DO NOT WRITE IN THIS AREA

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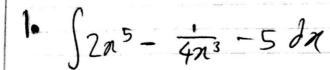
DO NOT WRITE IN THIS AREA

1. Find

$$\int \left(2x^5 - \frac{1}{4x^3} - 5\right) \mathrm{d}x$$

giving each term in its simplest form.

(4)



$$= \int 2n^5 - \frac{1}{4} x^{-3} - 5 dn$$

$$=\frac{1}{3}x^6+\frac{1}{8}x^{-2}-5x+C$$

$$= \frac{1}{3} x^6 + \frac{1}{8\pi^2} - 5x + C$$

$$y = \sqrt{x} + \frac{4}{\sqrt{x}} + 4, \quad x > 0$$

find the value of $\frac{dy}{dx}$ when x = 8, writing your answer in the form $a\sqrt{2}$, where a is a rational number.

$$\frac{\partial f}{\partial x} = \frac{1}{2} x^{-\frac{1}{2}} - 2 x^{-\frac{3}{2}}$$

$$=\frac{1}{2\sqrt{\chi}}-\frac{2}{(\sqrt{2})^3}$$

$$-\frac{\left(\frac{\partial x}{\partial x}\right)_{\chi=8}}{\left(\frac{1}{2\sqrt{8}}\right)^3} = \frac{1}{2\sqrt{8}} - \frac{2}{(\sqrt{8})^3}$$

$$=\frac{1}{4\sqrt{2}}-\frac{2}{(2\sqrt{2})^3}$$

$$=\frac{1}{4\sqrt{2}}=\frac{2}{8\sqrt{8}}$$

$$=\frac{1}{4\sqrt{2}}-\frac{1}{8\sqrt{2}}$$

$$=\frac{2}{8\sqrt{2}}-\frac{1}{8\sqrt{2}}$$

$$=\frac{1}{8\sqrt{2}}=\frac{1}{16}\sqrt{2}$$

3. A sequence $a_1, a_2, a_3,...$ is defined by

$$a_1 = 1$$

$$a_{n+1} = \frac{k(a_n + 1)}{a_n}, \quad n \ge 1$$

where k is a positive constant.

(a) Write down expressions for a_2 and a_3 in terms of k, giving your answers in their simplest form.

(3)

Given that
$$\sum_{r=1}^{3} a_r = 10$$

(b) find an exact value for k.

(3)

36).
$$Q_2 = k(-\alpha_2 - \frac{k(1+1)}{1} = 2k$$

$$a_3 = \frac{\kappa(2\mu+1)}{2\kappa} = \frac{2\kappa+1}{2} = \kappa + \frac{1}{2}$$

$$\alpha_2 = 2K$$

$$\alpha_3 = K + \frac{1}{2}$$

(b)
$$\int_{1}^{3} a_{1} = \alpha_{1} + \alpha_{2} + \alpha_{3} = 1 + 2k + k + \frac{1}{2}$$

= $3k + \frac{3}{2} = 10$

$$\Rightarrow 3K = \frac{17}{2} \Rightarrow K = \frac{17}{6}$$

The number of bicycles produ	140 bicycles each week, plans to increase its production. ced is to be increased by d each week, starting from 140 2, to 140 + 2 d in week 3 and so on, until the company is
(a) Find the value of d .	(2)
After week 12 the company pla	ans to continue making 206 bicycles each week.
(b) Find the total number of befrom and including week	•
(Na) a = 140	(5)
$4(a), \alpha = 140$ $U_{12} = 1$	40+119 = 508
	d=6
6	
Total= S12	+(508 x 40)
$=\frac{1}{2}($	12)(140 +206) + (206x40)
- 207	16+ 8240 = 10316

$$f(x) = x^2 - 8x + 19$$

(a) Express f(x) in the form $(x + a)^2 + b$, where a and b are constants.

(2)

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The curve C with equation y = f(x) crosses the y-axis at the point P and has a minimum point at the point Q.

(b) Sketch the graph of C showing the coordinates of point P and the coordinates of point O.

(3)

(c) Find the distance PQ, writing your answer as a simplified surd.

(3)

$$5(a)$$
. $F(x) = x^2 - 8x + 19 = (x - 4)^2 - 4^2 + 19$

 $(x-4)^{2}$



F(0) = 19

F(x) P(0,19)

6(4,3)

(c)

distance Pa= 142+162

16+162

16 (1+16)

6. (a) Given
$$y = 2^x$$
, show that

$$2^{2x+1} - 17(2^x) + 8 = 0$$

can be written in the form

$$2y^2 - 17y + 8 = 0$$

(2)

(b) Hence solve

$$2^{2x+1} - 17(2^x) + 8 = 0$$

(4)

$$=(2^{2x})(2)-17(2^{3})+8$$

$$= 2(2^{x})^{2} - 17(2^{n}) + 8$$

$$=2y^2-17y+8=0$$

(b)
$$2y^2 - 17y + 8 = 0$$

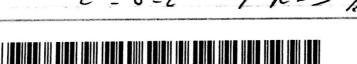
$$2y^2 - 17y + 8 = 2y^2 - 16y - y + 8$$

$$= 2y(y-8) - (y-8)$$

$$= (2y-1)(y-8) = 0$$

=)
$$y = \frac{1}{2}$$

 $y = 2^{3} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2} = 2^{2}$



7. The curve C has equation y = f(x), x > 0, where

$$f'(x) = 30 + \frac{6 - 5x^2}{\sqrt{x}}$$

Given that the point P(4, -8) lies on C,

(a) find the equation of the tangent to C at P, giving your answer in the form y = mx + c, where m and c are constants.

(4)

(b) Find f(x), giving each term in its simplest form.

(5)

$$= 30 + \frac{6 - 80}{2} = 30 - \frac{74}{2} = 30 - 37$$

$$= -8 = -7(4) + C$$

$$-1 y = -7x + 20$$

Question 7 continued

(b)
$$F'(x) = 30 + 6 \times \frac{1}{2} - 5 \frac{x^2}{x''^2}$$

$$=30+6x^{-1/2}-5x^{3/2}$$

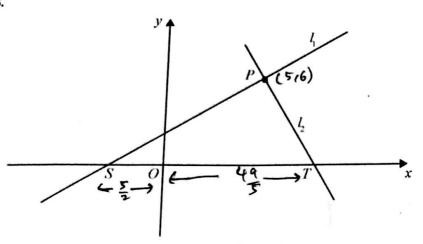
:
$$f(x) = \int f'(x) dx = 30x + 12x^{\frac{1}{2}} - 12x^{\frac{1}{2}} + C$$

$$= 120 + 24 - 2(\sqrt{4})^{5} + C$$

$$-80+C=-8$$

$$f(x) = 30x + 12\sqrt{x} - 2(\sqrt{x})^5 - 88$$

8.



Not to scale

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Figure 1

The straight line l_1 , shown in Figure 1, has equation 5y = 4x + 10

The point P with x coordinate 5 lies on ζ

The straight line l_2 is perpendicular to l_1 and passes through P.

(a) Find an equation for l_2 , writing your answer in the form ax + by + c = 0 where a, band c are integers.

(4)

The lines l_1 and l_2 cut the x-axis at the points S and T respectively, as shown in Figure 1.

(b) Calculate the area of triangle SPT.

(4)

$$g(a)$$
. $Q(b)$, $\chi = 5 = 7$ $5y = 4(5) + 10 = 30$

: for
$$f_2$$
 gradient = $\frac{-1}{4/5} = -\frac{5}{4}$

For
$$\ell z$$
: $\mathcal{O}_{\ell}^{\rho}$, $y=\delta=-\frac{5}{4}(5)$

$$y=6=-\frac{5}{4}(5)+k$$

Question 8 continued

$$\therefore K = 6 + \frac{25}{4} = \frac{27}{4} + \frac{25}{4} = \frac{99}{4}$$

$$l_1: y=0 \Rightarrow 5y=0 = 4\pi+10$$

=> $\pi_s = -\frac{5}{2}$

$$\int \left(-\frac{5}{2},0\right)$$

$$\therefore \chi_{\tau} = \frac{49}{5}$$

$$=\frac{25}{10}+\frac{98}{10}$$

$$=\frac{123}{10}$$

Area =
$$\frac{1}{2}$$
 × $\frac{123}{10}$ × $6 = 3 \times \frac{123}{10}$

$$=\frac{369}{10}$$

17

- (a) On separate axes sketch the graphs of
 - (i) y = -3x + c, where c is a positive constant,

(ii)
$$y = \frac{1}{x} + 5$$

On each sketch show the coordinates of any point at which the graph crosses the y-axis and the equation of any horizontal asymptote.

(4)

Given that y = -3x + c, where c is a positive constant, meets the curve $y = \frac{1}{x} + 5$ at two distinct points,

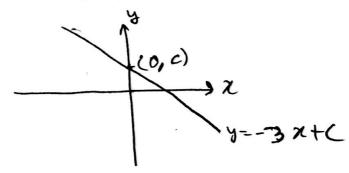
(b) show that $(5 - c)^2 > 12$

(3)

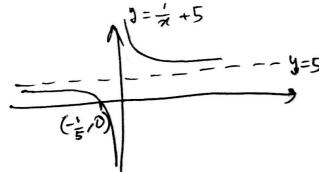
(c) Hence find the range of possible values for c.

(4)

9 (a)(i)

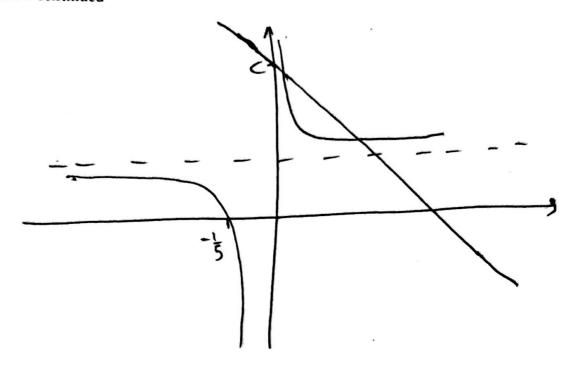


(ji)



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Question 9 continued



$$\frac{1}{12} - 321 + C = \frac{1}{21} + \frac{1}{2} + \frac{$$

We're told they neet at two distirct points.

$$\frac{1}{\pi} + 3n + 5 - C = 0$$

$$\Rightarrow 1 + 3n + (5 - c)x = 0$$

$$3x^2 + (5-c)x + 1=0$$

discrimment = 62-4ac= (5-c)2-4(3)(1) >0

Question 9 continued

$$(5-c)^2-12=0$$

 $(5-c)^2=12$
 $(5-c)=\pm 2\sqrt{3}$

$$0 < C < 5 - 2\sqrt{3}$$
 $C > 5 + 2\sqrt{3}$

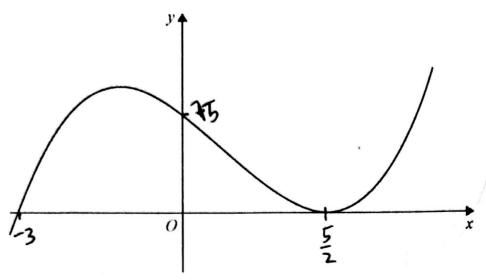


Figure 2

Figure 2 shows a sketch of part of the curve y = f(x), $x \in \mathbb{R}$, where

$$f(x) = (2x - 5)^2(x + 3)$$

- (a) Given that
 - (i) the curve with equation y = f(x) k, $x \in \mathbb{R}$, passes through the origin, find the value of the constant k,
 - (ii) the curve with equation y = f(x + c), $x \in \mathbb{R}$, has a minimum point at the origin, find the value of the constant c.

(b) Show that
$$f'(x) = 12x^2 - 16x - 35$$

Points A and B are distinct points that lie on the curve y = f(x).

The gradient of the curve at A is equal to the gradient of the curve at B.

Given that point A has x coordinate 3

(c) find the x coordinate of point B.

$$\begin{array}{c} :: \ \mathsf{K} = 75 \\ (ii) \ \mathsf{C} = 5 \\ 2 \end{array}$$

(b)
$$f(x) = (2n-5)^2(n+3)$$

= $(2n-5)(2n-5)(n+3)$
= $(4n^2-20n+25)(n+3)$

$$= 4x^3 - 8x^2 - 35x + 75$$

$$= \frac{1}{5}(x) - \frac{1}{5}(4x^3 - 10x^2 - 35x + 25x + 75)$$

$$f'(n) = \frac{\partial}{\partial n} \left(4n^3 - 8n^2 - 35n + 75 \right)$$

$$= (12n^2 - 16n - 35)$$

(c).
$$f'(3) = 12(3)^2 - 16(3)^3 - 35 = 25$$

25 is gradert at A and B

$$\frac{1}{12} - \frac{1}{16} = \frac{1}{25}$$

=)
$$(2\pi^2 - 16\pi - 66 = 0)$$

 $\chi = 3$ is a solution
 $(3-3)(12\pi+20)=0$

$$2 = 3 \quad |S = 30 \text{ MBON}$$

$$2 = 3 \quad |S = 30 \text{ MBON}$$

$$3 = 3 \quad |S = -\frac{5}{3} = 3 \quad |S$$