$ ' for M1, but must be present in final line for A1 |


| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | (iv) | $\begin{aligned} & x^{2}-12 x+33=8-2 x \text { or } \\ & (x-6)^{2}-3=8-2 x \end{aligned}$ | M1 | for equating curve and line; correct eqns only; <br> or for attempt to subst $(8-y) / 2$ for $x$ in $y=x^{2}-12 x+33$ | annotate this question if partially correct |
|  |  | $x^{2}-10 x+25=0$ | M1 | for rearrangement to zero, condoning one error such as omission of ' $=0$, |  |
|  |  | $(x-5)^{2}[=0]$ | A1 | or showing $b^{2}=4 a c$ | allow $\frac{10 \pm \sqrt{0}}{2}$ oe if $b^{2}-4 a c=0$ is not used explicitly <br> A0 for $(x-5)^{2}=y$ |
|  |  | $x=5$ www [so just one point of contact] | A1 | may be part of coordinates $(5, k)$ | allow recovery from $(x-5)^{2}=y$ |
|  |  | point of contact at $(5,-2)$ | A1 | dependent on previous A1 earned; allow for $y=-2$ found |  |
|  |  | alt. method | or |  | examiners: use one mark scheme or the other, to the benefit of the candidate if both methods attempted, but do not use a mixture of the schemes |
|  |  | for curve, $y^{\prime}=2 x-12$ | M1 |  |  |
|  |  | $2 x-12=-2$ | M1 | for equating their $y^{\prime}$ to -2 |  |
|  |  | $x=5$, and $y$ shown to be -2 using eqn to curve | A1 |  |  |
|  |  | $\operatorname{tgt}$ is $y+2=-2(x-5)$ | A1 |  |  |
|  |  | deriving $y=8-2 x$ | A1 |  | condone no further interim step if all working in this part is correct so far |
|  |  |  | [5] |  |  |


| Question |  | Answer$\begin{gathered} y=(x+5)(x+2)(2 x-3) \text { or } \\ y=2(x+5)(x+2)(x-3 / 2) \end{gathered}$ | $\frac{\text { Marks }}{2}$[2] | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (i) |  |  | M1 for $y=(x+5)(x+2)(x-3 / 2)$ or $(x+5)(x+2)(2 x-3)$ with no equation or $(x+5)(x+2)(2 x-3)=0$ <br> but M0 for $y=(x+5)(x+2)(2 x-3)-30$ or $(x+5)(x+2)(2 x-3)=30$ etc | allow ' $\mathrm{f}(x)=$ ' instead of ' $y=$ ' <br> ignore further work towards (ii) <br> but do not award marks for (i) in (ii) |
| 12 | (ii) | correct expansion of a pair of their linear twoterm factors ft isw <br> correct expansion of the correct linear and quadratic factors and completion to given answer $y=2 x^{3}+11 x^{2}-x-30$ | M1 <br> M1 <br> [2] | ft their factors from (i); need not be simplified; may be seen in a grid must be working for this step before given answer <br> or for direct expansion of all three factors, allow M2 for $2 x^{3}+10 x^{2}+4 x^{2}-3 x^{2}+20 x-15 x-6 x-30$ <br> oe (M1 if one error) <br> or M1M0 for a correct direct expansion of $(x+5)(x+2)(x-3 / 2)$ <br> condone lack of brackets if used as if they were there | allow only first M1 for expansion if their (i) has an extra - 30 etc do not award $2^{\text {nd }}$ mark if only had ( $x-3 / 2$ ) in (i) and suddenly doubles RHS at this stage <br> condone omission of ' $y=$ ' or inclusion of ' $=0$ ' for this second mark (some cands have already lost a mark for that in (i)) <br> allow marks if this work has been done in part (i) - mark the copy of part (i) that appears below the image for part (ii) |


| Question |  | Answer <br> ruled line drawn through $(-2,0)$ and $(0,10)$ and long enough to intersect curve at least twice $-5.3 \text { to }-5.4 \text { and } 1.8 \text { to } 1.9$ | Marks <br> B1 <br> B2 <br> [3] | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12 | (iii) |  |  | tolerance half a small square on grid at $(-2,0)$ and $(0,10)$ <br> B1 for one correct ignore the solution -2 but allow B1 for both values correct but one extra or for wrong 'coordinate' form such as $(1.8,-5.3)$ | insert BP on spare copy of graph if not used, to indicate seen - this is included as part of image, so scroll down to see it accept in coordinate form ignoring any $y$ coordinates given; |
| 12 | (iv) | $\begin{aligned} & 2 x^{3}+11 x^{2}-x-30=5 x+10 \\ & 2 x^{3}+11 x^{2}-6 x-40[=0] \end{aligned}$ <br> division by $(x+2)$ and correctly obtaining $2 x^{2}$ $+7 x-20$ <br> substitution into quadratic formula or for completing the square used as far as $\begin{aligned} & x+\frac{7}{4}^{2}=\frac{209}{16} \text { oe } \\ & {[x=] \frac{-7 \pm \sqrt{209}}{4} \text { oe isw }} \end{aligned}$ | M1 <br> M1 <br> M1 <br> M1 <br> A1 [5] | for equating curve and line; correct eqns only <br> for rearrangement to zero, condoning one error <br> or showing that $(x+2)\left(2 x^{2}+7 x-20\right)=2 x^{3}$ $+11 x^{2}-6 x-40$, with supporting working condone one error eg $a$ used as 1 not 2 , or one error in the formula, using given $2 x^{2}+7 x-20=0$ <br> dependent only on $4^{\text {th }}$ M1 | annotate this question if partially correct |

