

**GCE**

**Mathematics**

Unit **4732**: Probability and Statistics 1

Advanced Subsidiary GCE

**Mark Scheme for June 2014**

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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## Annotations and abbreviations

Annotation in scoris	Meaning
<b>BP</b>	Blank Page – this annotation <b>must</b> be used on all blank pages within an answer booklet (structured or unstructured) and on each page of an additional object where there is no candidate response.
✓ and ✖	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

## Subject-specific Marking Instructions for GCE Mathematics (OCR) Statistics strand

- a Annotations should be used whenever appropriate during your marking.

**The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.** It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

### **M**

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

### **A**

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

### **B**

Mark for a correct result or statement independent of Method marks.

## E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.

Candidates are expected to give numerical answers to an appropriate degree of accuracy. 3 significant figures may often be the norm for this, but this always needs to be considered in the context of the problem in hand. For example, in quoting probabilities from Normal tables, we generally expect *some* evidence of interpolation and so quotation to 4 decimal places will often be appropriate. But even this does not always apply – quotations of the standard critical points for significance tests such as 1.96, 1.645, 2.576 (maybe even 2.58 – but not 2.57) will commonly suffice, especially if the calculated value of a test statistic is nowhere near any of these values. Sensible discretion *must* be exercised in such cases.

Discretion must also be exercised in the case of small variations in the degree of accuracy to which an answer is given. For example, if 3 significant figures are expected (either because of an explicit instruction or because the general context of a problem demands it) but only 2 are given, loss of an accuracy ("A") mark is likely to be appropriate; but if 4 significant figures are given, this

should not normally be penalised. Likewise, answers which are slightly deviant from what is expected in a very minor manner (for example a Normal probability given, after an attempt at interpolation, as 0.6418 whereas 0.6417 was expected) should not be penalised. However, answers which are *grossly* over- or under-specified should normally result in the loss of a mark. This includes cases such as, for example, insistence that the value of a test statistic is (say) 2.128888446667 merely because that is the value that happened to come off the candidate's calculator. Note that this applies to answers that are given as final stages of calculations; intermediate working should usually be carried out, and quoted, to a greater degree of accuracy to avoid the danger of premature approximation.

The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h Genuine misreading (of numbers or symbols, occasionally even of text) occurs. If this results in the object and/or difficulty of the question being considerably changed, it is likely that all the marks for that question, or section of the question, will be lost. However, misreads are often such that the object and/or difficulty remain substantially unaltered; these cases are considered below.

The simple rule is that *all* method ("M") marks [and of course all independent ("B") marks] remain accessible but at least some accuracy ("A") marks do not. It is difficult to legislate in an overall sense beyond this global statement because misreads, even when the object and/or difficulty remains unchanged, can vary greatly in their effects. For example, a misread of 1.02 as 10.2 (perhaps as a quoted value of a sample mean) may well be catastrophic; whereas a misread of 1.6748 as 1.6746 may have so slight an effect as to be almost unnoticeable in the candidate's work.

A misread should normally attract *some* penalty, though this would often be only 1 mark and should rarely if ever be more than 2. Commonly in sections of questions where there is a numerical answer either at the end of the section or to be obtained and commented on (eg the value of a test statistic), this answer will have an "A" mark that may actually be designated as "cao" [correct answer only]. This should be interpreted *strictly* – if the misread has led to failure to obtain this value, then this "A" mark must be withheld even if all method marks have been earned. It will also often be the case that such a mark is implicitly "cao" even if not explicitly designated as such.

On the other hand, we commonly allow "fresh starts" within a question or part of question. For example, a follow-through of the candidate's value of a test statistic is generally allowed (and often explicitly stated as such within the marking scheme), so that the candidate may exhibit knowledge of how to compare it with a critical value and draw conclusions. Such "fresh starts" are not affected by any earlier misreads.

A misread may be of a symbol rather than a number – for example, an algebraic symbol in a mathematical expression. Such misreads are more likely to bring about a considerable change in the object and/or difficulty of the question; but, if they do not, they should be treated as far as possible in the same way as numerical misreads, *mutatis mutandis*. This also applied to misreads of text, which are fairly rare but can cause major problems in fair marking.

The situation regarding any particular cases that arise while you are marking for which you feel you need detailed guidance should be discussed with your Team Leader.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

**S1 June 2014 Mark Scheme Final (without introduction)**

Note: “(3 sfs)” means “answer which rounds to ... to 3 sfs”. If correct ans seen to  $\geq$  3sfs, ISW for later rounding  
 Penalise over-rounding only once in paper.

Question		Answer	Marks	Guidance	
1	(i)	Median = 7.45 (m) IQR = 7.75 – 6.7	B1 M1	cao allow 7.775 – 6.6 or 77.5 – 67 or 77.75 – 66 or 7.8 – 6.5 even though this is an incorrect method or 78 – 65	These <u>pairs</u> of values only, and subtract, for M1 eg 7.45, 7.75 – 6.7 = 1.05 B1M1A1 7.45, 7.775 – 6.6 = 1.175 B1M1A1 7.45, 7.8 – 6.5 = 1.3 B1M1A0 7.45, 7.7 – 6.5 = 1.2 B1M0A0  7.45, 77.5 – 67 = 10.5 B1M1A0 74.5, 77.5 – 67 = 10.5 B0M1A1 74.5, 7.75 – 6.7 = 10.5 B0M1A1 74.5, 77.75 – 66 = 11.75 B0M1A1  7.45, 78 – 65 = 13 B1M1A0 74.5, 78 – 65 = 13 B0M1A0 74.5, 77 – 65 = 12 B0M0A0
		= 1.05 (m) allow 1.175 or 1.18 NOT 1.3	A1	allow 10.5 or 11.75 or 11.8 but <u>only</u> if med = 74.5	
			[3]		



Question		Answer	Marks	Guidance																																
1	(ii)	<table style="border-collapse: collapse; margin-left: 20px;"> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">4</td><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">5</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;"></td><td style="padding: 2px 5px;"></td><td style="padding: 2px 5px;"></td><td style="padding: 2px 5px;">5</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">3</td><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">0</td><td style="padding: 2px 5px;">6</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">8</td><td style="padding: 2px 5px;">7</td><td style="padding: 2px 5px;">7</td><td style="padding: 2px 5px;">6</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;">4</td><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">7</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;"></td><td style="padding: 2px 5px;">6</td><td style="padding: 2px 5px;">5</td><td style="padding: 2px 5px;">7</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;"></td><td style="padding: 2px 5px;"></td><td style="padding: 2px 5px;"></td><td style="padding: 2px 5px;">8</td></tr> <tr><td style="border-right: 1px solid black; padding: 2px 5px;"></td><td style="padding: 2px 5px;"></td><td style="padding: 2px 5px;">5</td><td style="padding: 2px 5px;">8</td></tr> </table> <p>Complete correct diag including order and key and alignment</p>	4	2	2	5				5	3	3	0	6	8	7	7	6	4	3	2	7		6	5	7				8			5	8	<p>B1*</p> <p>B1dep</p> <p>[2]</p>	<p>Allow a separate diag with leaves to left of stem.</p> <p>If only a separate diag is drawn, with leaves to <u>right</u> of stem: all correct including order, alignment and key: B1</p> <p>If <u>all</u> digits are in correct rows and orders, &amp; correct key, award this mark <u>unless</u> EITHER:</p> <p>1. eg a 2<sup>nd</sup> digit in one row is <u>clearly</u> aligned with a 3<sup>rd</sup> digit in another OR</p> <p>2. 1st, 3rd, 4th &amp; 5th rows are <u>very</u> different lengths, eg because of crossing out and replacement</p> <p>correct digits in correct leaves, ignore order, allow one omitted or extra or misplaced or incorrect digit</p> <p>key: eg 8 6 4 means 6.8 (B) and 6.4 (A) allow just 8   6 means 6.8 NOT 8   6 means 8.6</p> <p>Allow 8   6 means 68, if consistent with (i)</p>
4	2	2	5																																	
			5																																	
3	3	0	6																																	
8	7	7	6																																	
4	3	2	7																																	
	6	5	7																																	
			8																																	
		5	8																																	
1	(iii)	<p>One correct comment on size: B1. One correct comment on spread or shape: B1. The following are examples only. Ignore any working; mark the statements only. Allow "First set" or "Right" for A, "Second set" or "Left" for B.</p>																																		
		<p>A higher <u>overall</u></p> <p>A has more taller trees or fewer shorter</p> <p>A has higher median (mean, ave, medium)</p> <p>B more evenly spread or distributed</p> <p>B more spread out</p> <p>B has larger range or IQR or sd</p> <p>Ranges of both are similar</p> <p>A is nearer to normal</p> <p>A is negatively skewed</p> <p>A has a (unique) mode, or modal class or peak; (B doesn't)</p>	<p>B1</p> <p>B1</p> <p>[2]</p>	<p>B shorter <u>overall</u></p> <p>B has fewer taller trees or more shorter</p> <p>B has lower median (mean, ave, medium)</p> <p>A less evenly spread or distributed</p> <p>A less spread out</p> <p>A has smaller range or IQR or sd</p> <p>Allow A's heights are more consistent</p> <p>Not other comment about skew</p> <p>Ignore any other reference to mode or most common</p> <p>Ignore all else even if incorrect</p>	<p>NOT A higher than B</p> <p>NOT B has shorter trees than A</p> <p>Allow just quoting the two medians, even if wrong, so long as med of A is gter than med of B.</p> <p>Similarly if quote IQRs</p> <p>NOT any reference to outliers</p> <p>NOT any reference to sample size</p> <p>NOT any reference to indiv trees</p> <p>NOT two comments on size</p> <p>NOT two comments on spread</p> <p>eg highest on both is 8.5 B0</p>																															

Question			Answer	Marks	Guidance
2	(a)		$(0^2 \times 0.3) + 2^2 \times 0.4 + 4^2 \times 0.3$ $- 2^2$ or $-4$ $= 2.4$	M1 M1 A1 <b>[3]</b>	last two terms correct. NOT eg $\div 6$ or $\div 3$ allow $-(\text{any number})^2$ , dep +ve result $2^2 \times 0.3 + (0) + 2^2 \times 0.3$ M2 1st or 3rd term correct M1 $\div 3$ M0M0A0
2	(b)	(i)	$2k + 3k + 4k + 5k = 1$ oe  $(k = \frac{1}{14}$ <b>AG</b> )	B1  <b>[1]</b>	or $14k = 1$ oe " $= 1$ " is essential NOT just $2 + 3 + 4 + 5 = 14$ so $k = \frac{1}{14}$ Allow verification, eg stating that $\frac{2}{14} + \frac{3}{14} + \frac{4}{14} + \frac{5}{14} = 1$
2	(b)	(ii)	$\frac{2}{14}, \frac{3}{14}, \frac{4}{14}, \frac{5}{14}$ or $\frac{2}{14}, \frac{6}{14}, \frac{12}{14}, \frac{20}{14}$ $\Sigma xp$ $= \frac{20}{7}$ or $2\frac{6}{7}$ or 2.86 (3 sf) oe, eg $\frac{40}{14}$	B1 M1 A1  <b>[3]</b>	$\geq 3$ correct $\geq 3$ correct terms added SC $1 \times \frac{1}{14} + 2 \times \frac{2}{14} + 3 \times \frac{3}{14} + 4 \times \frac{4}{14} (=2.143)$ B0M1A0 $2k, 6k, 12k, 20k$ B1 $2k + 6k + 12k + 20k$ or $40k$ M1 $\div 4$ M0A0

Question		Answer	Marks	Guidance	
3	(i)	Use of 5 or 6 instead of 5.5 for last value of x: all M-marks can be scored, but no A-marks. (ans: 5 gives 2.32 and 1.23; 6 gives 2.39 and 1.40) Use of 5 <u>and</u> 6 instead of 5.5 (probably with freqs 19400/2) could lead to correct mean M1A1, but possibly M1M1A0 for sd.			
		$\frac{\Sigma fx}{\Sigma f}$ attempted ( $= \frac{662000}{280900}$ ) = 2.36 (3 sf) $\frac{\Sigma fx^2}{\Sigma f}$ attempted ( $= \frac{2042350}{280900} = 7.270737$ )  – "2.36" <sup>2</sup> (= 1.70 to 1.72, 3 sf)  s.d. = 1.31 or 1.30 (3 sf)	M1  A1  M1    M1  A1  <b>[5]</b>	3 terms of $\Sigma fx$ correct.. <u>and</u> $\div \Sigma f$ Allow incorrect $\Sigma f$ NOT $\Sigma x$  3 terms of $\Sigma fx^2$ correct and $\div \Sigma f$ Allow incorrect $\Sigma f$ NOT $\Sigma x$  dep +ve result $\div 5$ or $\div 6$ M0M0A0 allow 1.3	$\div 5$ or $\div 6$ M0A0  $\frac{\Sigma f(x-\bar{x})^2}{\Sigma f}$ 3 terms of num correct <u>and</u> $\div \Sigma f$ M2 $(86900 \times 1.36^2 + 92500 \times 0.36^2 + 45000 \times 0.64^2 + 37100 \times 1.64^2 + 19400 \times 3.1^2)$ , ( $\frac{482210.64}{280900}$ ) 2 terms of num correct <u>and</u> $\div \Sigma f$ M1  Allow incorrect $\Sigma f$ but NOT if $\Sigma f = \Sigma x$ NB $\sqrt{\quad}$ not requ'd for M1M1  Correct answer(s) without working score full marks
3	(ii)	2 3	B1 B1 <b>[2]</b>	allow IQR = 3 – 1 = 2, ie UQ = 3 implied  Ignore working for both, even if Incorrect NB 3, 2 B0B0 unless labelled correctly	

Question		Answer	Marks	Guidance
4	If $\frac{2}{3}$ is interpreted consistently as 0.6 or 0.66 or 0.67 or 0.7, max marks: (i)(a) M1M1A0 (i)(b) B0 (i)(c) B1ft B1ft (ii) B1M1M1A0			
4	(i)	(a)	Binomial seen or implied 0.6228 – 0.3497 = 0.273 (3 sf)	M1 M1 A1 [3] by use of table or ${}^9C_6$ or $(\frac{2}{3})^p(\frac{1}{3})^q$ ( $p + q = 9$ ) ${}^9C_6(\frac{1}{3})^3(\frac{2}{3})^6$ $\frac{1792}{6561}$ Eg 0.6228 seen
4	(i)	(b)	0.3497 or 0.350 (3 sf)	B1 [1] NB 0.3498 (from 0.6228 - 0.273) rounds to 0.350 so B1
4	(i)	(c)	6 2	B1ft B1ft [2] NB 2, 6 B0B0 unless labelled correctly
4	(ii)		27 seen B(27, $\frac{2}{3}$ ) seen or implied  ${}^{27}C_{18}(\frac{1}{3})^9(\frac{2}{3})^{18}$  = 0.161 (3 sf)	B1 M1  M1 A1 [4] not necessarily in a statement  or attempt eg P( $X_1 = 1$ ) × P( $X_2 = 8$ ) × P( $X_3 = 9$ ), P( $X_1 = 2$ ) × P( $X_2 = 7$ ) × P( $X_3 = 9$ ), P( $X_1 = 3$ ) × P( $X_2 = 6$ ) × P( $X_3 = 9$ ), etc ≥3 sets with $X_1+X_2+X_3=18$ (not nec'y added) M1 NB P( $X_1 = 6$ ) × P( $X_2 = 6$ ) × P( $X_3 = 6$ ) = $0.273^3 = 0.0203$ M0M0A0  $\frac{55}{729}$ (= 0.0754) M0M0A0

Question		Answer	Marks	Guidance	
5	(i)	$S_{xx} = 20400 - \frac{360^2}{8} \quad (= 4200)$ $S_{yy} = 6.88 - \frac{6.8^2}{8} \quad (= 1.1)$ $S_{xy} = 241 - \frac{360 \times 6.8}{8} \quad (= -65)$ $r = \frac{"-65"}{\sqrt{"4200" \times "1.1"}}$ $= -0.956 \text{ (3 sf)}$	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>Correct sub in a correct <math>S</math> formula</p> <p>Correct sub in 3 correct <math>S</math> formulae and a correct <math>r</math> formula</p> <p>Correct ans with no working M2A1</p>	<p>Ignore comment about <math>-1 &lt; r &lt; -0.9</math></p>
5	(ii)	eg As you move further away, prices drop	<p>B1</p> <p>[1]</p>	<p>High prices go with short distances oe</p> <p>Allow "<u>Strong</u> (or high or good or equiv) <u>neg</u> corr'n between price and distance"</p>	<p>Both variables must be in context ; miles &amp; £ enough</p> <p>Ignore all else, even if incorrect</p> <p>NOT just <u>neg</u> corr'n between price &amp; dist</p>
5	(iii)	None	<p>B1</p> <p>[1]</p>		<p>Ignore all else, even if incorrect</p>
5	(iv)	$b = \frac{"-65"}{"4200"} \quad (= -0.0154762)$ $Y - \frac{6.8}{8} = "-0.0154762"(x - \frac{360}{8}) \text{ oe}$ $y = -0.0155x + 1.55 \text{ (3 sf) oe}$ $\text{or } y = \frac{433}{280} - \frac{13}{840}x \text{ oe}$	<p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>	<p>ft their <math>S_{xy}</math> &amp; <math>S_{xx}</math> from (i) for M-marks only</p> <p>or <math>a = \frac{6.8}{8} + "-0.0154762" \times \frac{360}{8} \text{ oe}</math></p> <p>allow <math>y = -0.015x + 1.5</math> (or figs which round to these)</p> <p>(NOT <math>y = -0.016x + 1.6</math> NOT <math>y = -0.02x + 1.5</math>)</p> <p>Correct ans with no working M2A1</p>	<p>or fresh start correct method</p> <p>Must have "y = "</p> <p>Allow figures in equn which round to the correct figures to <u>either</u> 3 sf <u>or</u> 2 sf, even if they result from arith errors.</p>
5	(v)	Values of $x$ are chosen beforehand or $x$ is independent or controlled	<p>B1</p> <p>[1]</p>	<p><math>x</math> is fixed or given or set or predetermined oe</p>	<p>Not "<math>x</math> is constant."</p> <p>Not just "<math>y</math> depends on <math>x</math>"</p> <p>Ignore all other, even if incorrect</p>

Question		Answer	Marks	Guidance	
6	(i)	6 5 4 3 2 1	B1 [1]		
6	(ii)	$\Sigma d^2 = 0$ for first 6 teams $\Sigma d^2 = 2$ $1 - \frac{6 \Sigma d^2}{8(8^2 - 1)}$ $= \frac{41}{42}$ or 0.976 (3 sf)	M1 B1 M1 A1 [4]	May be implied by use of $\Sigma d^2 = 2$  ft their $\Sigma d^2 (\neq 0)$	using ranks from (i) can score 2nd M1 only
7	(i)	$\frac{n}{n+45} = \frac{5}{8}$ or $n : 45 = 5 : 3$ or $\frac{3}{8} : 45 =$ $\frac{5}{8} : n$ $n = 75$	M1 A1 [2]	$\frac{3F}{8} = 45$ & $n = \frac{5}{8} \times F$ ; $45 \times \frac{8}{3} = 45$ ; $45 \times \frac{8}{3} \times \frac{5}{8}$	correct first step involving $n$ or complete correct method for finding $n$
	(ii)	$\frac{45 + "75" + 52}{45 + "75" + 52 + 78}$ alone oe  $= \frac{86}{125}$ or $\frac{172}{250}$ or 0.688 (3 sf) oe	M1 A1ft [2]	$1 - \frac{78}{45 + "75" + 52 + 78}$ oe or $\frac{"250" - 78}{"250"}$ oe Completely correct method  ft their integer answer to (i) eg if their (i) is 28, ans 0.616 or $\frac{125}{203}$ M1A1ft	$\frac{45 + "75" + 52}{"250"} + \frac{52 + "75" + 78}{"250"} - \frac{78}{"250"}$ or $0.48 + 0.508 - 0.48 \times 0.508$
7	(iii)	(a) $\frac{10}{25} \times \frac{6}{24}$ or $\frac{6}{25} \times \frac{10}{24}$ seen (or $\frac{2}{5} \times \frac{1}{4}$ or $\frac{6}{25} \times \frac{5}{12}$ ) oe  $(\frac{10}{25} \times \frac{6}{24} + \frac{6}{25} \times \frac{10}{24})$ or $\frac{10}{25} \times \frac{6}{24} \times 2$ $= \frac{1}{5}$	M1 A1 [2]	or $\frac{10}{25} \times \frac{6}{25} + \frac{6}{25} \times \frac{10}{25}$ or $\frac{10}{25} \times \frac{6}{25} \times 2$ oe  $\frac{{}^{10}C_1 \times {}^6C_1}{{}^{25}C_2}$ oe or $\frac{10 \times 6}{300}$ oe	ie allow M1 if '2×' is omitted <b>OR</b> if 25 instead of 24, but not both errors  allow M1 for correct num or denom  NB long methods <u>may</u> be correct, eg $(\frac{14}{25} \times \frac{10}{14}) \times (\frac{11}{24} \times \frac{6}{11})$ same as $\frac{10}{25} \times \frac{6}{24}$

Question		Answer	Marks	Guidance
7	(iii) (b)	FA + MC or FC + MA Either $\frac{4}{25} \times \frac{5}{24} \times 2$ or $\frac{10}{25} \times \frac{6}{24} \times 2$ NB ft their (iiia)  $(\frac{4}{25} \times \frac{5}{24} \times 2 + \frac{10}{25} \times \frac{6}{24} \times 2 = \frac{1}{5} + \frac{1}{15})$  $= \frac{4}{15}$ or 0.267 (3 sf)	M1         A1 [2]	Allow $\frac{10}{25} \times \frac{6}{25} \times 2$ or $\frac{4}{25} \times \frac{5}{25} \times 2$ or $\frac{10}{25} \times \frac{6}{24} + \frac{4}{25} \times \frac{5}{24}$ or $\frac{10}{25} \times \frac{6}{25} + \frac{4}{25} \times \frac{5}{25}$ NB ft their (iii)(a)   $\frac{{}^{10}C_1 \times {}^6C_1}{{}^{25}C_2} + \frac{{}^4C_1 \times {}^5C_1}{{}^{25}C_2}$ oe or $\frac{60+20}{300}$ oe  cao   NB see note on long methods in 7(iia)
8	(i)	${}^5C_2$ oe seen anywhere or num= 10 alone  $\frac{{}^5C_2}{{}^8C_4}$ oe or $\frac{{}^5C_2 \times 4!}{{}^8P_4}$ oe all correct  $= \frac{1}{7}$ or 0.143 (3 sf)	M1  M1  A1  [3]	$\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5}$ or $\frac{20}{1680}$ or $\frac{1}{84}$ oe seen  $\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \times {}^4C_2 \times 2$ or $\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \times 4! \div 2$ oe or $\frac{1}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5} \times 12$ oe all correct  Correct ans scores M1M1A1 regardless of method.  alone or $\times \dots$ eg $\frac{2}{8} \times \frac{1}{7} \times \frac{5}{6} \times \frac{4}{5}$ M1 $\frac{4}{8} \times \frac{3}{7} \times \frac{4}{6}$ oe all correct M2 NB $\frac{\text{incorrect}}{{}^8C_4}$ does not score
8	(ii)	$6! \times 2$ alone or $5! \times 6 \times 2$ alone oe  $= 1440$	M2  A1 [3]	M1 for $6!$ or $5! \times 6$ or ${}^6P_5$ or 720 seen NB $5!$ scores M0 unless $5! \times 6$ or $5! \times 12$  M1 for $7! \times 2$ alone NB $7!$ scores M0 unless $7! \times 2$ alone

Question		Answer	Marks	Guidance	
8	(iii)	$6! \times 4$ alone or $6! \times 2 \times 2$ alone  = 2880	M2  A1 [3]	M1 for $6!$ or ${}^6P_5$ or 720 seen or $5! \times 6$ seen but NOT from $5! \times 3!$	5!: M0 unless $5! \times 6$ or $5! \times 12$ or $5! \times 24$
9	If 0.3 and 0.7 are interchanged consistently through all four parts, all M-marks can be scored, but no A-marks. If $1 - 0.3$ is calculated incorrectly (eg 0.6 or 0.66 or $\frac{2}{3}$ ) consistently, lose the A-mark in (i) but all other marks are available on ft, so long as $0 < \text{ans} < 1$ .				
9	(i)	$0.7^4 \times 0.3$ alone = 0.0720 (3 sf) or $\frac{7203}{100000}$ oe	M1 A1 [2]	allow 0.072	
9	(ii)	$(0.7 + 0.7^2 + 0.7^3) \times 0.3$  = 0.4599 or 0.460 (3sf) or $\frac{4599}{10000}$ oe	M2  A1 [3]	M1 for 1 term omitted, wrong or extra. must add terms, not mult.  Allow 0.46	$(1 - 0.7^4) - 0.3$ or $0.7599 - 0.3$ M2 $(1 - 0.7^4) - \dots$ or $1 - 0.3 - \dots$ M1 $0.7599 - \dots$ or $0.7 - \dots$ M1 Just $1 - 0.7^4$ or $1 - 0.3$ : M0 $(1 + 0.7 + 0.7^2 + 0.7^3) \times 0.3 - 0.3$ M2 1 term omitted, wrong or extra M1
9	(iii)	$1 - 0.7^6$  = 0.882 (3 sf)	M2  A1 [3]	M1 for $0.7^6$ alone or $1 - 0.7^5$ (= 0.832) or $1 - 0.7^7$ (= 0.918)	$0.3(1 + 0.7 + 0.7^2 + 0.7^3 + 0.7^4 + 0.7^5)$ M2 or (ii) + $0.3(1 + 0.7^4 + 0.7^5)$ M2 or (i) + (ii) + $0.3(1 + 0.7^5)$ M2  one term omitted or extra: M1 must add terms, not mult.  NB ans 0.832 might be M1M0A0 from omitting last term. Could be, eg, their (ii) + $0.3(1 + 0.7^4)$  correct working, but subtr from 1: M1



Question		Answer	Marks	Guidance
9	(iv)	$(1 - "0.882")^2 \times "0.882"$ oe  = 0.0122 (3 sf)	M1  A1ft <b>[2]</b>	or $(0.7^6)^2 \times (1 - 0.7^6)$ or $0.1176^2 \times (1 - 0.1176)$ or $(0.7^6)^2 \times$ their "0.882" or $0.3(0.7^{12} + (0.7^{13} + 0.7^{14} + \dots + 0.7^{17}))$ allow 0.0123  Not $0.7^2 \times 0.3$  Completely correct method ft their "0.882" except if 0.3 or 0.7

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