

Mark Scheme (Results)

Summer 2014

Pearson Edexcel GCE in Core Mathematics 2 (6664\_01)

#### **Edexcel and BTEC Qualifications**

Edexcel and BTEC qualifications come from Pearson, the world's leading learning company. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information, please visit our website at <a href="https://www.edexcel.com">www.edexcel.com</a>.

Our website subject pages hold useful resources, support material and live feeds from our subject advisors giving you access to a portal of information. If you have any subject specific questions about this specification that require the help of a subject specialist, you may find our Ask The Expert email service helpful.

www.edexcel.com/contactus

# Pearson: helping people progress, everywhere

Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: <a href="https://www.pearson.com/uk">www.pearson.com/uk</a>

Summer 2014
Publications Code UA038455
All the material in this publication is copyright
© Pearson Education Ltd 2014

### **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL GCE MATHEMATICS

# **General Instructions for Marking**

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

#### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# **General Principles for Core Mathematics Marking**

(But note that specific mark schemes may sometimes override these general principles).

# Method mark for solving 3 term quadratic:

### 1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q)$$
, where  $|pq| = |c|$ , leading to  $x = ...$ 

$$(ax^2 + bx + c) = (mx + p)(nx + q)$$
, where  $|pq| = |c|$  and  $|mn| = |a|$ , leading to  $x = ...$ 

### 2. Formula

Attempt to use the correct formula (with values for a, b and c).

# 3. Completing the square

Solving 
$$x^2 + bx + c = 0$$
:  $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0$ ,  $q \neq 0$ , leading to  $x = \dots$ 

### Method marks for differentiation and integration:

### 1. Differentiation

Power of at least one term decreased by 1.  $(x^n \rightarrow x^{n-1})$ 

### 2. Integration

Power of at least one term increased by 1.  $(x^n \rightarrow x^{n+1})$ 

# Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

### **Exact answers**

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

| Question<br>Number | Scheme   |                  |                      |                    |                | Marks  |                       |
|--------------------|--|------------------|----------------------|--------------------|----------------|--|-----------------------|
|                    | <u> </u>   | 1                | 1.25                 | 1.5                | 1.75           | 2  |                       |
| 1()                | у  | 1.414            | 1.601                | 1.803              | 2.016          | 2.236  |                       |
| 1.(a)              | At $x = 1.25$ , $y = 1.601$ (only) $\begin{cases} 1.601 & \text{(May not be in the table and can score if seen as part of their working in (b))} \end{cases}$  |                  |                      |                    |                | B1 cao   |                       |
|                    | $\frac{1}{2} \times 0$   | .25;×{1.4        | 14 + 2.236 + 2       | (their 1.60        | 01+1.803+2.    | 016)}  | [1]<br>B1;<br>M1 A1ft |
|                    | B1; for using $\frac{1}{2} \times 0.25$ or equivalent.   | or $\frac{1}{8}$ | <u>M1: Stru</u><br>{ | <u>icture of</u> } | as show        | r the correct expression<br>n following through<br>te's y value found in |                       |
| <b>(b)</b>         | M1 requires the correct structure for the y values. It needs to contain first y value plus last y value and the second bracket to be multiplied by 2 and to be the summation of the remaining y values in the table with no additional values. If the only mistake is a copying error or is to omit one value from $2()$ bracket this may be regarded as a slip and the M mark can be allowed (nb: an extra repeated term, however, forfeits the M mark). M0 if any values used are x values instead of y values.  A1ft: for the correct underlined expression as shown following through candidate's y value found in part (a).  Bracketing mistakes: e.g. $\left(\frac{1}{2} \times \frac{1}{4}\right) (1.414 + 2.236) + 2 \left(\text{their } 1.601 + 1.803 + 2.016\right) (=11.29625)$ |                  |                      |                    |                |  |                       |
|                    | $\left(\frac{1}{2} \times \frac{1}{4}\right) 1.414 + 2.236 + 2 \text{ (their } 1.601 + 1.803 + 2.016) \text{ (= } 13.25275\text{)}$<br>Both score B1 M1 A0 unless the final answer implies that the calculation has been done correctly (then full marks could be given).  |                  |                      |                    |                |  |                       |
|                    | Alternative: Separate trapezia may be used, and this can be marked equivalently. $\left[\frac{1}{8}(1.414+1.601)+\frac{1}{8}(1.601+1.803)+\frac{1}{8}(1.803+2.016)+\frac{1}{8}(2.016+2.236)\right]$ B1 for $\frac{1}{8}$ (aef), M1 for correct structure, 1st A1ft for correct expression, ft their 1.601  |                  |                      |                    |                |  |                       |
|                    | $\left\{ = \frac{1}{8}(14.49) \right\} = 1.8112$   | 25               |                      | 1.81 or a          | awrt 1.81      |  | A1                    |
|                    | ·  |                  | t answer <u>only</u> |                    |                |  |                       |
|                    | If required accuracy   | is not se        | en in (a), full i    | marks can          | still be score | d in (b) (e.g. uses 1.6)   | F 43                  |
|                    |  |                  |                      |                    |                |  | [4]<br>Total 5        |
| <u> </u>           |  |                  |                      |                    |                |  | I Otal 3              |

| Question<br>Number | Scheme   |  |                |  |
|--------------------|--|--|----------------|--|
|                    |  | ark (a) and (b) in that order  |                |  |
|                    | $f(x) = 2x^3 - 7x^2 + 4x + 4$  |  |                |  |
|                    | $f(2) = 2(2)^3 - 7(2)^2 + 4(2) + 4$  | Attempts f(2) or f(-2)   | M1             |  |
| <b>2.</b> (a)      | = 0, and so $(x - 2)$ is a factor.  Note: Long division scores no marks in   | $f(2) = 0$ with no sign or substitution errors $(2(2)^3 - 7(2)^2 + 4(2) + 4 = 0)$ is sufficient) <b>and for conclusion.</b> Stating "hence factor" or "it is a factor" or a "tick" or "QED" or "no remainder" or "as required" are fine for the conclusion <b>but not = 0 just underlined and not hence (2 or f(2)) is a factor.</b> Note also that a conclusion can be implied from a <u>preamble</u> , eg: "If $f(2) = 0$ , $(x - 2)$ is a factor" | A1             |  |
|                    |  |  | [2]            |  |
|                    | $f(x) = \{(x-2)\}(2x^2 - 3x - 2)$  | M1: Attempts long division by $(x-2)$ or other method using $(x-2)$ , to obtain $(2x^2 \pm ax \pm b)$ , $a \ne 0$ , even with a remainder. Working need not be seen as this could be done "by inspection."  A1: $(2x^2 - 3x - 2)$  | M1 A1          |  |
| (b)                | $= (x-2)(x-2)(2x+1) \operatorname{or} (x-2)^{2} (2x+1)$ or equivalent e.g. $= 2(x-2)(x-2)(x+\frac{1}{2}) \operatorname{or} 2(x-2)^{2} (x+\frac{1}{2})$ | dM1: Factorises a 3 term quadratic. (see rule for factorising a quadratic in the General Principles for Core Maths Marking). This is dependent on the previous method mark being awarded but there must have been no remainder. Allow an attempt to solve the quadratic to determine the factors.  A1: cao – needs all three factors on one line. Ignore following work (such as a solution to a quadratic equation.)                                | <b>d</b> M1 A1 |  |
|                    | Note = $(x-2)(\frac{1}{2}x-1)(4x+2)$ would lose the last mark as it is not <b>fully</b> factorised   |  |                |  |
|                    |  | y award full marks in (b)  |                |  |
|                    |  | \27  | [4]            |  |
|                    |  |  | Total 6        |  |

| Question<br>Number | Schem  | e  | Marks     |  |  |
|--------------------|--|--|-----------|--|--|
| <b>3.</b> (a)      | $(2-3x)^6 = 64 + \dots$  | 64 seen as the only constant term in their expansion.  | B1        |  |  |
|                    | $\left\{ (2-3x)^6 \right\} = (2)^6 + \frac{^6C_1}{}(2)^5(-3\underline{x}) + \frac{^6C_2}{}(2)^4(-3\underline{x})^2 + \dots$  |  |           |  |  |
|                    | M1: $\binom{6}{1} \times \times x$ or $\binom{6}{1} \times \times x^2$ . For <u>either</u> the x term <u>or</u> the $x^2$ term. Requires <u>correct</u>  |  |           |  |  |
|                    | binomial coefficient in any form with the cor  |  |           |  |  |
|                    | coefficient (perhaps including powers of 2 and/or $-3$ ) may be wrong or missing. The terms  |  |           |  |  |
|                    | can be "listed" rather than adde ${}^{6}C_{1}2^{5} - 3x + {}^{6}C_{2}2^{4} - 3x^{2} + \dots$ Scores M0 u   |  |           |  |  |
|                    | $C_1 Z = -3x + C_2 Z = -3x + \dots$ Scores Mu t  |  |           |  |  |
|                    |  | A1: Either $-576x$ or $2160x^2$  |           |  |  |
|                    | $= 64 - 576x + 2160x^2 + \dots$  | (Allow + $-576x$ here)<br>A1: Both $-576x$ and $2160x^2$                                     | A1A1      |  |  |
|                    |  | A1: Both $-5/6x$ and $2160x$<br>(Do not allow $+ -576x$ here)                                |           |  |  |
|                    |  | (Do not allow $+ - 370x$ here)   | [4]       |  |  |
| (a) Way 2          | (2 2 ) 6   | 64 seen as the only constant term in their   |           |  |  |
| (3)                | $(2-3x)^6 = 64 + \dots$  | expansion.   | B1        |  |  |
|                    |  | M1: $({}^{6}C_{1} \times \times x) \operatorname{or}({}^{6}C_{2} \times \times x^{2})$ . For |           |  |  |
|                    | $\left[ \left( 1 - \frac{3}{2}x \right)^6 = 1 + \frac{{}^6C_1}{2} \left( \frac{-3}{2}\underline{x} \right) + \frac{{}^6C_2}{2} \left( \frac{-3}{2}\underline{x} \right)^2 + \right]$   | either the x term or the $x^2$ term. Requires  |           |  |  |
|                    |  | $\frac{\text{correct}}{\text{with the correct power of } x}$ , but the other                 | 3.54      |  |  |
|                    |  | part of the coefficient (perhaps including   | <u>M1</u> |  |  |
|                    |  | powers of 2 and/or $-3$ ) may be wrong or  |           |  |  |
|                    |  | missing. The terms can be "listed" rather  |           |  |  |
|                    |  | than added. Ignore any extra terms.  A1: Either $-576x$ or $2160x^2$                         |           |  |  |
|                    |  | (Allow + $-576x$ here)   |           |  |  |
|                    | $= 64 - 576x + 2160x^2 + \dots$  | A1: Both $-576x$ and $2160x^2$   | A1A1      |  |  |
|                    |  | (Do not allow $+ -576x$ here)  |           |  |  |
| (b)                | ( ")   |  |           |  |  |
| (0)                | Candidate writes down $\left(1+\frac{x}{2}\right)\times\left(\text{their part}\right)$   | (a) answer, at least up to the term in $x$ ).  |           |  |  |
|                    | (Condone missir  |  |           |  |  |
|                    | $\left(1 + \frac{x}{2}\right) \left(64 - 576x +\right) \text{ or } \left(1 + \frac{x}{2}\right)$   | $\int (64 - 576x + 2160x^2 +) \text{ or }$   | M1        |  |  |
|                    | $\left(1 + \frac{x}{2}\right) 64 - \left(1 + \frac{x}{2}\right) 576x \text{ or } \left(1 + \frac{x}{2}\right) 6$   | $4 - \left(1 + \frac{x}{2}\right) 576x + \left(1 + \frac{x}{2}\right) 2160x^2$               |           |  |  |
|                    | or $64 + 32x, -576x - 288x^2$ , 2  | $2160x^2 + 1080x^3$ are fine.  |           |  |  |
|                    |  | A1: At least 2 terms correct as shown. (Allow $+ -544x$ here)                                |           |  |  |
|                    | $= 64 - 544x + 1872x^2 + \dots$  | A1: $64 - 544x + 1872x^2$  | A1A1      |  |  |
|                    |  | The terms can be "listed" rather than added. Ignore any extra terms.                         |           |  |  |
|                    |  |  | [3]       |  |  |
|                    | CC. If a condidate commend in Jersey 1   | your of a only the Massaches are 2.22  | Total 7   |  |  |
|                    | SC: If a candidate expands in descending powers $\{(2-3x)^6\} = (-3x)^6 + {}^6C_1(2-3x)^6 = (-3x)^6 + {}^6C_1(2-3x)$ |  |           |  |  |
|                    | $\{(2-5x)^{-1}\} = (-5x)^{-1} + \frac{{}^{-1}C_1}{2}$  | ) (-3x) + C <sub>2</sub> (2) (-3x) +   |           |  |  |

| Question<br>Number | Scheme   |   |             |  |
|--------------------|--|---|-------------|--|
| 4.                 |  | M1: $x^n \to x^{n+1}$ A1: At least one of either $\frac{x^4}{6(4)}$ or $\frac{x^{-1}}{(3)(-1)}$ .   |             |  |
|                    | $\left\{ \int \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \frac{x^4}{6(4)} + \frac{x^{-1}}{(3)(-1)}$   | A1: $\frac{x^4}{6(4)} + \frac{x^{-1}}{(3)(-1)}$ or equivalent.  | M1A1A1      |  |
|                    |  | e.g. $\frac{x^4}{6} + \frac{x^{-1}}{3}$ (they will lose the final mark if they cannot deal with this correctly)   |             |  |
|                    | Note that some candidates may change   |   |             |  |
|                    | $\int \frac{x^3}{6} + \frac{1}{3x^2} dx = \int 3x^5 + 6dx $ in which case all  | low the M1 if $x^n \to x^{n+1}$ for their changed   |             |  |
|                    | function and allow the   | M1 for limits if scored   |             |  |
|                    | $\left\{ \int_{1}^{\sqrt{3}} \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \left( \frac{\left(\sqrt{3}\right)}{24} \right)$  | $- + \frac{\left(\sqrt{3}\right)^{-1}}{-1(3)} - \left(\frac{\left(1\right)^{4}}{24} + \frac{\left(1\right)^{-1}}{-1(3)}\right)$   | <b>d</b> M1 |  |
|                    | $2^{nd}$ dM1: For using limits of $\sqrt{3}$ and 1 on an integration way round. The $2^{nd}$ M1 is dependent   | tegrated expression and subtracting the correct ent on the 1 <sup>st</sup> M1 being awarded.  |             |  |
|                    | $=\left(\frac{9}{9}-\frac{1}{1}\right)-\left(\frac{1}{1}-\frac{1}{1}\right)=\frac{2}{9}-\frac{1}{1}\sqrt{3}$   | $\frac{2}{3} - \frac{1}{9}\sqrt{3}$ or $a = \frac{2}{3}$ and $b = -\frac{1}{9}$ .<br>Allow equivalent fractions for $a$ and/or $b$ and 0.6 recurring and/or 0.1 recurring but do <b>not</b> | Alcso       |  |
|                    |  | allow $\frac{6-\sqrt{3}}{9}$  | TTESO       |  |
|                    | This final mark is cao and cso – there   | e must have been no previous errors   | TD 4 1 5    |  |
|                    | Common Errors (U   | Tenally 3 out of 5)   | Total 5     |  |
|                    | $\left\{ \int \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \int \left( \frac{x^3}{6} + 3x \right) dx$   | $a^{-2} dx = \frac{x^4}{6(4)} + \frac{3x^{-1}}{(-1)} M1A1A0$  |             |  |
|                    | $\left\{ \int_{1}^{\sqrt{3}} \left( \frac{x^{3}}{6} + \frac{1}{3x^{2}} \right) dx \right\} = \left( \frac{\left(\sqrt{3}\right)^{4}}{24} + \frac{1}{3x^{2}} \right) dx $   | $\frac{3\left(\sqrt{3}\right)^{-1}}{-1} - \left(\frac{\left(1\right)^4}{24} + \frac{3\left(1\right)^{-1}}{-1}\right) dM1$   |             |  |
|                    | $= \left(\frac{9}{24} - \frac{3}{\sqrt{3}}\right) - \left(\frac{1}{24} + \frac{3}{-1}\right) = \frac{10}{3} - \sqrt{3} \text{A0}$  |   |             |  |
|                    | $\left\{ \int \left(\frac{x^3}{6} + \frac{1}{3x^2}\right) dx \right\} = \int \left(\frac{x^3}{6} + \left(3x\right)^2\right) dx$  | $\int_{0}^{2} dx = \frac{x^4}{6(4)} + \frac{(3x)^{-1}}{(-1)} M1A1A0$  |             |  |
|                    | $\left\{ \int_{1}^{\sqrt{3}} \left( \frac{x^{3}}{6} + \frac{1}{3x^{2}} \right) dx \right\} = \left( \frac{\left(\sqrt{3}\right)^{4}}{24} + \frac{\left(3\sqrt{3}\right)^{-1}}{-1} \right) - \left( \frac{\left(1\right)^{4}}{24} + \frac{\left(3\times1\right)^{-1}}{-1} \right) dM 1$ |   |             |  |
|                    | $=\left(\frac{9}{24}-\frac{1}{3\sqrt{3}}\right)-\left(\frac{1}{24}\right)$   | $\left(\frac{1}{4} - \frac{1}{3}\right) = \frac{2}{3} - \frac{\sqrt{3}}{9} A0$  |             |  |
|                    | Note this is the correct answer  | r but follows incorrect work.   |             |  |

| Question<br>Number |   | Scheme   | Marks       |  |
|--------------------|---|--|-------------|--|
| 5.(a)              | Area $BDE = \frac{1}{2}(5)^2(1.4)$  | M1: Use of the correct formula or method for the area of the sector  | M1A1        |  |
|                    | $=17.5 \text{ (cm}^2)$  | A1: 17.5 oe  |             |  |
| <b>a</b> >         |   |  | [2]         |  |
| <b>(b)</b>         |   | can be marked together   |             |  |
|                    | $6.1^2 = 5^2 + 7.5^2 - (2 \times 5 \times 7.5 \cos DBC)  \text{o}$  | r $\cos DBC = \frac{5^2 + 7.5^2 - 6.1^2}{2 \times 5 \times 7.5}$ (or equivalent)   | M1          |  |
|                    |   | nent involving the angle DBC   |             |  |
|                    | Angle $DBC = 0.943201$  | awrt 0.943   | A1          |  |
|                    | Note that work for (b) may l  | be seen on the diagram or in part (c)  | [2]         |  |
| (c)                | Note that candidates may work in de   | egrees in (c) (Angle $DBC = 54.04$ deg rees )  | [2]         |  |
|                    | Area <i>CBD</i> =   | $=\frac{1}{2}5(7.5)\sin(0.943)$  |             |  |
|                    |   | Area $CBD = \frac{1}{2}5(7.5)\sin(\text{their } 0.943)$ or awrt  |             |  |
|                    | Angle $EBA = \pi - 1.4 - "0.943"$   | 15.2. (Note area of $CBD = 15.177$ )   | M1          |  |
|                    | (Maybe seen on the diagram)  A correct method for the area of triangle <i>CBD</i> which can be implied by awrt 15.2 |  | 1,11        |  |
|                    | $\pi-1.4$   | - "their 0.943"  |             |  |
|                    | A value for angle <i>EBA</i> of awrt 0.8 (from 0.7985926536 or 0.7983916536) or value for angle                     |  |             |  |
|                    | EBA of $(1.74159 \text{their angle } DBC)$ would imply this mark.   |  |             |  |
|                    | $AB = 5\cos(\pi - 1.4 - "0.943")$   |  |             |  |
|                    | or $AE = 5\sin(\pi - 1.4 - 0.943)$  |  |             |  |
|                    | <u>This is depende</u>  | $AB = 5\cos(\pi - 1.4 - \text{their } 0.943)$ $AB = 5\cos(0.79859) = 3.488577938$ $Allow M1 \text{ for } AB = \text{awrt } 3.49$ $Or$ $AE = 5\sin(\pi - 1.4 - \text{their } 0.943)$ $AE = 5\sin(0.79859) = 3.581874365688$ $Allow M1 \text{ for } AE = \text{awrt } 3.58$ $It \text{ must be clear that } \pi - 1.4 - "0.943" \text{ is being used for angle EBA.}$ $Note \text{ that some candidates use the sin rule here but it must be used correctly - do not allow mixing of degrees and radians.}$ $-"0.943") \times 5\sin(\pi - 1.4 - "0.943")$ ent on the previous M1 | M1          |  |
|                    |   | ors in finding the area of triangle EAB  | <b>d</b> M1 |  |
|                    |   | r area $EAB = \text{awrt } 6.2$  |             |  |
|                    | Area $ABCDE = 15.1$   | 7+ 17.5 + 6.24 = 38.92   |             |  |
|                    |   | awrt 38.9  | A1cso       |  |
|                    | Note that a sign amon in (b) can sive the -1  | otives angle (2.100 ) and sould lead to the  | [5]         |  |
|                    | answer in (c) – this would lose the final ma  | btuse angle (2.198) and could lead to the correct  | Tota        |  |

| Question<br>Number | Sc   | cheme  | Marks       |  |  |
|--------------------|--|--|-------------|--|--|
| 6(a)               | 20 . 160   | M1: Use of a correct $S_{\infty}$ formula  |             |  |  |
|                    | $S_{\infty} = \frac{20}{1 - \frac{7}{8}} \; ; = 160$   | A1: 160  | M1A1        |  |  |
|                    | Accept correct answer only (160)   |  |             |  |  |
|                    |  |  | [2]         |  |  |
| <b>(b)</b>         | 20(1 (7)12)  | M1: Use of a correct $S_n$ formula with $n = 12$   |             |  |  |
|                    | $S_{12} = \frac{20(1-(\frac{7}{8})^{12})}{1-\frac{7}{8}}$ ; = 127.77324  | (condone missing brackets around 7/8)  | M1A1        |  |  |
|                    | $1-\frac{7}{8}$  | A1: awrt 127.8   |             |  |  |
|                    | T & I in (b) requires all 12 terms to be calc  | ulated correctly for M1 and A1 for awrt 127.8  |             |  |  |
|                    |  |  | [2]         |  |  |
| (c)                |  | Applies $S_N$ ( <b>GP only</b> ) with $a = 20$ , $r = \frac{7}{8}$ and                               |             |  |  |
|                    | $160 - \frac{20(1 - (\frac{7}{8})^{N})}{1 - \frac{7}{2}} < 0.5$  | "uses" $0.5$ and their $S_{\infty}$ at any point in their  | M1          |  |  |
|                    | $1 - \frac{7}{8}$  | working. (condone missing brackets around  |             |  |  |
|                    |  | $7/8$ )(Allow =, <, >, $\geq$ , $\leq$ ) but see note below.   |             |  |  |
|                    | $(7)^{N}$ $(0.5)$  | Attempt to isolate $+160\left(\frac{7}{8}\right)^N$ or $+\left(\frac{7}{8}\right)^N$ oe              |             |  |  |
|                    | $160\left(\frac{7}{8}\right)^{N} < (0.5) \text{ or } \left(\frac{7}{8}\right)^{N} < \left(\frac{0.5}{160}\right)$                | (Allow =, $<$ , $>$ , $\ge$ , $\le$ ) but see note below.  | <b>d</b> M1 |  |  |
|                    | (-)  | Dependent on the previous M1   |             |  |  |
|                    |  | Uses the power law of logarithms or takes logs   |             |  |  |
|                    |  | base 0.875 correctly to obtain an equation or an inequality of the form                              |             |  |  |
|                    | $N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{160}\right)$   |  |             |  |  |
|                    |  | $N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{\text{their S}_{-}}\right)$                    | 3.4.1       |  |  |
|                    |  | or   | M1          |  |  |
|                    |  | $N > \log_{0.875} \left( \frac{0.5}{\text{their S}} \right)$   |             |  |  |
|                    |  | $N > \log_{0.875} \left( \frac{1}{\text{their } S_{\infty}} \right)$                                 |             |  |  |
|                    |  | (Allow =, $<$ , $>$ , $\ge$ , $\le$ ) but see note below.  |             |  |  |
|                    | $N > \frac{\log(\frac{0.5}{160})}{\log(\frac{7}{9})} = 43.19823 \Rightarrow N = 44$  |  | A1 cso      |  |  |
|                    | $\log\left(\frac{7}{8}\right) = 43.17623 \Rightarrow 17 = 44$  | IV - ++ (MIOW IV =++ but not IV > ++   | AI CSU      |  |  |
|                    |  | e in a candidate's working loses the final mark.   |             |  |  |
|                    |  | tion of the inequality is reversed in the final line full marks for using =, as long as no incorrect |             |  |  |
|                    | working seen.  | run marks for using –, as long as no incorrect   |             |  |  |
|                    |  |  | [4]         |  |  |
|                    | m • 1 0 ×  | (M. 1  | Total 8     |  |  |
|                    |  | provement Method in (c):   |             |  |  |
|                    | $1^{\text{st}}$ M1: Attempts $160 - S_N$   | or $S_N$ with at least one value for $N > 40$  |             |  |  |
|                    | 2 <sup>nd</sup> M1: Attempts 160   | $0 - S_N$ or $S_N$ with $N = 43$ or $N = 44$   |             |  |  |
|                    | $3^{\text{rd}}$ M1: For evidence of examining $160 - S_N$ or $S_N$ for <b>both</b> $N = 43$ <b>and</b> $N = 44$ with <b>both</b> |  |             |  |  |
|                    | correct to 2 DP  |  |             |  |  |
|                    | Eg: $160 - S_{43} = \text{awrt } 0.51 \text{ and } 160 - S_{44} = \text{awrt } 0.45$   |  |             |  |  |
|                    | or $S_{43} = \text{awrt} 159.49 \text{ and } S_{44} = \text{awrt} 159.55$  |  |             |  |  |
|                    | A1: $N = 44 \cos \theta$   |  |             |  |  |
|                    | Answer of $N = 44$ onl   | y with no working scores no marks  |             |  |  |

| Question<br>Number | Scheme   |  |         |
|--------------------|--|--|---------|
| _                  | (i) $9\sin(\theta + 60^{\circ})$   | $=4; 0 \le \theta < 360^{\circ}$   |         |
| 7.                 |  | $x = 0; -\pi \le x < \pi$  |         |
| (i)                | $\sin(\theta + 60^{\circ}) = \frac{4}{9}$ , so $(\theta + 60^{\circ}) = 26.3877$   | Sight of $\sin^{-1}\left(\frac{4}{9}\right)$ or awrt 26.4° or 0.461°   | M1      |
|                    | $(\alpha = 26.3877)$   | Can also be implied for $\theta = \text{awrt} - 33.6$ (i.e. $26.4 - 60$ )  | IVII    |
|                    |  | $\theta + 60^{\circ}$ = either "180 – their $\alpha$ " or  |         |
|                    |  | " $360^{\circ}$ + their $\alpha$ " and not for $\theta$ = either   |         |
|                    | So, $\theta + 60^{\circ} = \{153.6122, 386.3877\}$   | " $180$ – their $\alpha$ " or " $360^{\circ}$ + their $\alpha$ ". This   | M1      |
|                    |  | can be implied by later working. The candidate's $\alpha$ could also be in radians but do not allow mixing of degrees and radians. |         |
|                    |  | A1: At least one of  |         |
|                    | and $\theta = \{93.6122, 326.3877\}$   | awrt 93.6° or awrt 326.4°  | A1 A1   |
|                    |  | A1: Both awrt 93.6° and awrt 326.4°  |         |
|                    |  | nust come from correct work  |         |
|                    | Ignore extra solutions outside the range. In an otherwise fully correct solution deduct the final A1for any extra solutions in range |  |         |
|                    | in an otherwise runy correct solution deduct the final 71101 any extra solutions in runge  |  |         |
| (ii)               | $2\left(\frac{\sin x}{\cos x}\right) - 3\sin x = 0$  | Applies $\tan x = \frac{\sin x}{\cos x}$   | M1      |
|                    | Note: Applies $\tan x = \frac{\sin x}{\cos x}$ can be implied by $2\tan x - 3\sin x = 0 \Rightarrow \tan x (2 - 3\cos x)$            |  |         |
|                    | $2\sin x - 3\sin x \cos x = 0$   |  |         |
|                    | $\sin x(2-3\cos x)=0$  |  |         |
|                    | $\cos x = \frac{2}{3}$   | $\cos x = \frac{2}{3}$   | A1      |
|                    |  | A1: One of either awrt $0.84$ or awrt $-0.84$  |         |
|                    | $x = \operatorname{awrt}\{0.84, -0.84\}$   | A1ft: You can apply ft for $x = \pm \alpha$ , where  | A1A1ft  |
|                    |  | $\alpha = \cos^{-1} k$ and $-1 \le k \le 1$  |         |
|                    |  | ny extra answers in range in an otherwise  |         |
|                    | correct solution   | withhold the A1ft.  Both $x = 0$ and $-\pi$ or awrt $-3.14$ from   |         |
|                    | $\left\{\sin x = 0 \Rightarrow\right\} x = 0 \text{ and } -\pi$  | $\sin x = 0$ In this part of the solution, ignore extra  | B1      |
|                    | Note solutions on (21)   | solutions in range.  |         |
|                    | `  | 415, -0.8410, 0, 0.8410 }  |         |
|                    | Ignore extra solutions outside the range For <b>all</b> answers in degrees in (ii) M1A1A0A1ftB0 is possible                          |  |         |
|                    | ì  |  |         |
|                    | Allow the use of $\theta$ in place of $x$ in (ii)  |  | [5]     |
|                    | 1  |  | Total 9 |

| Question<br>Number | Scheme  |   | Marks   |
|--------------------|---|---|---------|
| 8.                 | Graph of $y = 3^x$ and solving  | $3^{2x} - 9(3^x) + 18 = 0$  |         |
| (a)                |   | At least two of the three criteria correct. (See notes below.)  | B1      |
|                    |   | All three criteria correct. (See notes below.)  | B1      |
|                    | (0,1)<br>O x  | <b>Criteria number 1:</b> Correct shape of curve for $x \ge 0$ and at least touches the positive y-axis. <b>Criteria number 2:</b> Correct shape of curve for $x < 0$ . Must not touch the x-axis or have any turning points. <b>Criteria number 3:</b> $(0,1)$ stated or in a table or 1 marked on the y-axis. Allow $(1,0)$ rather than $(0,1)$ if marked in the "correct" place on the y-axis. | [2]     |
| (b)                | $(3^{x})^{2} - 9(3^{x}) + 18 = 0$ or $y = 3^{x} \Rightarrow y^{2} - 9y + 18 = 0$                          | Forms a quadratic of the correct form in $3^x$ or in "y" where "y" = $3^x$ or even in x where "x" = $3^x$   | M1      |
|                    | $\{(y-6)(y-3)=0 \text{ or } (3^x-6)(3^x-3)=0 \}$  |   |         |
|                    | $y = 6$ , $y = 3$ or $3^x = 6$ , $3^x = 3$  | <b>Both</b> $y = 6$ and $y = 3$ .   | A1      |
|                    | $\left\{3^{x} = 6 \Rightarrow\right\} x \log 3 = \log 6$ or $x = \frac{\log 6}{\log 3}$ or $x = \log_3 6$ | A valid method for solving $3^x = k$<br>where $k > 0$ , $k \ne 1$ , $k \ne 3$<br>$x \log 3 = \log k \text{ or } x = \frac{\log k}{\log 3} \text{ or } x = \log_3 k$   | dM1     |
|                    | x = 1.63092   | awrt 1.63   | A1cso   |
|                    | Provided the first M1A1 is scored, the second $x = 1$   | M1A1 can be implied by awrt 1.63 $x = 1$ stated as a solution from <i>any</i> working.  | B1      |
|                    |   |   | [5]     |
|                    |   |   | Total 7 |

| Question   | Scheme  |   | Marks   |  |
|------------|---|---|---------|--|
| Number     |   |   |         |  |
| 0 (-)      | Mark (a) and (b) together  Uses the addition form of Dythogores                   |   |         |  |
| 9. (a)     |   | Uses the addition form of Pythagoras  |         |  |
|            | ( 5)2   | on $6\sqrt{5}$ and 4. Condone missing   |         |  |
|            | $OQ^2 = (6\sqrt{5})^2 + 4^2 \text{ or } OQ = \sqrt{(6\sqrt{5})^2 + 4^2}  \{=14\}$ | brackets on $\left(6\sqrt{5}\right)^2$  | M1      |  |
|            |   | (Working or 14 may be seen on the diagram)  |         |  |
|            |   | $y_Q = \sqrt{(\text{their } OQ)^2 - 11^2}$  |         |  |
|            | $y_Q = \sqrt{14^2 - 11^2}$  | Must include $$ and is dependent on the first M1 and requires OQ > 11   | dM1     |  |
|            | $=\sqrt{75} \text{ or } 5\sqrt{3}$  | $\sqrt{75}$ or $5\sqrt{3}$  | A1cso   |  |
|            |   |   | [3]     |  |
| <b>(b)</b> |   | M1: $(x \pm 11)^2 + (y \pm \text{their } k)^2 = 4^2$  |         |  |
|            | $(x-11)^2 + (y-5\sqrt{3})^2 = 16$   | Equation must be of this form and must use $x$ and $y$ not other letters. $k$ could be their last answer to part (a). Allow their $k \neq 0$ or just the letter $k$ . | - M1A1  |  |
|            |   | A1: $(x-11)^2 + (y-5\sqrt{3})^2 = 16$<br>or $(x-11)^2 + (y-5\sqrt{3})^2 = 4^2$  |         |  |
|            |   | <b>NB</b> $5\sqrt{3}$ must come from correct  |         |  |
|            |   | work in (a) and allow awrt 8.66   |         |  |
|            | Allow in expanded form for the final A1   |   |         |  |
|            | e.g. $x^2 - 22x + 121 + y^2 - 10$   | $\sqrt{3}y + 75 = 16$   |         |  |
|            | · ·   | •   | [2]     |  |
|            |   |   | Total 5 |  |
|            | Watch out for:  |   |         |  |
|            | (a) $OQ = \sqrt{\left(6\sqrt{5}\right)^2 + 4^2} = \sqrt{46} \text{ M}1$           |   |         |  |
|            | $y_Q = \sqrt{46 - 11^2} \text{ M0 (OQ} < 11)$                                     |   |         |  |
|            | $y_Q = \sqrt{75} \text{ A0}$  |   |         |  |
|            | (b) $(x-11)^2 + (y-5)^2$  | $(\sqrt{3})^2 = 16 \mathrm{M1A0}$   |         |  |

| Question<br>Number | Scheme  |  |  | Marks   |
|--------------------|---|--|--|---------|
| 10. (a)            | $\frac{1}{2}(9x+6x)4x$ or $2x\times15x$ or $\left(\frac{1}{2}4x\times(9x-6x)+6x\times4x\right)$ or $6x^2+24x^2$ or $\left(9x\times4x-\frac{1}{2}4x\times(9x-6x)\right)$ or $36x^2-6x^2$ | trapezium.  Note that 3 incorrect w  If there is a area of the | t attempt at the area of a $0x^2$ on its own or $30x^2$ from ork e.g. $5x \times 6x$ is M0. clear intention to find the trapezium correctly allow the A1 can be withheld if there s. | M1A1cso |
|                    | $\Rightarrow 30x^2y = 9600 \Rightarrow y = \frac{9600}{30x^2} \Rightarrow y = \frac{320}{x^2} *$  |  | t proof with at least one e step and no errors seen. quired.   |         |
|                    |   |  |  | [2]     |
| (b)                | $(S =) \frac{1}{2} (9x + 6x) 4x + \frac{1}{2} (9x + 6x) 4x + 6xy + 9xy + 5xy + 4xy$   |  |  | M1A1    |
|                    | M1: An attempt to find the area of six faces of the prism. The 2 trapezia may be combined as  |  |  |         |
|                    | $(9x + 6x)4x$ or $60x^2$ and the 4 other faces may be combined as $24xy$ but all six faces must be  |  |  |         |
|                    | included. There must be attempt at the areas of two trapezia that are dimensionally correct.  A1: Correct expression in any form.   |  |  |         |
|                    | Allow just $(S =) 60x^2 + 24xy$ for M1A1<br>$y = \frac{320}{x^2} \Rightarrow (S =) 30x^2 + 30x^2 + 24x \left(\frac{320}{x^2}\right)$  |  |  | M1      |
|                    | Substitutes $y = \frac{320}{x^2}$ into their expression for S (may be done earlier). S should have at least   |  |  |         |
|                    | one $x^2$ term and one $xy$ term but there may be other terms which may be dimensionally incorrect.   |  |  |         |
|                    | So, $(S =) 60x^2 + \frac{7680}{x} *$  |  | Correct solution only. "S = " is <b>not</b> required here.   | A1* cso |
|                    |   |  |  | [4]     |

| 10(c) | $\frac{dS}{dx} = 120x - 7680x^{-2} \left\{ = 120x - \frac{7680}{x^2} \right\}$             | M1: Either $60x^2 \rightarrow 120x$ or $\frac{7680}{x} \rightarrow \frac{\pm \lambda}{x^2}$ A1: Correct differentiation (need not be  | M1                |
|-------|--|---|-------------------|
|       |  | simplified).  | A1 aef            |
|       | $120x - \frac{7680}{x^2} = 0$ $\Rightarrow x^3 = \frac{7680}{120}; = 64 \Rightarrow x = 4$ | M1: $S' = 0$ and "their $x^3 = \pm$ value" or "their $x^{-3} = \pm$ value" Setting their $\frac{dS}{dx} = 0$ and "candidate's ft <i>correct</i> power of $x = a$ value". <b>The power of <math>x</math> must be consistent with their differentiation</b> . If inequalities are used this mark cannot be gained until candidate states value of $x$ or $S$ from their $x$ without inequalities. $S' = 0$ can be implied by $120x = \frac{7680}{x^2}$ . Some may spot that $x = 4$ gives $S' = 0$ and provided they clearly show $S'(4) = 0$ allow this mark as long as $S'$ is correct. (If $S'$ is incorrect this method is allowed if their derivative is clearly zero for their value of $x$ ) Note that the value of $x$ is not explicitly required so the use of $x = \sqrt[3]{64}$ to give $S = 2880$ would | M1A1cso           |
|       | Note some candidates stop here and de  | imply this mark. o not go on to find S – maximum mark is 4/6  |                   |
|       |  | Substitute candidate's value of $x \neq 0$ into a   |                   |
|       | $\{x=4,\}$   | formula for S. <b>Dependent on both previous M</b>  | <b>dd</b> M1      |
|       | $S = 60(4)^2 + \frac{7680}{4} = 2880 \text{ (cm}^2\text{)}$                                | marks.  |                   |
|       | 3 - 00(4) + — - 2000 (CIII )   | 2880 cso (Must come from correct work)  | A1 cao<br>and cso |
|       |  |   | [6]               |

| 10(d) | M1: Attempt $S''(x^n \to x^{n-1})$ and considers  |          |
|-------|---|----------|
|       | sign.  This mark requires an attempt at the second derivative and some consideration of its sign.  There does not necessarily need to be any substitution. An attempt to solve $S'' = 0$ is M0  A1: $120 + \frac{15360}{x^3}$ and $> 0$ and conclusion.  Requires a correct second derivative of $120 + \frac{15360}{x^3}$ (need not be simplified) and a valid reason (e.g. $> 0$ ), and conclusion.  Only follow through a correct second derivative i.e. $x$ may be incorrect but must be positive and/or $S''$ may have been evaluated incorrectly. | M1A1ft   |
|       | A correct $S''$ followed by $S''("4") = "360"$ therefore minimum would score no marks in (d)  |          |
|       | A correct $S''$ followed by $S''("4") = "360"$ which is positive therefore minimum would score  |          |
|       | both marks  |          |
|       |   | [2]      |
|       | Note parts (c) and (d) can be marked together.  |          |
|       |   | Total 14 |