

10.

Figure 2

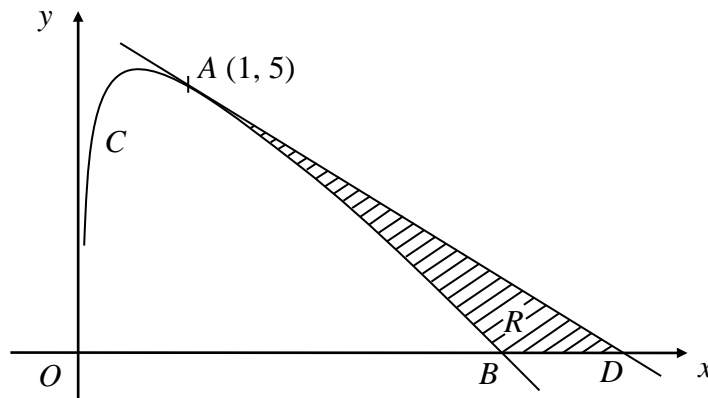


Figure 2 shows part of the curve C with equation

$$y = 9 - 2x - \frac{2}{\sqrt{x}}, \quad x > 0.$$

The point $A(1, 5)$ lies on C and the curve crosses the x -axis at $B(b, 0)$, where b is a constant and $b > 0$.

(a) Verify that $b = 4$. (1)

The tangent to C at the point A cuts the x -axis at the point D , as shown in Fig. 2.

(b) Show that an equation of the tangent to C at A is $y + x = 6$. (4)

(c) Find the coordinates of the point D . (1)

The shaded region R , shown in Fig. 2, is bounded by C , the line AD and the x -axis.

(d) Use integration to find the area of R . (6)
