OCR Maths S2

Mark Scheme Pack

2005-2014

1	(i) (a) $Po(2): 1 - P(\le 3)$	M1		Po(2) tables, "1 – " used
	= 0.1429	A1	2	Answer, a.r.t. 0.143
	(1) $\mathbf{p}_{z}(2/2) = 2/3 \left(\frac{2}{2}\right)^2$	M1		Parameter 2/3
	(b) $PO(2/3)$: $e^{-2/3} \frac{3}{2!}$	M1		Poisson formula correct, $r = 2$, any μ
	= 0.114	A1	3	Answer, a.r.t. 0.114
	(ii) Foxes may congregate so not	B1		Independent/not constant rate/singly used
	independent	B1	2	Any valid relevant application in context
2	N(80/7, 400/49)	B1		80/7. a.e.f (11.43)
	$13.5 - \frac{80}{7}$	B1		400/49 or 20/7 seen, a.e.f. (8.163 or 2.857)
	$\frac{20}{7}$	M1		Standardise with <i>np</i> & <i>npq</i> or \sqrt{npq} or <i>nq</i> , no
	= 0.725	A1		\sqrt{n}
	$1 - \Phi(0.725)$	A1		\sqrt{npa} correct
	= 0.2343	M1		13.5 correct
		A1	7	Normal tables used, answer < 0.5
				Answer, a.r.t. 0.234
				[SR: Binomial, complete expression M1, 0.231
				A1
				Po(80/7) B1, complete expression M1, 0.260
				A1
				Normal approx to Poisson, B1B0 M1A0A1
				M1A0]
3	$H_0: p = 0.3$	B1		NH stated, must be this form (or π)
	$H_1: p \neq 0.3$	B1		AH stated, must be this form (or π) [μ : B1
	B(8, 0.3)	M1		both]
	$P(\le 4) = 0.9420;$ $P(> 4) =$	A1		B(8, 0.3) stated or implied
	0.0580	M1		Any one of these four probabilities seen
	$P(\le 5) = 0.9887;$ $P(> 5) =$	N/1		<i>Either</i> compare $P(\ge 5) \& 0.025 / P(\le 4) \&$
	0.0113	MI		0.975
	Compare 0.025 or critical value 6	A 1.1	_	<i>Or</i> critical region ≥ 6 with 5
	Do not reject H_0	ΑΙν	7	H_0 not rejected, can be implied, needs
	Insufficient evidence that			essentially correct method
	manufacturer's claim is wrong			Correct conclusion in context
				[SR: Normal, Poisson: can get
				$P(\leq 5)$: first 4 marks. $P(= 5)$: first 3 marks
_	(i) P(80, 0, 02)	M1		$\frac{\text{OIIIY.}}{\text{P}(90, 0.02)} = \frac{1}{2} \frac{1}{$
4	(1) $B(80, 0.02)$	M1		B(50, 0.02) seen or implied, e.g. $N(1.0, 1.568)Bo(mp)$ used
	$\frac{approx FO(1.0)}{1 P(< 1) - 1 O 5240}$	M1		$1 \mathbf{D}(< 1) \text{ used}$
	$1 - \Gamma(\geq 1) = 1 - 0.3249$ - 0.4751		1	$1 - \Gamma(\geq 1) \text{ used}$
	- 0.4731	111	-	SR : Exact: M1 M0 M0 0 477 A11
	(ii) $P(< A) = 0.0763 P(> 5) =$	M1		Evidence for correct method e.g. answer 6
	(1) $1 (\geq 4) - 0.2703, f (\geq 3) - 0.0237$	A1		At least one of these probabilities seen
	D(< 5) = 0.0040 D(> 6) =	Al	3	Answer 6 only
	$F(\geq 3) = 0.3940, F(\geq 0) = 0.0060$	111	5	[SR N(1.6.1.568): 2.326 - $(r - 1.6)/\sqrt{1.568}$ M1
	Therefore least value is 6			r = 5 or (with cc) 6 A1
	Therefore least value is 0			$F_{\text{xact: M1 A0 A11}}$
1		l		

5	(i) $\frac{0-\mu}{2} = -2,$	M1	Standardise, allow –, allow $\mu^2/4$
	$\mu / 2$	A1	z = 2 or -2
	independent of µ	A1	<i>z</i> -value independent of μ and any relevant
	$1 - \Phi(2) = 1 - 0.9772 =$	A1	4 statement
	0.0228		Answer, a.r.t. 0.023
	(ii) $\Phi[(9-6)/3]$	M1	Standardise and use Φ [no \sqrt{n}]
	$\Phi(1.0) = 0.8413$	A1	0.8413 [not 0.1587]
	$[\Phi(1,0)]^3$	M1	Cube previous answer
	= 0.59546	A1	4 Answer, in range [0.595, 0.596]
	(iii) Annual increases not	B1	1 Independence mentioned, in context. Allow
	independent		"one year affects the next" but not "years not
	1		random"
6	$H_0: u = 32: H_1: u > 32$, where u is	B1	One hypothesis correctly stated, <i>not</i> x or \overline{x} or \overline{w}
	population mean waist measurement	B1	Both completely correct, u used
	$\frac{1}{W} = 32.3$	B1	Sample mean 32.3 seen
	$s^2 = 52214, 50/50 = \overline{W}^2$ [= 1]	M1	Correct formula for s^2 used
	$r^{2} = 50/40 \times r^{2}$ [= 50/40 or 1.0204]	M1	Multiply by 50/49 or $$
	$\sigma = 30/49 \times s$ [= 30/49 of 1.0204]		T T T T T T T T T T T T T T T T T T T
	$\alpha: z = (32.3 - 32) \times \sqrt{49}$	M1	Correct formula for z, can use s, aef, need $\mu = 32$
	= 2.1	A1	$z = 2.1 \text{ or } 1 - \Phi(z) = 0.0179, not - 2.1$
	Compare 2.1 with 3.09	B1	Explicitly compare their 2.1 with 3.09(0) or their
	or 0.0179 with 0.001		0.0179 with 0.001
	$\beta: CV = 32 + 3.09 \div \sqrt{49}$	M1	$32 + z \times \sigma/\sqrt{n}$ [allow \pm , s, any z]
	= 32.44	B1	$z = 3.09$ and (later) compare \overline{x}
	Compare CV with 32.3	A1√	CV in range [32.4, 32.5], $\sqrt{\text{on } k}$
	Do not reject H_0	M1√	Correct conclusion, can be implied, needs
	5	,	essentially correct method including \sqrt{n} .
	Insufficient evidence that waists are		any reasonable σ , but not from $\mu = 32.3$
	actually larger	A1√	Interpreted in context
		10	1
7	(i) $80 - c = 2.326$	М	Equate standardised variable to Φ^{-1} , allow –
	$\frac{1}{8/\sqrt{12}} = 2.320$	1	$\sqrt{12}$, 8 correct
		А	2.326 or a.r.t 2.33 seen, signs must be correct
	<i>c</i> = 74.63	1 4	Answer, a.r.t. 74.6, cwo, allow \leq or \geq
		В	
		1	
		А	
		1	
	(ii) (a) Type I error	B 1	"Type I error" stated, needs evidence
	(b) Correct	1√ 1	"Correct" stated or clearly implied
		В	Wrong <i>c</i> : $74 < c < 75$, $B1\sqrt{B1}$
		1√	c < 74, both "correct", B1. 75 < $c < 80$, both
			"Type I", B1
			Also allow if only one is answered
	(111) $\frac{74.63 - \mu}{8\sqrt{12}} = -1.555$	M1*d	$\frac{c-\mu}{c+\sqrt{2}} = (\pm)\Phi^{-1}$, allow no $\sqrt{12}$ but not 80, not
	$\delta / \sqrt{12}$	ep	8/ 12
	Salva for u		0.8264
	Solve for μ	A1√	Correct including sign, \vee on their <i>c</i>
	$\mu = 78.22$	dep*	Solve to find μ , dep, answer consistent with signs
		MI	Answer, a.r.t. 78.2
		AI	
		4	

8	(i)	$\int_{-\infty}^{1} x^n dx = \left[\frac{x^{n+1}}{x}\right]_{-\infty}^{1} = \frac{1}{x}$	M1		Integrate x^n , limits 0 and 1
		$\int_{0}^{n} \left[\frac{n+1}{2} \right]_{0}^{n+1}$ k/(n+1) = 1 so k = n + 1	M1 A1	3	Equate to 1 and solve for k Answer $n + 1$, not 1^{n+1} , c.w.o.
	(ii)	$\int_{0}^{1} x^{n+1} dx = \left[\frac{x^{n+2}}{n+2}\right]_{0}^{1} = \frac{1}{n+2}$	M1 A1		Integrate x^{n+1} , limits 0 and 1, not just $x.x^n$ Answer $\frac{1}{n+2}$
		$\mu = \frac{k}{n+2} = \frac{n+1}{n+2} \mathbf{AG}$	A1	3	Correctly obtain given answer
	(iii)	$\int_{0}^{1} x^{5} dx = \left[\frac{x^{6}}{6}\right]_{0}^{1} \left[=\frac{1}{6}\right]$	M1 M1		Integrate x^5 , limits 0 and 1, allow with <i>n</i> Subtract $\left(\frac{4}{5}\right)^2$
		$\sigma^2 = \frac{4}{6} - \left(\frac{4}{5}\right)^2 = \frac{2}{75}$	A1	3	Answer $\frac{2}{75}$ or a.r.t. 0.027
	(iv)	$N\left(\frac{4}{5},\frac{2}{7500}\right)$	B1 B1 B1√	3	Normal stated Mean $\frac{4}{5}$ or $\frac{n+1}{n+2}$
	(v)	Same distribution, translated	M1		Can be negative translation; <i>or</i> integration, must include correct method for integral
		Mean 0	A1√		(Their mean) $-\frac{4}{5}$, c.w.d.
		Variance $\frac{2}{75}$	B1√ 3		Variance same as their (iii), or $\frac{2}{75}$ by integration

1		$x = x \int_{-\infty}^{4} x = x \int_{-\infty}^{1} x^{4} \int_{-\infty}^{4} x = x \int_{-\infty}^{1} x^{4} \int_{-\infty}^{1} x = x \int_{-\infty}^{1} x \int_{-\infty}^{1} x = x \int_{-\infty}^{1} x \int_{-\infty}^$	M1		Integrate <i>x</i> f(<i>x</i>), limits 3 & 4 [can be implied]
		$\mu - \frac{3}{37} \int_{3} x^{3} dx = \frac{3}{37} \left[\frac{1}{4} \right]_{3} $			$\left[\frac{525}{148} \text{ or } 3.547\right]$
		$3\frac{81}{148}$]	M1		Attempt to integrate $x^2 f(x)$, limits 3 & 4
		Γ5] ⁴	A1		Correct indefinite integral, any form
		$\frac{3}{37}\int_{3}^{4} x^4 dx = \frac{3}{37}\left \frac{x}{5}\right $	A1		$\frac{2343}{185}$ or in range [12.6, 12.7] [can be implied]
		$\begin{bmatrix} -12 \\ -12 \end{bmatrix}_3$	M1		Subtract their μ^2
		$= 12\frac{122}{185}$ or 12.003	A1	6	Answer, in range [0.0575, 0.084]
		$\sigma^2 = 12\frac{123}{185} - 3\frac{81}{148}^2 = 0.0815$			
2	(i)	Find $P(R \ge 6)$ or $P(R < 6)$	M1		Find $P(= 6)$ from tables/calc, OR RH critical
		= 0.0083 or 0.9917	A1		
		Compare with 0.005 loop he from	D1		$P(\geq 6)$ in range [0.008, 0.0083] or $P(< 6) =$
		Compare with 0.025 [can be from	ы	1	0.9917 OP CP is 6 with probability
		[0.05 if "empty I H tail	A1√	4	0 0083/0 9917
		stated]	, ·		Explicitly compare with 0.025 for 0.975 if
		Reject H ₀			consistent]
					OR state that result is in critical region
					Correct comparison and conclusion, $$ on their p
	(ii)	$n = 9$, $P(\le 1) = 0.0385$ [> 0.025]	M1		At least one, or $n = 8$, $P(\le 1) = 0.0632$
		$n = 10, P(\le 1) = 0.0233 [< 0.025]$	A1		Both of these probabilities seen, don't need
		Therefore <i>n</i> = 9	B1	3	0.025
					Answer $n = 9$ only, indep't of M1A1, not from P(=
3	(i)	$(140 - u)/\sigma = -2.326$	M1		One standardisation equated to Φ^{-1} allow "1_"
J	(')	$(300 - \mu)/\sigma = 0.842$	B1		σ^2
		(000 µ)/0 = 0.042	A1√		Both 2.33 and 0.84 at least, ignore signs
		Solve to obtain:	M1		Both equations completely correct, $$ on their z
		μ = 257.49	A1		Solve two simultaneous equations to find one
		σ = 50.51	A1	6	variable
					μ value, in range [257, 258]
					σ in range [50.4, 50.55]
	(ii)	Higher	B1	•	"Higher" or equivalent stated
4	(i)	as there is positive skew	B1 D1	2	Plausible reason, allow from normal calculations
4	(1)	selected (and all selections	ы	'	alone is insufficient, but don't need this. An
		independent) OR each possible			example is insufficient.
		sample equally likely			
[(ii)	B(6, 5/8)	M1		B(6, 5/8) stated or implied, allow e.g. 499/799
		${}^{6}C_{4} p^{4} (1-p)^{2}$	M1		Correct formula, any p
		= 0.32187	A1√	3	Answer, a.r.t. 0.322, can allow from wrong <i>p</i>
	(iii)	N(37.5, 225/16)	B1		Normal, mean 37.5, or 37.47 from 499/799,
		$\frac{39.5 - 37.5}{2} = 0.5333$	B1 M1 -l		499/800 14.0625 or 2.75 open offers 14.07/44.1 or 2.75
		3.75		b	14.0020 of 3.75 seen, allow 14.07/14.1 of 3.75 Standardisa, wrong or no co, no and no \sqrt{r}
		1	den M	1	Stanuardise, wrong of no cc, np , npq , no \sqrt{n}
		ι – Ψ(U.5333) – 0 207	A1	•	Tables used answer $< 0.5 \text{ p} = 5/8$
		- 0.231	6		Answer, a.r.t. 0.297
			-		SR: $np < 5$: Po(np) stated or implied.
					B1

5	(i)	B(303, 0.01)	B1		B(303, 0.01) stated, allow $p = 0.99$ or 0.1
		D (0.00)	D 4		Allow Bin implied clearly by parameters
		≈ Po(3.03)	B1	2	(ii)
	(ii)	-3.03 (1 - 2.02 3.03^{2}) - 0.4165	M1		Correct formula, ± 1 term or "1 – " or both
		$e^{-5.05}(1+3.03+\frac{1}{2}) = 0.4103$	A1	2	Convincingly obtain 0.4165(02542) [Exact:
		AG			0.41535]
	(iii)	$302 \text{ seats} \Rightarrow \mu = 3.02$	M1		Try smaller value of μ
		$e^{-3.02}(1+3.02) = 0.1962$	M1		Formula, at least one correct term
			AI		Correct number of terms for their μ
		0.196 < 0.2		F	0.1962 [or 0.1947 from exact]
	00	So 302 seats.		D	Answer 302 only
	SR:	B(303, 0.99): B1B0; M0; M1 then N(2	298.98,2.	98	98) or equiv, standardise: M1A1 total 4/9
	ЗΝ.	$\rho = 0.1$. $D(303, 0.1), N(30.3, 0.1)$	21.21) D		$0,$ Standardise 2 with $np \propto \sqrt{npq}$, with $0,$
	SR	6/0	npαvn	υq,	solve quadratic for \sqrt{n} , $n = 339$. WHWHWHAT, total
	0.0	B(303, 0, 01) ≈ N(3, 03, 2, 9997). B1B	0. M0A0	·м	140
6	(i)	Customers arrive independently	B1 1	1	Valid reason in context, allow "random"
	(ii)	1 – 0.9921	M1		Poisson tables. "1 –", or correct formula \pm 1 term
	()	= 0.0079	A1 2	2	Answer, a.r.t. 0.008 [1 – 0.9384 = 0.0606: M1A0]
	(iii)	N(48, 48)	B1		Normal, mean 48
	. ,	z = 55.5 - 48	B1√		Variance or SD same as mean $$
		$\overline{\sqrt{48}}$	M1 dep		Standardise, wrong or no cc, $\mu = \lambda$
		= 1.0825	A1		Correct cc, $\sqrt{\lambda}$
		1 – Ф(1.0825)	dep M1		Use tables, answer < 0.5
		= 0.1394	A1	6	Answer in range [0.139, 0.14]
	(iv)	$e^{-\lambda} < 0.02$	M1		Correct formula for P(0), OR P(0 λ = 4) at least
		$\lambda > -$ ln 0.02	M1		In used OR λ = 3.9 at least by T & I
		= 3.912	A1		3.91(2) seen OR λ = 3.91 at least by T & I
		0.4t = 3.912: $t = 9.78$ minutes	M1	_	Divide λ by 0.4 or multiply by 150, any distribution
		t = 9 minutes 47 seconds	A1 5		587 seconds \pm 1 sec [inequalities not needed]

7	(i)	$\frac{c - 4000}{60 / \sqrt{50}} = 1.645$ Solve $c = 4014$ [4013.958] Critical region is > 4014	M1 B1 A1√ M1 A1 A1√ 6	Standardise unknown with $\sqrt{50}$ or 50 [ignore RHS] z = 1.645 or -1.645 seen Wholly correct eqn, $$ on their z [1 - 1.645: M1B1A0] Solve to find c Value of c, a.r.t. 4014 Answer "> 4014", allow \geq , $$ on their c, needs M1M1
	(ii)	Use "Type II is: accept when H_0 false" $\frac{4020 - 4014}{60 / \sqrt{50}}$ = 0.7071 [0.712 from 4013.958] 1 - Φ (0.7071) = 0.240 [0.238 from 4013.958]	M1dep depM1 A1√ A1 M1 A1 6	Standardise 4020 and 4014 $$, allow 60 ² , cc With $\sqrt{50}$ or 50 Completely correct LHS, $$ on their <i>c</i> <i>z</i> -value in range [0.707, 0.712] Normal tables, answer < 0.5 Answer in range [0.2375, 0.2405]
	(iii)	Smaller Smaller cv, better test etc	B1 B1 2	"Smaller" stated, no invalidating reason Plausible reason
	(iv)	Smaller Smaller cv, larger prob of Type I etc	B1 B1 2	"Smaller" stated, no invalidating reason Plausible reason
	(v)	No, parent distribution known to be normal	B2 2	"No" stated, convincing reason SR: If B0, "No", reason that is not invalidating: B1

For over-specified answers (> 6SF where inappropriate) deduct 1 mark, no more than once in paper.

1	$\frac{22-\mu}{\mu} = -\Phi^{-1}(0.242)$	M1		Standardise with Φ^{-1} , allow +, "1 –" errors, cc, $\sqrt{5}$ or 5^2
	5	A1		Correct equation including signs, no cc, can be wrong Φ^{-1}
	= -0.7	B1		0.7 correct to 3 SF, can be +
	$\mu = 25.5$	A1	4	Answer 25.5 correct to 3 SF
2	(i) $900 \div 12 = 75$	B1	1	75 only
	(ii) (a) True, first choice is random	B1	1	True stated with reason based on first choice
	(b) False, chosen by pattern	B1	1	False stated, with any non-invalidating reason
	(iii) Not equally likely	M1		"Not equally likely", or "Biased" stated
	e.g. $P(1) = 0$, or triangular	A1	2	Non-invalidating reason
3	Let <i>R</i> be the number of 1s	B1		B(90, 1/6) stated or implied, e.g. Po(15)
	$R \sim B(90, 1/6)$	B1		Normal, $\mu = 15$ stated or implied
	≈ N(15, 12.5)	B1		12.5 or $\sqrt{12.5}$ or 12.5 ² seen
	13.5 - 15 [= -0.424]	M1		Standardise, <i>np</i> and <i>npq</i> , allow errors in $$ or cc or both
	$\sqrt{12.5}$	A1		$\sqrt{\text{and cc both right}}$
	0.6643	A1	6	Final answer, a.r.t. 0.664. [Po(15): 1/6]
4	(i) $\overline{w} = 100.8 \div 14 = 7.2$	B1		7.2 seen or implied
	938.70 -2 [15 21]	M1		Use Σw^2 – their \overline{w}^2
	$-\frac{14}{14} - w^2 = 15.21$			
	× 14/13	M1		Multiply by $n/(n-1)$
	= 16.38	A1	4	Answer, a.r.t. 16.4
	(ii) $N(7.2, 16.38 \div 70)$	B1		Normal stated
	[= N(7.2, 0.234)]	B 1√		Mean their \overline{w}
		B 1√	3	Variance [their (i) $\sqrt{2}$ ÷ 70], allow arithmetic slip
5	(i) $\lambda = 1.2$	B1		Mean 1.2 stated or implied
	Tables or formula used	M1		Tables or formula [allow ± 1 term, or "1 –"] correctly used
	0.6626	A1	3	Answer in range [0.662, 0.663]
				[.3012, .6990, .6268 or .8795: B1M1A0]
	(ii) B(20, 0.6626 $$)	M1		B(20, p), p from (i), stated or implied
	${}^{20}C_{13} 0.6626^{13} \times 0.3374^7$	M1		Correct formula for their p
	0.183	A1	3	Answer, a.r.t. 0.183
	(iii) Let <i>S</i> be the number of stars	B1		Po(24) stated or implied
	$S \sim \text{Po}(24)$	B1		Normal, mean 24
	≈ N(24, 24)	B1√		Variance 24 or 24^2 or $\sqrt{24}$, $\sqrt{124}$ if 24 wrong
	$\frac{29.5 - 24}{12271}$ [=1 12271	M1		Standardise with λ , λ , allow errors in cc or $$ or both
	$\sqrt{24}$ [-11227]	A1		$\sqrt{\lambda}$ and cc both correct
	0.8692	A1	6	Answer, in range [0.868, 0.8694]

6	(i)	$\begin{bmatrix} bx^2 \end{bmatrix}^2$	M1		Use total area $= 1$
	(1)	$\left \frac{ax+2}{2} \right _{0} = 1$	B1		Correct indefinite integral, or convincing area method
		2a + 2b = 1	A1	3	Given answer correctly obtained, "1" appearing before
		2u + 2v - 1 AG			last line $[if + c, must see it eliminated]$
	(ii)	$\left[\frac{ax^2}{ax^2} + \frac{bx^3}{ax^3}\right]^2 - \frac{11}{ax^2}$	M1		Use $\int xf(x)dx = 11/9$, limits 0, 2
		$\begin{bmatrix} 2 & 3 \end{bmatrix}_0^{-9}$	B1		Correct indefinite integral
		$2a + \frac{8b}{10} = \frac{11}{10}$	A1		Correct equation obtained, a.e.f.
		3 9	M1		Obtain one unknown by correct simultaneous method
		Solve simultaneously	A1		a correct, $1/6$ or a.r.t 0.167
		$a = \frac{1}{6}, b = \frac{1}{3}$	A1	6	<i>b</i> correct, 1/3 or a.r.t. 0.333
	(iii)	$e \sigma P(< 11/9) = 0.453 \text{ or}$	M1		Use $P(r < 11/9)$ or integrate to find median m
	(111)	$\begin{bmatrix} 1 & 2 \end{bmatrix}^m$ $\begin{bmatrix} 1 & 2 \end{bmatrix}^m$	M1		Substitute into $f(r)dr \sqrt{n a} b$ limits 0 and 11/9 or m
		$\left ax + \frac{bx}{2} \right = 0.5, m = 1.303 \text{ or } \frac{\sqrt{13} - 1}{2}$			Substitute into $f(x) dx$, voin u, v , mints o and $f(x) dx$ in m
			A1		Correct numerical answer for probability or m
		Hence median > mean	$\Delta 1$	4	Correct conclusion, ewo
				-	["Negative skew" M2: median \geq mean Δ 2]
7	(;)	$U_{n} = 0.25$ [or $n > 0.25$]	R1		[Negative skew , $M2$, includin > includi, $A2$] Fach hypothesis correct $B1 + B1$ allow $n > 25$ if 25 used
'	(1)	$H_0: p = 0.55$ [or $p \ge 0.55$]	DI R1		Each hypothesis confect, B1+B1, allow $p \ge .55$ if .55 used [Wrong or no symbol B1 but nor nor \overline{r} : B0]
		$n_1 \cdot p < 0.55$ P(14, 0.25)	M1		[wrong of no symbol, b 1, but 7 of x of x. b 0]
		D(14, 0.55) D(<2) = 0.0820 > 0.025	1111		N(4.0) but not $\mathbf{P}_0(4.0)$
	α:	$P(\le 2) = 0.0839 > 0.025$	Λ1		N(4.9,), but <i>not</i> PO(4.9)
	þ:	$CR \leq 1$, probability 0.0205	R1		0.0839 seen, $\partial P(\leq 1) = 0.0205$ if clearly using CR
		Do not reject H_0 . Insufficient	M1		Compare binomial tail with 0.025, $\partial r R = 2$ binomial CR
		evidence that proportion that can		7	Do not reject H_0 , v on their probability, <i>not</i> from N or Po
		receive Channel C is less than 35%		···	or $P(<2)$; Contextualised conclusion V
	(11)	B(8, 0.35): P(0) = 0.0319	MI		Attempt to find $P(0)$ from $B(n, 0.35)$
		B(9, 0.35): P(0) = 0.0207	AI		One correct probability $[P(\le 2) = .0236, n = 18: M1A1]$
			AI		Both probabilities correct
		Hence largest value of <i>n</i> 1s 8	AI	4	Answer 8 or \leq 8 only, needs minimum M1A1
	or	$0.65^n > 0.025; n \ln 0.65 > \ln 0.025$	M1N	<i>A</i> 1	$p^n > 0.025$, any relevant p; take ln, or T&I to get 1 SF
		8.56; largest value of $n = 8$	A1A	.1	In range [8.5, 8.6]; answer 8 or \leq 8 only
8	(i) α:	$\frac{100.7 - 102}{2} = -2.076$	M1		Standardise 100.7 with $\sqrt{80}$ or 80
		5.6/ \(\sqrt{80}\)	A1		a.r.t. -2.08 obtained, must be $-$, <i>not</i> from $\mu = 100.7$
		Compare with –2.576	B1		-2.576 or -2.58 seen and compare z, allow both +
	or β :	$\Phi(-2.076) = 0.0189$	M 1		Standardise 100.7 with $\sqrt{80}$ or 80
		$[or \Phi(2.076) = 0.981]$	A1		a.r.t. 0.019, allow 0.981 only if compared with 0.995
		and compare with 0.005 [or 0.995]	B 1	(3)	Compare correct tail with 0.005 or 0.995
	or γ :	$102 - k \times 5.6$	M 1		This formula, allow +, 80, wrong SD, any k from Φ^{-1}
	0. 1.	$102 - \frac{1}{\sqrt{80}}$			
		k = 2.576, compare 100.7	B 1		k = 2.576/2.58, – sign, and compare 100.7 with CV
		100.39	A1	(3)	CV a.r.t. 100.4
		Do not reject H ₀	M1		Reject/Do not reject. $\sqrt{1}$ needs normal. 80 or $\sqrt{80}$. Φ^{-1} or
		Insufficient evidence that quantity			equivalent, correct comparison. <i>not</i> if clearly $\mu = 100.7$
		of SiO_2 is less than 102	A1	2	Correct contextualised conclusion
	(ii) (a)	c-102	M1		One equation for c and n equated to Φ^{-1} allow cc
	(II) (a)	$\frac{1}{5.6/\sqrt{n}} = -2.326$	B1		wrong sign σ^2 : 2.326 or 2.33
		13.0256 AG	A1	3	Correctly obtain given equation needs in principle to
		$102-c = \frac{100}{\sqrt{n}}$		-	have started from $c = 102 = 2326$
	(1-)	c-100 9.212	M1		Second equation, as before
	(b)	$\frac{c}{5} \frac{100}{c} = 1.645$ or $c - 100 = \frac{9.212}{\sqrt{2}}$		2	Completely correct aef
		$5.0/\sqrt{n}$ \sqrt{n}	1 1 1	-	
	(c)	Solve simultaneous equations	M1		Correct method for simultaneous equations find a crain
		$\sqrt{n-11}$ 12			\sqrt{n} correct to 3 SE
		n = -124	A1		n = 124 only
		$n_{min} - 127$		4	$n_{min} = 124$ OIIIy Critical value correct 100.8 or bottor
		C – 100.03	111	-	Chucar value contect, 100.0 01 Detter

1	(i)	$\hat{\mu} = 4830.0/100 = 48.3$	B1		48.3 seen
		$249509.16/100 - (\text{their } \bar{x}^2)$	M1		Biased estimate: 162.2016: can get B1M1M0
		× 100/99	M1		Multiply by $n/(n-1)$
		= 163.84	A1	4	Answer, 164 or 163.8 or 163.84
	(ii)	No. Central Limit theorem applies.	B2	2	"No" with statement showing CLT is understood
	(11)	so can assume distribution is	22	-	(though CLT does not need to be mentioned)
		normal			[SR: No with reason that is not wrong: B1]
2		B(130, 1/40)	B1		B(130, 1/40) stated or implied
4		$P_{130}(130, 170)$	M1		B(150, 1740) stated of implied B(150, 1740) stated of implied
		$\approx FO(5.25)$			Peremeter their an encompating (a, b)
		$e^{-\lambda} \frac{1}{4!}$			Connect formula on intermelation
				_	A success 0.18 success 0.180
		= 0.180	AI	5	Answer, 0.18 or a.r.t. 0.180
2		D' ' 1	D1	-	[SR: $N(3.25, 3.17)$ or $N(3.25, 3.25)$: B1M1A1]
3	(1)	Binomial	BI	. <u>I</u>	Binomial stated or implied
	(11)	Each element equally likely	B1		All elements, or selections, equally likely stated
		Choices independent	B1	2	Choices independent [not just "independent"]
					[can get B2 even if (i) is wrong]
4	(i)	<i>Two of:</i> Distribution symmetric	B1		One property
		No substantial truncation	B1	2	Another definitely different property
		Unimodal/Increasingly			Don't give both marks for just these two
		unlikely further from μ , etc			"Bell-shaped": B1 only unless "no truncation"
	(ii)	Variance 8 ² /20	M1		Standardise, allow cc, don't need n
		47.0 - 50.0 = -1.677	A1		Denominator (8 or 8^2 or $\sqrt{8}$) ÷ (20 or $\sqrt{20}$ or 20^2)
		$z = \frac{1}{\sqrt{8^2/20}}$ 1.577	A1		<i>z</i> -value, a.r.t. –1.68 or +1.68
		V0 / 20	Δ1	4	Answer a rt 0.052
		$\Phi(1.677) = 0.0522$	A 1	-	Allswel, a.i.t. 0.933
5	(i)	$\Phi(1.677) = 0.9532$	R1	1	Allswei, a.i.t. 0.955
5	(i)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15	B1 M1	1	Answer, a.r.t. 0.993 $\lambda > 2.5$ or 15, allow μ , don't need "H _J " $\lambda = 15$ word $N(15, 15)$ acts this mark only 1
5	(i) (ii)	$\Phi(1.677) = 0.9532$ $H_1: \lambda > 2.5 \text{ or } 15$ Use parameter 15 P(> 22)	B1 M1 M1	1	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_1"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$
5	(i) (ii)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15 Use parameter 15 P(> 23)	B1 M1 M1	1	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_1"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5
5	(i) (ii)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15 Use parameter 15 P(> 23) Use 0.9805 = 0.0195 or 1.95%	B1 M1 M1	1	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_J"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122
5	(i) (ii)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15 Use parameter 15 P(> 23) $1 - 0.9805 = 0.0195$ or 1.95%	B1 M1 M1 A1	- 1 3	Answer, a.r.t. 0.933 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SPL 2 triled 2.0% extra 2/2 here]
5	(i) (ii)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15 Use parameter 15 P(> 23) 1 - 0.9805 = 0.0195 or 1.95%	B1 M1 M1 A1	<u>1</u> 3	Answer, a.r.t. 0.933 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here]
5	(ii) (iii)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15 Use parameter 15 P(> 23) 1 - 0.9805 = 0.0195 or 1.95% P($\leq 23 \mid \lambda = 17$) = 0.9367 P($\leq 23 \mid \lambda = 17$) = 0.9367	B1 M1 M1 A1 M1	3	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.0047, 0.9551, .0217, .0022, .0007, .8989,
5	(i) (ii) (iii)	$\Phi(1.677) = 0.9532$ $H_1: \lambda > 2.5 \text{ or } 15$ Use parameter 15 $P(> 23)$ $1 - 0.9805 = 0.0195 \text{ or } 1.95\%$ $P(\le 23 \mid \lambda = 17) = 0.9367$ $P(\le 23 \mid \lambda = 18) = 0.8989$	M1 M1 A1	3	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 D
5	(i) (ii) (iii)	$\begin{split} \Phi(1.677) &= 0.9532 \\ \hline H_1: \ \lambda > 2.5 \ or \ 15 \\ \hline Use \ parameter \ 15 \\ P(> 23) \\ \hline 1 &= 0.9805 = 0.0195 \ or \ 1.95\% \\ \hline P(\leq 23 \mid \lambda = 17) = 0.9367 \\ P(\leq 23 \mid \lambda = 18) = 0.8989 \\ \hline Parameter = 17 \end{split}$	M1 M1 A1 M1 A1	3	Answer, a.r.t. 0.993 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo
5	(i) (ii) (iii)	$\Phi(1.677) = 0.9532$ $H_1: \lambda > 2.5 \text{ or } 15$ Use parameter 15 $P(> 23)$ $1 - 0.9805 = 0.0195 \text{ or } 1.95\%$ $P(\le 23 \mid \lambda = 17) = 0.9367$ $P(\le 23 \mid \lambda = 18) = 0.8989$ Parameter = 17	MI MI A1 MI A1	3	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used } [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17]
5	(i) (ii) (iii)	$\begin{split} \Phi(1.677) &= 0.9532 \\ \hline H_1: \ \lambda > 2.5 \ \text{or} \ 15 \\ \hline Use \ parameter \ 15 \\ P(> 23) \\ \hline 1 &= 0.9805 = 0.0195 \ \text{or} \ 1.95\% \\ \hline P(\leq 23 \mid \lambda = 17) = 0.9367 \\ P(\leq 23 \mid \lambda = 18) = 0.8989 \\ \hline Parameter = 17 \\ \hline \lambda = 17/6 \ \text{or} \ 2.83 \end{split}$	B1 M1 M1 A1 M1 M1 M1	3	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used } [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85]
5	(i) (ii) (iii)	$\Phi(1.677) = 0.9532$ H ₁ : $\lambda > 2.5$ or 15 Use parameter 15 P(> 23) 1 - 0.9805 = 0.0195 or 1.95% P($\leq 23 \mid \lambda = 17$) = 0.9367 P($\leq 23 \mid \lambda = 18$) = 0.8989 Parameter = 17 $\lambda = 17/6$ or 2.83	AI B1 M1 A1 A1 A1 A1 M1	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0]
5	(i) (ii) (iii)	$\begin{split} \Phi(1.677) &= 0.9532 \\ \hline H_1: \ \lambda > 2.5 \text{ or } 15 \\ \hline Use \text{ parameter } 15 \\ P(> 23) \\ \hline 1 &- 0.9805 = 0.0195 \text{ or } 1.95\% \\ \hline P(\leq 23 \mid \lambda = 17) = 0.9367 \\ P(\leq 23 \mid \lambda = 18) = 0.8989 \\ Parameter = 17 \\ \hline \lambda = 17/6 \text{ or } 2.83 \\ \hline H_0: \ p = 0.19, \ H_1: \ p < 0.19 \end{split}$	A1 B1 M1 M1 A1 M1 A1 B2	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \bar{x} or r: B0
5	(i) (ii) (iii)	$\Phi(1.677) = 0.9532$ $H_1: \lambda > 2.5 \text{ or } 15$ Use parameter 15 $P(> 23)$ $1 - 0.9805 = 0.0195 \text{ or } 1.95\%$ $P(\le 23 \mid \lambda = 17) = 0.9367$ $P(\le 23 \mid \lambda = 18) = 0.8989$ Parameter = 17 $\lambda = 17/6 \text{ or } 2.83$ $H_0: p = 0.19, H_1: p < 0.19$ where p is population proportion	A1 B1 M1 M1 A1 M1 A1 B2 M1	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only
5	(i) (ii) (iii) (i)	$\begin{split} & \Phi(1.677) = 0.9532 \\ \hline H_1: \ \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ \hline 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ \hline P(\le 23 \mid \lambda = 17) = 0.9367 \\ & P(\le 23 \mid \lambda = 18) = 0.8989 \\ & \text{Parameter } = 17 \\ \hline \lambda = 17/6 \text{ or } 2.83 \\ \hline H_0: \ p = 0.19, \ H_1: \ p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \end{split}$	A1 B1 M1 M1 A1 M1 B2 M1 A1	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693]
5	(i) (ii) (iii) (i)	$\begin{split} & \Phi(1.677) = 0.9532 \\ \hline H_1: \ \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ \hline 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ \hline P(\le 23 \mid \lambda = 17) = 0.9367 \\ & P(\le 23 \mid \lambda = 18) = 0.8989 \\ & \text{Parameter } = 17 \\ \hline \lambda = 17/6 \text{ or } 2.83 \\ \hline H_0: \ p = 0.19, \ H_1: \ p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \end{split}$	A1 B1 M1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1 M1 A1	3	Answer, a.r.t. 0.955 $\lambda > 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ λ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084
5	(i) (ii) (iii) (i)	$\begin{split} & \Phi(1.677) = 0.9532 \\ & H_1: \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ & 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ & P(\le 23 \mid \lambda = 17) = 0.9367 \\ & P(\le 23 \mid \lambda = 17) = 0.8989 \\ & \text{Parameter } = 17 \\ & \lambda = 17/6 \text{ or } 2.83 \\ & H_0: p = 0.19, H_1: p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \\ & \text{Compare } 0.1 \\ \end{split}$	B1 M1 M1 A1 M1 A1 B2 M1 A1 B2 M1 A1	3	Answer, a.r.t. 0.933 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like"
6	(i) (ii) (iii) (i) <i>or</i>	$\begin{split} & \Phi(1.677) = 0.9532 \\ & H_1: \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ & 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ & P(\le 23 \mid \lambda = 17) = 0.9367 \\ & P(\le 23 \mid \lambda = 17) = 0.8989 \\ & \text{Parameter } = 17 \\ & \lambda = 17/6 \text{ or } 2.83 \\ & H_0: p = 0.19, H_1: p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \\ & \text{Compare } 0.1 \\ & \text{Add binomial probs until ans } > 0.1 \\ \end{split}$	B1 M1 M1 A1 M1 A1 B2 M1 A1 B1 A1	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like" [P(≤ 2) = 0.239]
6	(i) (ii) (iii) (i) <i>or</i>	$\begin{split} & \Phi(1.677) = 0.9532 \\ \hline H_1: \ \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ \hline 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ \hline P(\leq 23 \mid \lambda = 17) = 0.9367 \\ & P(\leq 23 \mid \lambda = 18) = 0.8989 \\ & \text{Parameter } = 17 \\ \hline \lambda = 17/6 \text{ or } 2.83 \\ \hline H_0: \ p = 0.19, \ H_1: \ p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \\ \hline \text{Compare } 0.1 \\ & \text{Add binomial probs until ans } > 0.1 \\ & \text{Critical region } \leq 1 \\ \end{split}$	A1 B1 M1 M1 A1 M1 A1 M1 A1 B2 M1 A1 B2 M1 A1 B1 A1 B1 A1 B1	3	Answer, a.r.t. 0.933 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like" [P(≤ 2) = 0.239]
6	(i) (ii) (iii) (i) <i>or</i>	$\begin{split} & \Phi(1.677) = 0.9532 \\ & H_1: \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ & 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ & P(\leq 23 \mid \lambda = 17) = 0.9367 \\ & P(\leq 23 \mid \lambda = 18) = 0.8989 \\ & \text{Parameter } = 17 \\ & \lambda = 17/6 \text{ or } 2.83 \\ & H_0: p = 0.19, H_1: p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \\ & \text{Compare } 0.1 \\ & \text{Add binomial probs until ans } > 0.1 \\ & \text{Critical region } \leq 1 \\ & \text{Reject } H_0 \end{split}$	A1 M1 M1 A1 M1 A1 B2 M1 A1 B2 M1 A1 M1	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like" [P(≤ 2) = 0.239]
6	(i) (ii) (iii) (i) <i>or</i>	$\begin{split} & \Phi(1.677) = 0.9532 \\ & H_1: \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ & 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ & P(\leq 23 \mid \lambda = 17) = 0.9367 \\ & P(\leq 23 \mid \lambda = 18) = 0.8989 \\ & \text{Parameter } = 17 \\ & \lambda = 17/6 \text{ or } 2.83 \\ & H_0: p = 0.19, H_1: p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \\ & \text{Compare } 0.1 \\ & \text{Add binomial probs until ans } > 0.1 \\ & \text{Critical region } \leq 1 \\ & \text{Reject } H_0 \\ & \text{Significant evidence that proportion} \end{split}$	$\begin{array}{c} \text{A1} \\ \text{B1} \\ \text{M1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{B2} \\ \text{M1} \\ \text{A1} \\ \text{B1} \\ \text{B1} \\ \text{B1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\$	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_j"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \overline{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like" [P(≤ 2) = 0.239] Correct deduction and method [needs P(≤ 1)] Correct conclusion in context
6	(i) (ii) (iii) (i) <i>or</i>	$\begin{split} & \Phi(1.677) = 0.9532 \\ & H_1: \lambda > 2.5 \text{ or } 15 \\ & \text{Use parameter } 15 \\ & P(> 23) \\ & 1 - 0.9805 = 0.0195 \text{ or } 1.95\% \\ & P(\leq 23 \mid \lambda = 17) = 0.9367 \\ & P(\leq 23 \mid \lambda = 18) = 0.8989 \\ & \text{Parameter } = 17 \\ & \lambda = 17/6 \text{ or } 2.83 \\ & H_0: p = 0.19, H_1: p < 0.19 \\ & \text{where } p \text{ is population proportion} \\ & 0.81^{20} + 20 \times 0.81^{19} \times 0.19 \\ & = 0.0841 \\ & \text{Compare } 0.1 \\ & \text{Add binomial probs until ans } > 0.1 \\ & \text{Critical region } \leq 1 \\ & \text{Reject } H_0 \\ & \text{Significant evidence that proportion} \\ & \text{of } e' \text{ s in language is less than } 0.19 \\ \end{split}$	$\begin{array}{c} \text{A1} \\ \text{B1} \\ \text{M1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{B1} \\ \text{B1} \\ \text{M1} \\ \text{A1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\$	3	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_J"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ $\sqrt{\lambda}$ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but <i>x</i> or \overline{x} or <i>r</i> : B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like" [P(≤ 2) = 0.239] Correct deduction and method [needs P(≤ 1)] Correct conclusion in context [SR: N(3.8, 3.078): B2M1A0B1M0]
6	(i) (ii) (iii) (i) (i)	$\Phi(1.677) = 0.9532$ $H_1: \lambda > 2.5 \text{ or } 15$ Use parameter 15 $P(> 23)$ $1 - 0.9805 = 0.0195 \text{ or } 1.95\%$ $P(\le 23 \mid \lambda = 17) = 0.9367$ $P(\le 23 \mid \lambda = 18) = 0.8989$ Parameter = 17 $\lambda = 17/6 \text{ or } 2.83$ $H_0: p = 0.19, H_1: p < 0.19$ where <i>p</i> is population proportion $0.81^{20} + 20 \times 0.81^{19} \times 0.19$ $= 0.0841$ Compare 0.1 Add binomial probs until ans > 0.1 Critical region ≤ 1 Reject H_0 Significant evidence that proportion of <i>e</i> 's in language is less than 0.19 Letters not independent	$\begin{array}{c} \text{A1} \\ \text{B1} \\ \text{M1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{A1} \\ \text{B1} \\ \text{A1} \\ \text{B1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{A1} \\ \text{M1} \\ \text{B1} \\ \end{array}$	3 3 8	Answer, a.r.t. 0.955 $\lambda \ge 2.5 \text{ or } 15, \text{ allow } \mu, \text{ don't need "H_J"}$ $\lambda = 15 \text{ used} [N(15, 15) \text{ gets this mark only}]$ Find P(> 23 or ≥ 23), final answer < 0.5 eg 0.0327 or 0.0122 Answer, 1.95% or 2% or 0.0195 or 0.02 [SR: 2-tailed, 3.9% gets 3/3 here] One of these, or their complement: .9367, .8989, 0.9047, 0.8551, .9317, .8933, .9907, .9805 Parameter 17 [17.1076], needs P(≤ 23), cwo [SR: if insufficient evidence can give B1 for 17] Their parameter ÷ 6 [2.85] [SR: Solve (23.5 – λ)/ λ = 1.282 M1; 18.05 A0] Correct, B2. One error, B1, but x or \bar{x} or r: B0 Binomial probabilities, allow 1 term only Correct expression [0.0148 + 0.0693] Probability, a.r.t. 0.084 Explicit comparison of "like with like" [P(≤ 2) = 0.239] Correct deduction and method [needs P(≤ 1)] Correct conclusion in context [SR: N(3.8, 3.078): B2M1A0B1M0] Correct modelling assumption. stated in context

7	(i)		1			B1 B1		Horiz Posit	zontal straig ive parabola	ht line . symmetric	about 0
						B1	3	Com	pletely corre	ct, including	correct relationship
		_		_				betw	een two	-	-
								Don'	t need vertic	al lines or he	orizontal lines outside
								range	e, but don't g	give last B1 i	f horizontal line
								conti	nues past "±	:1 <i>''</i>	
	(ii)	S is eq	ually likely t	o take an	iy value	B2	2	Corre	ect statemen	t about distri	butions (not graphs)
		in rang	ge, T is more	likely at					[Partial	statement, o	r correct description
	(:::)	extren				M1		Tutoo	for one of	only: BI]	() an (4, 1)
	(111)	$\int_{-\frac{3}{2}}^{1} x^2$	$dx = \left \frac{x^3}{2} \right ^2$			IVI I		meg	rate I(x) with $recover$	able if <i>t</i> used	l) of $(l, 1)$
		$\mathbf{J}_t = \mathbf{I}$	$\begin{bmatrix} 2 \end{bmatrix}_t$			B1		Corre	ect indefinite	e integral	i luter j
		$\frac{1}{2}(1 - 1)$	t^3) = 0.2 or $\frac{1}{2}$	$2(t^3 + 1) =$	= 0.8	M1		Equa	te to 0.2, or	0.8 if [-1, <i>t</i>]	used
		$t^{3} = 0.0$	6			M1		Solve	e cubic equa	tion to find <i>t</i>	
0	(1)	t = 0.8	6434			Al	5	Answ	ver, in range	[0.843, 0.84	4]
8	(1)	64.2-	$\frac{-63}{-63}$ =	1.644		Mldep		Stanc	lardise 64.2	with \sqrt{n}	
		$\sqrt{12.23}$	5/23			AI den M1		z = 1	$\Phi(z)$ or 1.64	5, must be + $r < 0.5$	
		P(z > 1)	1.044)			A1	4	Answ	$\Psi(z)$, answe ver a r t 0 0	1 < 0.5	
	(ii)	= 0.03		3.5		M1		63 +	$3.5 \times k / \sqrt{50}$) k from Φ^{-1}	not –
	(11)	(a)	63 + 1.645	$\times \frac{1}{\sqrt{50}}$		B1		k = 1	.645 (allow	1.64, 1.65)	, 1101
			≥ 63.81	v 00		A1	3	Answ	ver, a.r.t. 63.	8, allow >, ≥	≥, =, c.w.o.
		(b)	P(< 63.8	$\mu = 65)$		M1		Use of	of correct me	eaning of Ty	pe II
		~ /	63.8-65	$= -2.39^{4}$	56	M1		Stand	lardise their	c with $\sqrt{50}$	
			$3.5/\sqrt{50}$	- 2.370		A1		$z = (\pm$	e) 2.40 [or –	2.424 or – 2.	.404 etc]
			0.0083			A1	4	Answ	ver, a.r.t. 0.0	08 [eg, 0.00	767]
	(iii)	B bette	er: Type II er	ror small	ler	B2√	2	This	answer: B2.	"B because	sample bigger": B1.
•			(and same	Type I e	error)	1.62			[SR: Pa	rtial answer: -	· B1]
9	(a)	np > 5	and $nq > 5$	at		M2		Use e	either $nq > 5$	or $npq > 5$	ar "r = 20" coop M11
		n > 20		IL		A1	3	Final	answer $n >$	20 or n > 20	only $n = 20$ seen. Will
	(b)	(i) 20	$70.5 - \mu = 1'$	75σ		M1		Stand	lardise once	and equate	to Φ^{-1} + cc
	(-)		$\mu = 46.5 = 2.2$	25σ		A1		Stand	lardise twice	e, signs corre	ect, cc correct
		•				B1		Both	1.75 and 2.2	25	
			Solve simulta	neously		M1		Corre	ect solution	method to ge	t one variable
		ļ	$\mu = 60$			AIV	6	μ, a.r	t. 60.0 or \pm	154.5	1 \ \ 11 \ 11
		($\sigma = 6$			AIV	0	σ, a.r	1.1.6.00 [N]	Vrong cc (be	$1 \wedge 1 \wedge 0$
		(ji) <i>1</i>	$nn = 60 \ nna$	= 36		Miden		nn –	60 and <i>nna</i>	$= 6^2 \text{ or } 6$	
		(11) /	q = 36/60 = 0	- 30).6		depM1		Solve	e to get q or	p or n	
		I	p = 0.4			A1√		p = 0	.4 $\sqrt[3]{}$ on wro	ong cc or z	
		1	n = 150			A1√	4	n = 1	50 $\sqrt{\text{on wro}}$	ong cc or z	
					σ	μ		q	p (±0.01)	n	_
			70.5	46.5	6	60		0.6	0.4	150	
						60.062	~		0.015	4 - 4 -	
			71	46	6.25	5	0.	6504	0.3496	171.8	
			71 5	46 5	6.25	500.302	Ο	6450	0 3550	170.6	
			/1.5	10.5	0.25	59.562	0.	0100	0.5550	170.0	
			70.5	45.5	6.25	5	0.	6558	0.3442	173.0	
			71.5	45.5	6.5	60.125	0.	7027	0.2973	202.2	
			70	46	6	59.5	0.	6050	0.3950	150.6	

1		$80 - \mu = \Phi^{-1}(0.05) = 1.645$	M1		Standardise once with Φ^{-1} , allow σ^2 , cc
		$\frac{-1045}{\sigma}$	B1		Both 1.645 (1.64, 1.65) and [0.674, 0.675], ignore signs
		$\frac{\mu - 50}{2} = \Phi^{-1}(0.75) = 0.674(5)$	A1		Both equations correct apart from wrong z, not 1–1.645
		σ	M1		Solve two standardised equations
		Solve simultaneously	A1		μ, a.r.t 58.7
		$\mu = 58.7$, $\sigma = 12.9$	A1	6	σ , a.r.t. 12.9 [not σ^2] [σ^2 : M1B1A0M1A1A0]
2	(i)	Let <i>R</i> denote the number of choices	M1		$B(12, \frac{5}{6})$ stated or implied, allow 501/600 etc
		which are 500 or less.	M1		p^{12} or q^{12} or equivalent
		$R \sim \mathrm{B}(12, \frac{5}{6})$	A1	3	Answer, a.r.t. 0.112
		$P(R = 12) = \left(\frac{5}{6}\right)^{12} [=0.11216]$			$[SR: \frac{500}{600} \times \frac{499}{599} \times \frac{498}{598} \times \dots; 0.110: M1A1]$
		= 0.112	4		[M1 for 0.910 or 0.1321 or vague number of terms]
	(ii)	Method unbiased; unrepresentative by	B1		State that method is unbiased
		chance	B1	2	Appropriate comment (e.g. "not unlikely")
-	(1)	R(+4) 0.0444	D1		[SR: partial answer, e.g. not <u>necessarily</u> biased: B1]
3	(1)	$P(\le 1) = 0.0611$	BI		10.0011 seen
		$P(\ge 9) = 1 - P(\le 8) = 1 - 0.9597$			Find $P(\ge 9)$, allow 8 or 10 [0.0866, 0.01/1]
		= 0.0403 0.0611 + 0.0403 [- 0.1014]	M1		Add probabilities of tails on 1 tails 2
		-1010403 = 0.1014	A1	5	Add probabilities of talls, ∂r 1 tall × 2 Answer [10, 1, 10, 2]% or probability
	(ii)	-10.170 D(2 < C < 8)	M1		Attempt at $P(2 \le C \le 8)$ not is allow $1 \le C \le 9$ atc
	(11)	-0.8944 = 0.0266 [-0.8678]	M1		Po(5.5) tables $P(\leq \text{top and}) = P(\leq \text{bottom and})$
		= 0.868	A1	3	Answer a r t 0.868 allow %
4	(i)	3296.0	B1	-	Mean 82.4, c.a.o.
-	(1)	$\hat{\mu} = \bar{y} = \frac{1}{40} = 82.4$	M1		Use correct formula for biased estimate
		286800.4 $_{82.4^2} [= 380.25]$	M1		Multiply by $n/(n-1)$
		40 - 82.4			[SR: all in one, M2 or M0]
		$S^2 \times \frac{40}{39}$; = 390	A1	4	Variance 390, c.a.o.
	(ii)	$(60 - 82.4) = \Phi(-1.134)$	M1		Standardise, allow 390, cc or biased estimate, +/-,
		$\Phi\left(\frac{1}{\sqrt{390}}\right)$			do not allow \sqrt{n}
		= 1 - 0.8716 = 0.128	A1	2	Answer in range [0.128, 0.129]
	(iii)	No, distribution irrelevant	B1	1	"No" stated or implied, any valid comment
5	(i)	$H_0: \mu = 500$ where μ denotes	B2		Both hypotheses stated correctly
		$H_1: \mu < 500$ the population mean			[SR: 1 error, B1, but \overline{x} etc: B0]
		α : $z = \frac{435 - 500}{500} = -1.3$	M1		Standardise, use $\sqrt{4}$, can be +
		$100 / \sqrt{4}$	A1		$z = -1.3$ (allow -1.29 from cc) or $\Phi(z) = 0.0968$ (.0985)
		Compare –1.282	B1		Compare <i>z</i> & $-1.282 \text{ or } p (< 0.5)$ & 0.1 or equivalent
		β: $500 - 1.282 \times 100/\sqrt{4}$	M1		$500 - z \times 100/\sqrt{4}$, allow $\sqrt{2}$ errors, any Φ^{-1} , must be -
		= 435.9; compare 435	A1√;B1		CV correct, $$ on their <i>z</i> ; 1.282 correct and compare
		Reject H ₀	M1√		Correct deduction, needs $\sqrt{4}$, $\mu = 500$, like-with-like
		Significant evidence that number of	A1	7	Correct conclusion interpreted in context
		visitors has decreased			
	(ii)	CLT doesn't apply as <i>n</i> is small	M1		Correct reason [" <i>n</i> is small" is sufficient]
1		So need to know distribution	B1	2	Refer to distribution, e.g. "if not normal, can't do it"

6	(i)	(a) $1 - 0.8153$	M1		Po(3) tables, "1 –" used, e.g. 0.3528 or 0.0839
		= 0.1847	A1	2	Answer 0.1847 or 0.185
		(b) $0.8153 - 0.6472$	M1		Subtract 2 tabular values, or formula $[e^{-3} 3^4/4!]$
		= 0.168	A1	2	Answer, a.r.t. 0.168
	(ii)	N(150, 150)	B1		Normal, mean 3×50 stated or implied
		(165.5 - 150)	B1		Variance or SD = 3×50 , or same as μ
		$1-\Phi \left \frac{100.0 - 100}{\sqrt{150}} \right $	M1		Standardise 165 with λ , $\sqrt{\lambda}$ or λ , any or no cc
		(150)	A1		$\sqrt{\lambda}$ and 165.5
		$= 1 - \Phi(1.266) = 0.103$	A1	5	Answer in range [0.102, 0.103]
	(iii)	(a) The sale of one house does not	B1		Relevant answer that shows evidence of correct
		affect the sale of any others			understanding [but not just examples]
		(b) The average number of houses	B1	2	Different reason, in context
		sold in a given time interval is			[Allow "constant rate" or "uniform" but not "number
		constant			constant", "random", "singly", "events".]
7	(i)	$r^2 \qquad \left[kr^2 \right]^2$			$\int_{-\infty}^{2} h_{\rm eff} h_{\rm eff} = 1$ on one of twice also
		$\left \frac{1}{k} k x dx \right = \frac{k x}{2} = 2k$	M1		Use $\int_0^\infty kx dx = 1$, or area of triangle
			A1	2	Correctly obtain $k = \frac{1}{2}$ AG
		$= 1 \text{ so } k = \frac{1}{2}$			
	(ii)	Уд			
			B1		Straight line, positive gradient, through origin
			B1	2	Correct, some evidence of truncation, no need for vertical
		x			
		0 2			
	(iii)	$\int_{-\frac{1}{2}}^{2} \frac{1}{x^{2}} dx = \left[\frac{1}{2}x^{3}\right]^{2} = \frac{4}{2}$	M1		Use $\int_{-\infty}^{\infty} kx^2 dx$; $\frac{4}{2}$ seen or implied
		$\int_0^2 x^2 dx^2 = \int_0^2 x^2 dx^2 = \int_0^$	A1		$\int_0^\infty \int_0^\infty dx y_3$
		$\int_{-1}^{2} \frac{1}{x^{3}} dx = \left[\frac{1}{x^{4}}\right]^{2} [=2]$	M1		Use $\int_{-\infty}^{\infty} kr^3 dr$: subtract their mean ²
		$\int_{0}^{2} \int_{0}^{2} \int_{0}^{\infty} \int_{0$	M1		$\int_0^\infty \int_0^\infty dx$, subtract their mean
		$2 - \left(\frac{4}{3}\right)^2 = \frac{2}{9}$	A1	5	Answer $\frac{2}{9}$ or a.r.t. 0.222, c.a.o.
	(iv)	Α V	M1		Translate horizontally, allow stated, or "1, 2" on axis
	()		A1√	2	One unit to right, 1 and 3 indicated, nothing wrong seen.
			111 1	-	no need for vertical or emphasised zero bits
		$ \longrightarrow_{x} $			[If in doubt as to \rightarrow or \downarrow . M0 in this part]
		1 3			[
	(v)	<u>7</u>	B1√		Previous mean + 1
		3	B1√	2	Previous variance
		$\frac{2}{9}$			[If in doubt as to \rightarrow or \downarrow , B1B1 in this part]

8 (i)	$H_0: p = 0.65 \text{ OR } p \ge 0.65$	B2		Both hypotheses correctly stated, in this form				
	$H_1: p < 0.65$			[One error (but not r , x or \overline{x}): B1]				
	B(12, 0.65)	M1		B(12, 0.65) stated or implied				
	α : P(≤ 6) = 0.2127	A1		Correct probability from tables, <i>not</i> $P(= 6)$				
	Compare 0.10	B1		Explicit comparison with 0.10				
	$β$: Critical region ≤ 5 ; $6 > 5$	B1		Critical region ≤ 5 or ≤ 6 or $\{\leq 4\} \cap \{\geq 11\}$ & compare 6				
	Probability 0.0846	A1		Correct probability				
	Do not reject H ₀	M1√		Correct comparison and conclusion, needs correct				
	Insufficient evidence that proportion			distribution, correct tail, like-with-like				
	of population in favour is not at least	A1√		Interpret in context, e.g. "consistent with claim"				
	65%		7	[SR: N(7.8, 2.73): can get B2M1A0B1M0: 4 ex 7]				
(ii)	Insufficient evidence to reject claim;	B1√		Same conclusion as for part (i), don't need context				
	test and p/q symmetric	B1	2	Valid relevant reason, e.g. "same as (i)"				
(iii)	$R \sim B(2n, 0.65), P(R \le n) > 0.15$	M1		B(2 <i>n</i> , 0.65), P($R \le n$) > 0.15 stated or implied				
	B(18, 0.65), p = 0.1391	A1		Any probability in list below seen				
		Al		p = 0.1391 picked out (i.e., not just in a list of > 2)				
	Therefore $n = 9$	AI	4	Final answer $n = 9$ only				
				[SR < n: M1A0, n = 4, 0.1061 A1A0]				
				[SR 2-tail: MIAIA0A1 for 15 or 14]				
				[SK: 9 only, no working: M1A1]				
				[MR B(12, 0.35): M1A0, $n = 4, 0.1061$ A1A0]				
				3 0.3529 7 0.1836 12 0.0942				
				4 0.2936 8 0.1594 13 0.0832				
				5 0.2485 9 0.1391 14 0.0736				
				6 0.2127 10 0.1218 15 0.0652				

General: Conclusions to hypothesis tests must acknowledge uncertainty. Thus "time is unchanged" is A0. Similarly, "Significant evidence that time is unchanged" is also A0.

1	(*)	Discut in formation of the second discution of the second	D2	2	((D) - 122 (6
I	(1)	Diased in favour of those with strong	D2	4	biased, unrepresentative, not indept or equiv
		political interest			[but <i>not</i> "not random"] stated, with sensible reason.
					[SR: partial answer, B1]
	(ii)	Obtain list of all pupils	B1		List, can be implied; number serially or randomly,
		Allocate numbers sequentially	B1		not just "number pupils"
		Choose using random numbers	B1	3	Select consistently with method of numbering,
		C			not just "select randomly"
					[SR: systematic: List B1, every n th B1, random start B1]
					[SR: names in a hat: B2]
2	(i)	(24-30) $(20-30)$	M1		Standardise one, allow $\sqrt{12}$, 12^2 , \sqrt{n}
	~ /	$\Phi\left[\frac{1}{12}\right] - \Phi\left[\frac{1}{12}\right]$	A1		Both standardisations correct allow cc here
		(12) (12)	M1		Correct handling of toils [0,2005 0,2024]
		$= \Phi(-0.5) - \Phi(-0.833)$		4	Correct nanding of tails $[0.3085 - 0.2024]$
		= (1 - 0.6915) - (1 - 0.7976) = 0.1061	AI	4	Answer, a.r.t. 0.106, c.a.o.
	(ii)	Not symmetrical (skewed)	M1		Any comment implying not symmetric
		Therefore inappropriate	Al	2	Conclude "not good model" [Partial answer: B1]
3		$H_0: \mu = 28$	B2		Both hypotheses correctly stated; one error, allow
		$H_1: \mu \neq 28$			wrong or no letter, but not x or t or \bar{x} , B1
		$\sigma^2 = 37.05 \times 40/39$ [= 38]	M1		Multiply 37.05 or $\sqrt{37.05}$ by $n/(n-1)$ or $\sqrt{[n/(n-1)]}$
		26.44-28	M1		Standardise with \sqrt{n} , allow $\sqrt{1}$ errors, cc. +
	α	$z = \frac{1}{\sqrt{28/40}} = -1.601$	A1		Correct z a r t -1.60 or $p \in [0.0547, 0.0548]$
		$\sqrt{38/40}$	R1		Explicit comparison of z with 1.645 or n with 0.05
		Compare –1.645, or 0.0547 with 0.05			Explicit comparison of z with $-1.0+5$ of p with 0.05
	β	Critical value $28 - z\sigma/\sqrt{n}$ [= 26.397]	MI		Allow " \pm ", \vee errors, cc, ignore other tail
		z = 1.645	BI		z = 1.645 in CV expression, and compare 26.44
		Compare 26.44 with 26.40	A1√		CV, $$ on their <i>z</i> , rounding to 3 SF correct
		Do not reject H_0 [can be implied]	M1		Needs \sqrt{n} , correct method & comparison, <i>not</i> $\mu = 26.44$
		Insufficient evidence that time taken has	A1√	8	Conclusion interpreted in context, $$ on z,
		changed.			
4	(i)	53-50 < 2.326	M1		Standardise with 10 or $\sqrt{10}$ and Φ^{-1}
		$\frac{1}{\sigma/\sqrt{10}} < 2.320$	A1		Both sides same sign, $\sqrt{10}$, don't worry about <
			B1		2.326 or 2.33 seen
		$\sigma > 4.08$ AG	A1	4	Convincingly obtain $\sigma > 4.08$ to 3.SF one other step
					[SR: Substitution: standardise & substitute 4.08 M1:
		[Allow ≥]			0.0101 A1: 4.07 or 4.075 tried M1: full justification A11
	(ii)	P(Type I) = 0.01 used e.g. $Geo(0.01)$	M1		Not enough merely to state $p = 0.01$
	(11)	1(1) (1) (1) (1) (1) (1) (1) (1) (1) (1) (1)	M1		$p^4 \times q$
		- 0 0006		3	$p \wedge q$
5	(i)		M1	5	Allswei, a.i.t. 0.0090
5	(1)	$\int_{-\frac{3}{2}}^{\frac{1}{2}} (x^2 - x^4) dx = \frac{3}{2} \left[\frac{x^3}{x^3} - \frac{x^5}{x^5} \right] = \frac{1}{5}$	1/11		Attempt $\int x^2 f(x) dx$
		$\int_{-1}^{4} \frac{1}{4} \frac{1}{3} \frac{1}{5} \frac{1}{5}$	A 1		J_1 Compatindatinita integral
		$1/5 - 0^2$	AI D1		Maan O alagala in digata d
		- 1/5	BI		Mean 0 clearly indicated
		- 1/3	AI	4	Answer 1/5 or a.r.t. 0.200, don't need $\mu = 0$
	(11)		-		~
			B1		Correct graph, don't need $f(x)$ as well. Don't allow if
					graph goes further below axis than "pips".
		(a) - / / / / · · · · · · · · · · · · · · ·			Don't worry too much about exact shape
		(b) Areas equal, more spread out,	M1		Mention areas or total probability
		so g_{max} lower	A1		Convincing argument, not just "flatter"
		(c) W greater	B1dep		W greater
		as more spread out	depB1	5	with convincing reason
		us more spread out	··· I. = -		D

6	(a)	$P_0(2 375)$	M1		Po(19/8) stated or implied
0	<i>(a)</i>	(2.373)	M1		One compact Deisson formula, not tables
		$e^{-2.375}\left[\frac{2.375^3}{2.375^4} + \frac{2.375^4}{2.375^4}\right] = 0.2079 + 0.1233$			One correct Poisson formula, <i>not</i> tables
		(3! 4!)	AI		Complete correct expression, including addition
		= 0.3310	A1	4	Answer, a.r.t. 0.331
					[SR: $Po(2)$ or $Po(2.4)$ and tables, M1]
	(b)	(i) $n \text{ large OR} n > 50$	B1		Or equivalent [Allow \leq and \geq throughout]
		<i>p</i> small OR $np < 5$	B1	2	Or equivalent $e \sigma nn \approx nna$ or $n < 0.1$
		P second construction of the second		_	[Treat " $nn < 5$, $nna < 5$ " as single wrong statement]
			M1		[fired $np < 5$, $npq < 5$ as single wrong statement]
		(ii) $B(108, \frac{1}{36})$			
		$\approx Po(3)$	MI		$Po(np), \forall$ on their n, p
		1 P(< 2) = 1 0 6472	Al		Po(3)
		$1 - \Gamma(\leq 5) = 1 - 0.0472$	M1		Use Po tables, "1 –", <i>or</i> correct formula, ± 1 term,
		= 0.3528	A1	5	e.g. 0.1847; a.r.t. 0.353, allow from exact Binomial
7	(i)	Dropped catches must occur	B1		"independently" in context allow "random"
,	(1)	independently of one another and at	B1	2	"Constant average rate" in context
		acoustant success note	DI	4	Constant average rate, in context
		constant average rate			
	(11)	Use: "Reject H_0 when correct"	MI		Find $P(\geq r)$ where $r > \lambda$, e.g. $P(\geq 6)$ from $Po(2)$
		Po(10)	M1		Po(10) stated or implied [can be recovered in (iii)]
ar		$P(\ge 16) = 1 - P(\le 15) = 1 - 0.9513$	M1		Seek biggest prob < 0.05, e.g. 0.0835 or 0.0166,
r p					allow 0.0293 but no other LH tail
the		Probability 0.0487	A1		Answer in range [0.0487, 0.0488], cwd, cwo
i ei	(iii)	$H_0: \lambda = 10 \text{ or } 2 \text{ [or } \mu$]	B2		Hypotheses fully correct allow λ or μ
l ir	()	H_{1} : $\lambda > 10 \text{ or } 2$ [or μ]	22		[SP: one error B1 but r or R or r or \overline{x} : B0]
lec		$\Pi_1 \cdot \mathcal{N} > \Pi \cup \Pi_2 [01 \ \mu]$	Δ1		[5K. one choi, bi, but i on K of X of X. bo]
arc		$\alpha: P(\ge 14) = 1 - 0.8645 = 0.1355$			$p \in [0.135, 0.136]$ from Po(10)
aw		> 0.05	ы		Compare explicitly with 0.05 or 0.0487
e e		β : Critical region $r \ge 16$, $p = 0.0487$	A1√		$\sqrt{10}$ on answer from (ii)
n þ		Compare $r = 14$	B1√		
ca		Do not reject H_0 [can be implied]	M1		Method correct \sqrt{n} must be upper tail and ">"
cks		Insufficient evidence of an increase in	A 1 1	10	Conclusion interpreted in context
Лаı		the number of dronned catches	AIV	10	Conclusion interpreted in context $(SD, D(z, 14) = 0.0165 < 0.05, (D2 M1) = 0.0165$
~		the number of dropped catches			$[SK: P(\ge 14) = 0.9103 < 0.93; (B2 MI) A0 B1 M0A0;$
					same for $P(> 14)$ or $P(= 14)$]
0	(1)		Da		[SK: N(10,10): (11) 0.05 M0. (111) (B2) M1 A0 B1 M0A0]
8	(1)	$H_0: p = 0.4$ or $\mu = 4.8$	B 2		Both fully correct, B2.
		$H_1: p > 0.4$ or $\mu > 4.8$			[SR: one error, B1, but x or R or r or \overline{x} : B0]
		B(12, 0.4)	M1		B(12, 0.4) stated or implied, e.g. 0.9972 or 0.9847
		$P(\geq 9) = 1 - 0.9847 = 0.0153$	A1		Or: CR is ≥ 9 and $p \in [0.015, 0.0153]$
					Explicitly compare with 0.05 or 9 with $> 9 \sqrt{0}$
		Rojoct H. [can be implied]			Explicitly compare with 0.05, or \mathcal{I} with \mathcal{I} \mathcal{I} , \mathcal{I} on probability must be "\"
		Significant suidenes of increases in	IVI I	_	Reject Π_0 , v on probability, must be \geq
		Significant evidence of increase in	A1√	7	Conclusion interpreted in context
		proportion of audience members who			[SR: $P(\le 9)$ or $P(= 9)$ or $P(> 9)$: (B2 M1) A0 B1 M0A0]
		know sponsor's name			[SR: N(4.8, 2.88): (B2) M1 A0 B0 M0A0]
	(ii)	N(160, 96)	B1		Normal, mean 160
			B1		Variance (or SD) 96 [96/400: B2M0]
		(x-0.5)-160 - 1.645	M1		Standardise unknown with <i>nn</i> and \sqrt{nna} or <i>nna</i> &
		$\frac{1}{\sqrt{06}} = 1.075$	A1		equate to Φ^{-1} : $\sqrt{96}$ and signs correct ignore as
		·γ 20	B1		$\nabla T = 1.645$
		Solve to find $r [-176.6]$	M		$N\Pi S = 1.043$
		Minimum volum in 177		_	Solve [implied by 17/ or 176.6 or 176.1]
		winninum value is 1//	AI	1	177 only, from 176.6, CWO [cc error: 6 ex 7]

1		$U \sim B(800, 0.005) \approx Po(4)$	B1		Po(<i>nn</i>) stated or implied
-		D(U < 6)	M1		Tables or formula ± 1 term e.g. 0.7851 0.9480 0.1107 not 1
		-0.9903			Answer 0 880 or a r t $= 0.8803$
		= 0.0893	R1	1	Allswei 0.887 01 a.l.t. 0.8875
•		n > 30/1 arge, np < 3/p small	M	-	
2		$\frac{23.625 - 23}{5} = 2$	MI		Standardise with \sqrt{n} , allow \sqrt{n} errors
		$5/\sqrt{n}$	AI		Equate to 2 or a.r.t. 2.00, signs correct
		$\sqrt{n} = 16$	M1		Solve for \sqrt{n} , needs Φ^{-1} , <i>not</i> from $/n$
		<i>n</i> = 256	A1	4	256 only, allow from wrong signs
3	(i)	(a) $e^{-0.42}$	M1		Correct formula for $R = 0$ or 1
		= 0.657	A1		P(0), a.r.t. 0.657
		(b) 0.42 $e^{-0.42} = 0.276$	A1	3	P(1). a.r.t. 0.276
	(ii)	$P_0(2, 1)^{\circ}$	M1		Po(2, 1) stated or implied
	(11)	1 P(< 3) - 1 0 8386	M1		Tables or formula $e = 0.8386$ or 0.6496 or 0.9379 or
		$1 - 1 (\le 5) = 1 - 0.8580$ - 0.1614		3	complement: Answer in range $[0.161, 0.162]$
	(:::)	- 0.1014	D2	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	At loss 2 separate here, all decreasing
	(III)		D2	2	At least 5 separate bars, an decreasing
					Allow histogram. Allow convex
					P(0) < P(1) but otherwise UK: B1
					Curve: BI
					[no hint of normal allowed]
4	(i)	H : n = 0.14	P)		Doth correct 1 error \mathbf{P}_1 but \mathbf{x} or \mathbf{y} or $-$ etc. 0
4	(1)	$H_0 \cdot p = 0.14$	D2		Bour correct. I error, B1, but x of 7 or x etc. 0
		$H_1 \cdot p < 0.14$	MI		$\mathbf{D}(22, 0, 1, 4)$ (1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1
		B(22, 0.14) B(22, 0.14)			B(22, 0.14) stated or implied, e.g. $N(3.08, 2.6488)$ or $PO(3.08)$
		$P(\le 2) = .86^{-1} + (22 \times .86^{-1} \times .14) +$			Correct formula for 2 or 3 terms, or $P(\le 0) = 0.036$ and CR
		$(231 \times .86^{20} \times .14^{2}) = 0.3877$	AI		Correct answer, a.r.t. 0.388, or CR is $= 0$
		> 0.1	BI		Explicitly compare 0.1 or CR with 2, OK from Po but <i>not</i> from N
		Do not reject H_0 . Insufficient	MI		Correct comparison type and conclusion, needs binomial, at least
		evidence that company			2 terms, <i>not</i> from $P(<2)$
		overestimates viewing proportion	A1	8	Contextualised, some acknowledgement of uncertainty
					[SR: Normal: B2 M1 A0 B0 M0]
					[SR: 2-tailed, or $p > 0.14$, P(≥ 2): B1M1A2B0M1A1]
	(ii)	Selected independently	B1		Independent selection
		Each adult equally likely to be	B1	2	Choice of sample elements equally likely (no credit if not
		chosen			focussed on selection)
					[Only "All samples of size <i>n</i> equally likely": B1 only unless
					related to Binomial conditions]
5	(i)	1 []	B1		Horizontal straight line
	. /		B1		Symmetrical U-shaped curve
			B1	3	Both correct, including relationship between the two and not
			21	C	extending beyond $[-2, 2]$ curve through (0.0)
	(ii)	S is equally likely to take any	B2	2	Correct statement about both distributions $\sqrt{100}$ on their graph
	()	value		-	[Correct for one only or partial description: B1]
		T is more likely at extremities			Not "probability of S is constant" etc
	(iji)		M1		Integrate $r^2 \sigma(x)$ limits -2 2
	(111)	$\int_{-\frac{5}{2}}^{2} r^{6} dr - \frac{5}{2} \left \frac{x'}{x} \right ^{-1} \left -\frac{20}{20} \right $			Correct indefinite integral $[-5r^{7}/448]$
		$\begin{vmatrix} 64 \\ J_{-2} \end{vmatrix} = \begin{vmatrix} 64 \\ 7 \end{vmatrix} = \begin{vmatrix} -7 \\ 7 \end{vmatrix}$	R1		Context indefinite integral $[-3\lambda/440]$ 0 or 0^2 subtracted or $\mathbf{E}(\mathbf{V}) = 0$ scap weth $\frac{1}{2}f(x)dx = \left[xf(x)dx\right]^2$
		0^2	DI		U OF U SUDIFACIED OF $E(X) = U$ seen, <i>not</i> $Jx I(x)dx - JxI(x)dx$
		-0 -20	A 1	4	Answer $\frac{20}{7}$ or $2\frac{6}{7}$ or a.r.t. 2.86, don't need 0
		$-\frac{20}{7}$	AI	4	/
1		· ·	1		

6	(i)	20.25 50.000	M1		$50.0 \pm z\sqrt{(1.96/81)}$, allow one sign only, allow $\sqrt{\text{errors}}$
	.,	$50.0 \pm 1.96 \sqrt{\frac{20.25}{81}} = 50.0 \pm 0.98$	B1		z = 1.96 in equation (<i>not</i> just stated)
		=49.02,50.98	A 1 A 1		Both critical values, min 4 SF at some stage (if both 3SF, A1)
		$\overline{W} < 49.02$ and $\overline{W} > 50.98$	$\Lambda 1 $	5	CR, allow $\leq \geq$, don't need \overline{W} , $$ on their CVs, can't recover
		W < 19.02 and W > 50.90		5	[Ans 50 ± 0.98 : A1 only]
					[SR: 1 tail, M1B0A0; 50.8225 or 49. 1775: A1]
	(ii)	50.98 - 50.2 - 1.56	M1		Standardise one limit with same SD as in (i)
		0.5	A1		A.r.t. 1.56, allow – Can allow $$ here
		49.02 - 50.2	A1		A.r.t. –2.36, allow + J if very unfair
		= -2.50	M1	-	Correct handling of tails for Type II error
		$\Phi(1.56) - \Phi(-2.36) = 0.9315$	AI	5	Answer in range [0.931, 0.932]
					[SR 1-tail M1; –1.245 or 2.045 A1; 0.893 or 0.9795 A1]
	(111)	It would get smaller	BI	1	No reason needed, but withhold if definitely wrong reason seen.
7	(*)	^ <u>-</u> 10.7	D1		Allow from 1-tail
/	(1)	$\mu = t = 13.7$	Ы M1		15.7 stated
		$\frac{12657.28}{12657.28} - 13.7^2$ [=10.08]; $\times \frac{64}{12}$			correct formula for blased estimate
		64	MI		$\times \frac{1}{63}$ used, or equivalent, can come in later
		= 10.24	A1		Variance or SD 10.24 or 10.2
		$H_0: \mu = 13.1, H_1: \mu > 13.1$	B2		Both correct.
		$\underline{13.7 - 13.1}_{=} = 1.5 \text{ or } p = 0.0668$			[SR: One error, B1, but x or t or x or t, 0]
		$\sqrt{10.24/64}$	M1		Standardise, or find CV, with $\sqrt{64}$ or 64
		1.5 < 1.645 or $0.0668 > 0.05$	Al D1		$z = a.r.t. 1.50, \text{ or } p = 0.0668, \text{ or } \mathbb{CV} 13.758 [\vee 0 \text{ or } z]$
		1.5 < 1.045 01 0.0000 > 0.05	ы		Compare z & 1.645, or $p \approx 0.05$ (must be correct tail),
		Do not reject H_0 . Insufficient	M1		$\zeta = 1.045 \approx 15$ with $\zeta = 1.045 \approx 15$ with $\zeta = 13.7$
		evidence that time taken on	A1	11	Contextualised some acknowledgement of uncertainty
		average is greater than 13.1 min			[13.1 - 13.7; (6), M1 A0 B1 M0]
	(ii)	Yes, not told that dist is normal	B1	1	Equivalent statement, <i>not</i> " <i>n</i> is large", don't need "yes"
8	(i)	N(14.7, 4.41)	M1		Normal, attempt at <i>np</i>
		Valid because	A1		Both parameters correct
		np = 14.7 > 5; nq = 6.3 > 5	B1		Check $np > 5$; If both asserted but not both
		$\Phi(15.5-14.7) = 1 - \Phi(0.381)$	B1		nq or npq > 5 J 14.7 and 6.3 seen: B1 only
		$1-\Psi\left(\frac{1}{\sqrt{4.41}}\right)$			[Allow " <i>n</i> large, <i>p</i> close to $\frac{1}{2}$ "]
		= 1 - 0.6484	MI		Standardise, answer < 0.5, no \sqrt{n}
		= 0.3516		7	z, a.r.t. 0.381
	· · · · · ·		AI		Answer in range [0.351, 0.352] [Exact: M0]
	(II)	$K \sim N(14.7, 4.41/36)$			Normal, their np from (1)
		[= N(14.7, 0.55)] Valid by Control Limit Theorem	AIV D1		Particle Valiance/50 Particle CLT or large $n (= 36, not 21)$ or " $K_{\rm er}$ N so $\overline{K}_{\rm er}$ N"
		as 36 is large	DI		not same as (i) not $np > 5$ $na > 5$ for \overline{K}
		$(14.0 + \frac{1}{2} - 14.7)$ (1.00)	M1		Standardise 14.0 with 36 or $\sqrt{36}$
		$\Phi \left[\frac{1}{\sqrt{4}} \frac{1}{\sqrt{4}} \frac{1}{\sqrt{26}} \right] = \Phi(-1.96)$	A1		cc included, allow 0.5 here, e.g. $14.5 - 14.7$
		$\sqrt{\sqrt{4.41/30}}$	A1		z = -1.96 or -2.00 or -2.04 , allow + if answer < 0.5
		= 0.025	A1	7	0.025 or 0.0228
					[0.284 loses last 2] [Po(25.2) etc: probably 0]
	OR:	$B(756, 0.7) \approx N(529.2, 158.76)$	M1M1	A1	×36; N(529.6,); 158.76
		$(504.5 - 529.2) = \Phi(-1.96)$	B1		CLT as above, or $np > 5$, $nq > 5$, can be asserted here
		$\Psi\left[\frac{1}{\sqrt{158.76}}\right]^{-\Psi(-1.50)}$	MI		Standardise 14×36
		- 0.025	AI		cc correct and \sqrt{npq}
		- 0.043	AI		0.025 or 0.0228

4733

1	$\frac{105.0 - \mu}{\sigma} = -0.7; \frac{110.0 - \mu}{\sigma} = -0.5$ Solve: $\sigma = 25$ $\mu = 122.5$	M1 A1 B1 M1 A1 A1	6	Standardise once, equate to Φ^{-1} , allow σ^2 Both correct including signs & σ , no cc (continuity correction), allow wrong z Both correct z-values. "1 –" errors: M1A0B1 Get either μ or σ by solving simultaneously σ a.r.t. 25.0 $\mu = 122.5 \pm 0.3$ or 123 if clearly correct, allow from σ^2 but <i>not</i> from $\sigma = -25$.
2	Po(20) ≈ N(20, 20) Normal approx. valid as $\lambda > 15$ $1-\Phi\left(\frac{24.5-20}{\sqrt{20}}\right) = 1-\Phi(1.006)$ = 1 - 0.8427 = 0.1573	M1 A1 B1 M1 A1 A1	6	Normal stated or implied (20, 20) or (20, $\sqrt{20}$) or (20, 20^2), can be implied "Valid as $\lambda > 15$ ", <i>or</i> "valid as λ large" Standardise 25, allow wrong or no cc, $\sqrt{20}$ errors $1.0 < z \le 1.01$ Final answer, art 0.157
3	H ₀ : $p = 0.6$, H ₁ : $p < 0.6$ where p is proportion in population who believe it's good value $R \sim B(12, 0.6)$ α : P($R \le 4$) = 0.0573 > 0.05	B2 M1 A1 B1		Both, B2. Allow π , % One error, B1, except <i>x</i> or \overline{x} or <i>r</i> or <i>R</i> : 0 B(12, 0.6) stated or implied, e.g. N(7.2, 2.88) Not P(< 4) or P(\geq 4) or P(= 4) Must be using P(\leq 4), or P(> 4) < 0.95 and binomial Must be using CR: explicit comparison needed
	p: $p = 0.0153$ Do not reject H ₀ . Insufficient evidence that the proportion who believe it's good value for money is less than 0.6	A1 M1 A1	7	Correct conclusion, needs B(12,0.6) and ≤ 4 Contextualised, some indication of uncertainty [SR: N(7.2,) or Po(7.2): poss B2 M1A0] [SR: P(<4) or P(=4) or P(≥ 4): B2 M1A0]
4 (i)	Eg "not all are residents"; "only those in street asked"	B1 B1	2	One valid relevant reason A definitely different valid relevant reason <i>Not</i> "not a random sample", <i>not</i> "takes too long"
(ii)	Obtain list of whole population Number it sequentially Select using random numbers [Ignore method of making contact]	B1 B1 B1	3	"Everyone" or "all houses" must be implied <i>Not</i> "number it with random numbers" unless then "arrange in order of random numbers" SR : "Take a random sample": B1 SR : Systematic: B1 B0, B1 if start randomly chosen
(iii)	Two of: α : Members of population equally likely to be chosen β : Chosen independently/randomly γ : Large sample (e.g. > 30)	B1 B1	2	One reason. NB : If "independent", must be "chosen" independently, not "views are independent" Another reason. Allow "fixed sample size" but not both that and "large sample". Allow "houses"

5	(i)	Bricks scattered at constant average rate & independently of one another	B1 B1	2	B1 for each of 2 different reasons, in context. (Treat "randomly" ≡ "singly" ≡ "independently")
	(ii)	Po(12) $P(\le 14) - P(\le 7)$ [= .77200895] [or P(8) + P(9) + + P(14)]	B1 M1		Po(12) stated or implied Allow one out at either end or both, eg 0.617, or wrong column, but <i>not</i> from Po(3) nor, eg, .9105 – .7720
		= 0.6825	A1	3	Answer in range [0.682, 0.683]
	(iii)	$e^{-\lambda} = 0.4$ $\lambda = -\ln (0.4)$ = 0.9163 Volume = 0.9163 ÷ 3 = 0.305	B1 M1 A1 M1	4	This equation, aef, can be implied by, eg 0.9 Take ln, or 0.91 by T & I λ art 0.916 or 0.92, can be implied Divide their λ value by 3 [SR : Tables, eg 0.9÷3: B1 M0 A0 M1]
6	(i)	$33.6 \\ \frac{115782.84}{100} - 33.6^{2} \ [= 28.8684] \\ \times \frac{100}{99} = 29.16$	B1 M1 M1 A1	4	33.6 clearly stated [not recoverable later] Correct formula used for biased estimate $\times \frac{100}{99}$, M's independent. Eg $\frac{\Sigma r^2}{99}$ [-33.6 ²] SR B1 variance in range [29.1, 29.2]
	(ii)	$\overline{R} \sim N(33.6, 29.16/9) = N(33.6, 1.8^2)$	M1 A1		Normal, their μ , stated or implied Variance [their (i)]÷9 [not ÷100]
		$1 - \Phi\left(\frac{32 - 53.6}{\sqrt{3.24}}\right) \left[= \Phi(0.8889)\right]$	M1		Standardise & use Φ , 9 used, answer > 0.5, allow $\sqrt{\text{errors}}$, allow cc 0.05 but <i>not</i> 0.5
		= 0.8130	A1	4	Answer, art 0.813
	(iii)	No, distribution of <i>R</i> is normal so that of \overline{R} is normal	B2	2	Must be saying this. Eg "9 is not large enough": B0. Both: B1 max, unless saying that <i>n</i> is irrelevant.
7	(i)	$\frac{\frac{2}{9}\int_{0}^{3}x^{3}(3-x)dx = \frac{2}{9}\left[\frac{3x^{4}}{4} - \frac{x^{5}}{5}\right]_{0}^{3} [= 2.7] - \frac{11}{9}\left[\frac{3x^{2}}{4} - \frac{x^{5}}{5}\right]_{0}^{3} [= 2.7] - \frac{3}{9}\left[\frac{3x^{4}}{4} - \frac{x^{5}}{5}\right]_{0}^{3} [= 2.7]$	M1 A1 B1		Integrate $x^2 f(x)$ from 0 to 3 [not for µ]Correct indefinite integralMean is 1½, soi[not recoverable later]
		$(1/2) = \frac{1}{20}$ or 0.45	A1	5	Subtract their μ^2 Answer art 0.450
	(ii)	$(172) = \frac{1}{20} \text{ or } 0.45$ $= \frac{1}{20} \int_{0}^{0.5} x(3-x) dx = \frac{2}{9} \left[\frac{3x^2}{2} - \frac{x^3}{3} \right]_{0}^{0.5}$ $= \frac{2}{27} \text{ AG}$	M1 A1 M1 A1	5	Subtract their μ^2 Answer art 0.450 Integrate f(x) between 0, 0.5, must be seen somewhere Correctly obtain given answer $\frac{2}{27}$, decimals other than 0.5 not allowed, 1 more line needed (eg [] = $\frac{1}{3}$)
	(ii) (iii)	$(172) = \frac{1}{20} \text{ or } 0.45$ $= \frac{1}{20} \int_{0}^{0.5} x(3-x) dx = \frac{2}{9} \left[\frac{3x^2}{2} - \frac{x^3}{3} \right]_{0}^{0.5}$ $= \frac{2}{27} \text{ AG}$ $B(108, \frac{2}{27})$	MI A1 M1 A1 B1	5	Subtract their μ^2 Answer art 0.450 Integrate f(x) between 0, 0.5, must be seen somewhere Correctly obtain given answer $\frac{2}{27}$, decimals other than 0.5 not allowed, 1 more line needed (eg [] = $\frac{1}{3}$) B(108, $\frac{2}{27}$) seen or implied, eg Po(8)
	(ii) (iii)	$(142) = \frac{1}{20} \text{ or } 0.45$ $= \frac{1}{20} \text{ or } 0.45$ $= \frac{1}{20} \int_{0}^{0.5} x(3-x) dx = \frac{2}{9} \left[\frac{3x^{2}}{2} - \frac{x^{3}}{3} \right]_{0}^{0.5}$ $= \frac{2}{27} \text{ AG}$ $= \frac{2}{27} \text{ AG}$ $= \frac{1}{27} (9.5 - 8)$ $= 1 - \Phi \left(\frac{9.5 - 8}{\sqrt{7.4074}} \right)$ $= 1 - \Phi (0.5511)$	M1 A1 A1 B1 M1 A1 M1 A1 M1	5	Subtract their μ^2 Answer art 0.450 Integrate f(x) between 0, 0.5, must be seen somewhere Correctly obtain given answer $\frac{2}{27}$, decimals other than 0.5 not allowed, 1 more line needed (eg [] = $\frac{1}{3}$) B(108, $\frac{2}{27}$) seen or implied, eg Po(8) Normal, mean 8 variance (or SD) 200/27 or art 7.41 Standardise 10, allow $$ errors, wrong or no cc, needs to be using B(108,)

	(iv)	$\overline{X} \sim N(1.5, \frac{1}{240})$	$ \begin{array}{c} B1 \\ B1 \\ M \\ B1 \\ \end{array} $	NormalNB: not part (iii)Mean their μ Variance or SD (their 0.45)/108 [not (8, 50/729)]
8	(i)	$H_0: \mu = 78.0$ $H_1: \mu \neq 78.0$ $z = \frac{76.4 - 78.0}{\sqrt{68.9/120}} = -2.1115$ $> -2.576 \text{ or } 0.0173 > 0.005$ $78 \pm z \sqrt{(68.9/120)}$ $= 76.048$ $76.4 > 76.048$	B1 B1 M1 A1 B1 M1 A1√ B1	Both correct, B2. One error, B1, but x or \overline{x} : B0. Needs $\pm (76.4 - 78)/\sqrt{(\sigma \div 120)}$, allow $\sqrt{\text{errors}}$ art -2.11, or $p = 0.0173 \pm 0.0002$ Compare z with (-)2.576, or p with 0.005 Needs 78 and 120, can be - only Correct CV to 3 sf, $\sqrt{\text{ on } z}$ $z = 2.576$ and compare 76.4, allow from 78 \leftrightarrow 76.4
		Do not reject H_0 . Insufficient evidence that the mean time has changed	M1 A1√ 7	Correct comparison & conclusion, needs 120, "like with like", correct tail, \bar{x} and μ right way round Contextualised, some indication of uncertainty
	(ii)	$\frac{1}{\sqrt{68.9/n}} > 2.576$ $\sqrt{n} > 21.38,$ $n_{\min} = 458$ Variance is estimated	M1 M1 A1 B1 4	IGNORE INEQUALITIES THROUGHOUT Standardise 1 with <i>n</i> and 2.576, allow $\sqrt{\text{errors}}$, cc etc but <i>not</i> 2.326 Correct method to solve for \sqrt{n} (<i>not</i> from <i>n</i>) 458 only (<i>not</i> 457), <i>or</i> 373 from 2.326, signs correct Equivalent statement, allow "should use <i>t</i> ". In principle nothing superfluous, but "variance stays same" B1 bod

Specimen Answers

Questio	on 4: Part (i)	
α	Takes too long/too slow	B0
β	Interviewing people in the street isn't a random sample	B 0
γ	Many tourists so not representative	B1
δ	Those who don't shop won't have their views considered	B1
3	Interviewers biased as to who they ask	B1
ζ	Views influenced by views of others	B 1
Part (ii)		
α	Choose a random sample of the town and ask their opinion	B1
β	Choose names at random from the town's phone book	B1
γ	A random number machine determines which house numbers should be used, and every street should have the same proportion of residents interviewed	B0B0B1

	every sheet should have the sume proportion of residents interviewed	
δ	Visit everyone door to door and give them a questionnaire	B1B0B0
3	Assign everyone a number and select randomly	B1B0B0
ζ	Assign everyone a number and select using random numbers	B1B0B1
η	Ditto + "ignoring numbers that don't correspond to a resident"	B1B1B1
θ	Assign each eligible person a number and pick numbers from a hat	B1B1B0
l	Put names of all residents into a hat and pick them out	B1B1B0
	[NP: postal survey is biased]	

[11] postal survey is blased	[N	NB : 1	postal	survey	is	biased
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Part (iii)		
α	One person's view should not affect another's	B0
β	It is without bias	B0
γ	Results occur randomly	B 0
δ	Should be asked if they are for or against (binomial testing)	B 0
3	It will survey a diverse group from different areas so should be representative	B 0
ζ	Everyone's should be chose independently of everyone else	B1
η	The sample size must be large	B1
θ	Participants are chosen at random and independently from one another	B1 only
	[though $\eta \& \theta$ together would get B2]	

Question 5 (i)

Number of bricks must always be the same	H	30			
Results occur randomly					
The chance of a brick being in one place is always the same	H	30			
Events must occur independently and at constant average rate	H	30			
They must occur independently and at constant average rate	H	31 only			
Bricks' locations must be random and independent [effectiv	ely the same] B	31 only			
Only one brick in any one place; bricks independent [effectiv	ely the same] E	B1 only			
	Number of bricks must always be the sameResults occur randomlyThe chance of a brick being in one place is always the sameEvents must occur independently and at constant average rateThey must occur independently and at constant average rateBricks' locations must be random and independent[effective]Only one brick in any one place; bricks independent	Number of bricks must always be the sameHResults occur randomlyHThe chance of a brick being in one place is always the sameHEvents must occur independently and at constant average rateHThey must occur independently and at constant average rateHBricks' locations must be random and independent[effectively the same]Only one brick in any one place; bricks independent[effectively the same]			

Penalise over-specified answers (> 6 SF) first time but only once per paper. Use Or Oto annotate "over-assertive" or "no context" respectively

1		$\hat{\mu} = \bar{x} = 15.16$	B1		15.16 or 15.2 as answer only
		$\hat{\sigma}^2 = \frac{5}{4}s^2$	M1		Use $\frac{\Sigma x^2}{5} - \bar{x}^2$ [=1.0904]
			M1		Multiply by 5/4, or equiv for single formula
		= 1.363	A1	4	Final answer 1.36 or 1.363 only, not isw
2	(i)	Not all equally likely – those in	M1		Not all equally likely stated or implied
		range 0 to 199 more likely to be	A1	2	Justified by reference to numbers, no
		chosen			spurious reasons
	(ii)	Ignore random numbers greater	B 1	1	Any valid resolution of this problem, no
		than 799, or 399	2.64		spurious reasons
3		$B(60, 0.35) \approx N(21, 13.65)$	Ml		B(60, 0.35) stated or implied
		$\Phi(18.5-21) = \Phi(-0.6767)$	MI		N(21,)
		$\Phi\left(\frac{1}{\sqrt{13.65}}\right)$	Al		Variance or $SD = 13.65$
		= 1 - 0.7507	MI		Standardise, their np and $\forall npq$ or npq ,
		-1 0.7507	A 1		wrong or no cc
				6	Both \sqrt{npq} and cc correct
		= 0.2493	AI	0	Answer, a.r.t. 0.249
4		$H_0: \mu = 60; H_1: \mu < 60$	B2		Both correct, B2
		(α) $z = \frac{58.9 - 60}{2} = -1.967$			B1 for one error, but not x, t, \overline{x} or t
		$\sqrt{5^2}$ / 80	MI		Standardise 58.9 & $\sqrt{80}$, allow – or $\sqrt{100}$ errors
			Al		<i>z</i> , art –1.97 or <i>p</i> in range [0.024, 0.025]
		<-1.645	BI		Explicit comparison with -1.645 or 0.05, or
	or	5	M1		+1.043 of 0.93 II 1.907 of 0.970 used
	07.	$(p)_c = 60 - 1.645 \times \frac{3}{\sqrt{80}} = 59.08$	B1		$-2 \times 5/700$, any $z = \Phi^2$, anow 7 errors of + not just $\pm z = 1.645$ and compare 58.0
		58.9 < 59.08	A1		1, not just +, z = 1.045 and compare 50.5
		Reject H _o	M1		Correct first conclusion needs essentially
			1011		correct method including $\sqrt{80}$ or 80
		Significant evidence that people	A1	7	Contextualised uncertainty acknowledged
		underestimate time			$SR^{2} \mu = 58.9^{\circ} B0M1A0B1 max 2/7$
					SR: 2-tail: max 5/7
5	(i)	$H_0: \lambda = 11.0$	B2		Allow μ . Both correct, B2
		$H_1: \lambda > 11.0$			One error: B1, but not C , x etc
		(α) P(≥ 19) = 1 – 0.9823	M1		Find $P(\ge 19)$ [or $P(< 19)$ if later 0.95]
		= 0.0177	A1		art 0.0177 [0.9823, ditto]
		< 0.05	B1		Compare 0.05 [0.95 if consistent], needs
					M1
		$(\beta) \qquad CR \ge 18,$	M1		CR or CV 16/17/18/19 stated or clearly
					implied, but not <
		$P(\ge 18) = 0.0322$	A1		18 and 0.0322 both seen, allow 0.9678
		19 > 18	BI		Explicit comparison with 19, needs M1
		Reject H ₀	M1		Needs essentially correct method &
		Significant evidence of an	A1.	7	Contextualised uncertainty acknowledged
		increase in number of customers	111*	,	SR: Normal or $P(-19)$ or $P(< 19)$ or
		mercuse in number of customers			P(> 19) First R ² only
	(ii)	Can't deduce cause-and-effect or	B1	1	Conclusion needed No spurious reasons
	()	there may be other factors		*	If "DNR" in (i). "couldn't deduce even
					if"

6	(i)	(a) Probabilities don't total 1	B1	1	Equivalent statement
		(b) $P(>70)$ must be $< P(>50)$	B1	1	Equivalent statement
		(c) $P(>50) = 0.3 \implies \mu < 50$	B1	1	Any relevant valid statement, e.g. " $P(< 50)$
		$P(<70) = 0.3 \Rightarrow \mu > 70$			= 0.7 but P(< 50) must be < P(< 70)"
	(ii)	$\mu = 60$ by symmetry	B1		$\mu = 60$ obtained at any point, allow from Φ
		$10 - \Phi^{-1}(0,7) = 0.524(4)$	M1		One standardisation, equate to Φ^{-1} , not
		$\frac{-}{\sigma} = \Phi^{-}(0.7) = 0.324(4)$			0.758
		$\sigma = 10/0.5243$	B1		$\Phi^{-1} \in [0.524, 0.5245]$ seen
		= 19.084	A1	4	σ in range [19.07, 19.1], e.g. 19.073
7	(i)	A	M1		Horizontal line
	. ,		A1	2	Evidence of truncation
]			[no need for labels]
		5 11			-
		5 11			
	(ii)	$\mu = 8$	B1		8 only, cwd
		$\int_{1}^{11} t^2 dt = \begin{bmatrix} 1 & t^3 \end{bmatrix}^{11} [-67]$	M1		Attempt $\int kt^2 dt$, limits 5 and 11 seen
		$\int_{5}^{5} \frac{1}{6} i a a - \left[\frac{1}{18} i \right]_{5} [-07]$	B1		k = 1/6 stated or implied
		-8^{2}	M1		Subtract their (non-zero) mean ²
		= 3	A1	5	Answer 3 only, <i>not</i> from MF1
	(iii)	N(8, 3/48)	M1		Normal stated or implied
		$(8.3-8) = 1 \Phi(1.2)$	A1		Mean 8
		$1-\Phi\left(\frac{1}{\sqrt{3/48}}\right)^{-1}-\Phi(1.2)$	A1		Variance their (non-zero) (ii)/48
		-1 - 0.8848	M1		Standardise, \sqrt{n} , ignore sign or $\sqrt{1}$ errors. cc:
		- 1 0.0040			M0
		= 0.1151	A1		Answer, art 0.115
		Normal distribution only approx.	B1	6	Any equivalent comment, e.g. CLT used
8	(i)	$P(\le 4) = 0.0473$	M1		$P(\le r)$ from B(10, 0.7), $r = 3/4/5$, not N
		Therefore CR is ≤ 4	B1		"≤ 4" stated, not just "4", nothing else
		P(Type I error) = 4.73%	A1	3	Answer, art 0.0473 or 4.73%, must be stated
	(ii)	B(10, 0.4) and find P(> 4)	M1		Must be this, <i>not</i> isw, \checkmark on (i)
		$1 - P(\leq 4)$	M1		Allow for 0.6177 or 0.1622
		= 0.3669	A1	3	Answer, art 0.367
	(iii)	0.5×0.3669	M1		$0.5 \times (\mathbf{ii})$
		= 0.18345	A1	2	Ans correct to 3 SF, e.g. 0.184 from 0.367

9	(i)	$1 - P(\le 7) = 1 - 0.9881$	M1		Allow for 0.0038 or 0.0335
		= 0.0119	A1	2	Answer, a.r.t. 0.0119
	(ii)	Po(12)	M1		Po(12) stated or implied
		$P(\le 14) - P(\le 12)$	M1		Formula, 2 consecutive correct terms, or
		[0.7720 - 0.5760]			tables, e.g0905 or .3104 or .1629
		= 0.196	A1	3	Answer, art 0.196
	(iii)	$Po(60) \approx N(60, 60)$	M1		N(60,)
			A1		Variance or SD 60
		$\Phi(69.5-60) - \Phi(1.226)$	M1		Standardise, $\lambda \& \sqrt{\lambda}$, allow λ or wrong or no
		$\Phi\left(\frac{1}{\sqrt{60}}\right) = \Phi(1.220)$			сс
			A1		$\sqrt{\lambda}$ and cc both correct
		= 0.8899	A1	5	Answer 0.89 or a.r.t. 0.890
	(iv)	(a) $1 - e^{-3m}(1 + 3m)$	M1		M1 for one error, e.g. no "1 –", or extra term,
			A1	2	or 0 th term missing; answer, aesf
		(b) $m = 1.29$,	M1		Substitute 1.29 or 1.3 into appropriate fn
		p = 0.89842	A1		Comp 0.9 0.1 0
		m = 1.3, p = 0.9008	A1		1.29 0.898 0.1015800158
					1.3 0.901 0.09918 .0008146
		Straddles 0.9, therefore solution	Δ1	4	Explicit comparison with relevant value, &
		between 1.29 and 1.3	ΠΙ	-	conclusion, needs both ps correct
	or	Method for iteration; 1.296	M1A1		Can be implied by at least 1.296
		1.2965or better; conclusion	A1A1		Need at least 4 dp for M1A2
		stated			_

1	(i)(a)	$1 - P(\le 6) = 1 - 0.8675$	M1		1 – .9361 or 1 – .8786 or 1 – .8558: M19721: M0
		= 0.1325	A1	2	Or 0.132 or 0.133
	(b)	Po(0.42)	M1		Po(0.42) stated or implied
		$_{-0.42}$ 0.42 ² = 0.05795	M1		Correct formula, any numerical λ
		$e - \frac{1}{2!}$	A1	3	Answer, art 0.058. Interpolation in tables: M1B2
	(ii)	E.g. "Contagious so incidences do	B2	2	Contextualised reason, referred to conditions: B2. No
		not occur independently", or "more			marks for mere learnt phrases or spurious reasons, e.g.
		cases in winter so not at constant			not just "independently, singly and constant average
		average rate"			rate". See notes.
2	(i)	B(10, 0.35)	M1		B(10, 0.35) stated or implied
		P(< 3)	M1		Tables used, e.g. 0.5138 or 0.3373, or formula ± 1 term
		= 0.2616	A1	3	Answer 0.2616 or better or 0.262 only
	(ii)	Binomial requires being chosen	B2	2	Focus on "Without replacement" negating independence
		independently, which this is not, but			condition. It doesn't negate "constant probability"
		unimportant as population is large			condition but can allow B1 if "selected". See notes
3	(i)	$(32-40) = \Phi^{-1}(0,2) = -0.842$	M1		Standardise and equate to Φ^{-1} , allow "1 –" errors, σ^2 , cc
	. /	$\left(\frac{-\sigma}{\sigma}\right)^{-\frac{1}{2}}$ (0.2) = 0.012	B1		0.842 seen
		$\sigma = 95[06]$	A1	3	Answer, 9.5 or in range [9.50, 9.51], c.w.o.
	(ii)	B(90, 0, 2)	R1		B(90, 0, 2) stated or implied
	(11)	$\sim N(18, 14, 4)$	M1		N their nn
		$\sim 10(10, 14.4)$	A1		variance their nna allow $\sqrt{\text{errors}}$
		$1-\Phi\left(\frac{19.5-18}{2}\right) = 1-\Phi(0.3953)$	M1		Standardise with np and npq , allow \sqrt{chois}
		(14.4)	A1		Standardise with np and npq , and v , cc errors, e.g.
		= 1 - 0.6537 = 0.3463	Al	6	1.590, .440, .450, .460, .472, NPq and cc confectAnswer a r.t. 0.246 [NP: 0.2401 from Do: 1/6]
4		$\mathbf{H} \cdot \mathbf{n} = 0.4$	D1	v	Allswer, a.r.t. 0.540 [ND: 0.5491 from PO: 1/0]
4		$H_0: p = 0.4,$ $H_1: p > 0.4$	B1		Fully correct, B2. Allow π . p omitted or μ used in boin,
		R = B(16, 0.4)	M1		OI > WIOHg. BI OHHy. x OI x OI 0.4 etc. BOD(16, 0, 4) stated an implied allow N(6, 4, 2, 94)
	(α)	P(P > 11) = 0.0101			B(10, 0.4) stated of implied, allow $N(0.4, 5.84)$
	(α)	$\Gamma(K \ge 11) = 0.0191$			Allow for $P(\le 10) = 0.9808$, and < 0.99 , or $z = 2.092$ or
		> 0.01	A1		$p = 0.018$, but not $P(\le 11) = 0.9951$ or $P(=11) = 0.0143$
					Explicit comp with .01, or $z < 2.326$, not from ≤ 11 or $= 11$
	(β)	CR $R \ge 12$ and $11 < 12$	Al		Must be clear that it's ≥ 12 and not ≤ 11
		Probability 0.0049	AI		Needs to be seen, allow 0.9951 here, or $p = .0047$ from N
		Do not reject H_0 . Insufficient	M1	-	Needs like-with-like, $P(R \ge 11)$ or $CR R \ge 12$
		evidence that proportion of	AIFI	7	Conclusion correct on their p or CR, contextualised, not
		commuters who travel by train has			too assertive, e.g. "evidence that" needed.
_	(*)	increased	2.64		Normal, $z = 2.34$, "reject" [no cc] can get 6//
5	(1)	(a) $30+1.645 \times \frac{5}{30}$	MI D1		$30 + 5z/\sqrt{10}$, allow \pm but not just –, allow $\sqrt{10}$ errors
		$\sqrt{10}$			z = 1.645 seen, allow –
		= 32.6		4	Critical value, art 32.6
		Therefore critical region is $\overline{t} > 32.6$	AIFI	4	"> c " or " $\geq c$ ", FI on c provided > 30, can't be
			N / 1 4		recovered. Withhold if not clear which is CR
		(b) $P(t < 32.6 \mid \mu = 35)$	M1*		Need their c, final answer < 0.5 and μ = 35 at least, but
		$\frac{32.6-35}{2}$ [=-1.5178]	1*N(1		allow answer > 0.5 if consistent with their (1)
		$5/\sqrt{10}$		2	Standardise their CV with 35 and $\sqrt{10}$ or 10
		0.0645	AI	3	Answer in range $[0.064, 0.065]$, or 0.115 from 1.96 in (a)
	(ii)	$(32.6 - \mu) = 0$	M1		Standardise c with u, equate to Φ^{-1} , can be implied by:
	· /	$\mu = 32.6$	A1 FT		$\mu = \text{their } c$
		20 + 0.6m = 32.6	M1		Equate and solve for <i>m</i> , allow from 30 or 35
		m = 21	A1	4	Answer, a.r.t. 21, c.a.o.
					MR: 0.05: M1 A0 M1, 16.7 A1 FT
					Ignore variance throughout (ii)
					MR: 0.05: M1 A0 M1, 16.7 A1 FT Ignore variance throughout (ii)

6	(a)	N(24, 24)	B1	Normal, mean 24 stated or implied
		$(30.5-24) = 1 - \Phi(1.327)$	B1	Variance or SD equal to mean
		$1-\Phi\left(\frac{1}{\sqrt{24}}\right)$	M1	Standardise 30 with λ and $\sqrt{\lambda}$, allow cc or $\sqrt{\alpha}$ errors, e.g.
		- 0 0923	A1	.131 or .1103 ; 30.5 and $\sqrt{\lambda}$ correct
		- 0.0725	A1 5	Answer in range [0.092, 0.0925]
	(b)(i)	p or np [= 196] is too large	B1 1	Correct reason, no wrong reason, don't worry about 5 or 15
	(ii)	Consider $(200 - E)$	M1	Consider complement
		$(200 - E) \sim Po(4)$	M1	Po(200×0.02)
		$P(\geq 6) [= 1 - 0.7851]$	M1	Poisson tables used, correct tail, e.g. 0.3712 or 0.1107
		= 0.2149	A1 4	Answer a.r.t. 0.215 only
7		$H_0: \mu = 56.8$	B2	Both correct
		$H_1: \mu \neq 56.8$		One error: B1, but <i>not</i> \overline{x} , etc
		$\overline{x} = 17085/300 = 56.95$	B1	56.95 or 57.0 seen or implied
		300(973847	M1	Biased [2.8541] : M1M0A0
		$\frac{1}{299} \left(\frac{-56.95^2}{300} \right)$	M1	Unbiased estimate method, allow if ÷ 299 seen anywhere
		- 2 8637	A1	Estimate, a.r.t. 2.86 [not 2.85]
		56.95 - 56.8 - 1.535	M1	Standardise with $\sqrt{300}$, allow $\sqrt{\text{errors}}$, cc
	(α)	$z = \frac{28637}{\sqrt{2.8637/300}} = 1.555$	Al	$z \in [1.53, 1.54]$ or $p \in [0.062, 0.063]$, not – 1.535
		1.535 < 1.645 or 0.0624 > 0.05	AI	Compare explicitly z with 1.645 or p with 0.05, or
		1.555 < 1.045 01 0.0024 > 0.05		$2p > 0.1$, not from $\mu = 56.95$
	(β)	CV	M1	56.8 + $z\sigma/\sqrt{300}$, needn't have \pm , allow $\sqrt{100}$ errors
		$56.8 \pm 1.645 \times \sqrt{-300}$	A1	z = 1.645
		56.96 > 56.95	A1 FT	$c = 56.96$, FT on z, and compare 56.95 $[c_L = 56.64]$
		Do not reject H_0 ;	M1	Consistent first conclusion, needs 300, correct method
		3 07		and comparison
		insufficient evidence that mean	A1 FT	Conclusion stated in context, not too assertive, e.g.
		thickness is wrong	11	"evidence that" needed
8	(i)	r^{∞} $\begin{bmatrix} r^{-a+1} \end{bmatrix}^{\infty}$	M1	Integrate $f(x)$, limits 1 and ∞ (at some stage)
		$\int_{1} kx^{-a} dx = \left k \frac{x}{a+1} \right $	B1	Correct indefinite integral
		$\lfloor -u+1 \rfloor_1$	A1 3	Correctly obtain given answer, don't need to see
		Correctly obtain $k = a - 1$ AG		treatment of ∞ but mustn't be wrong. Not k^{-a+1}
	(ii)	$\int_{0}^{\infty} a^{-3} dx = \left[a x^{-2}\right]^{\infty} dx$	M1	Integrate $xf(x)$, limits 1 and ∞ (at some stage)
		$\int_{1} 3x^{-3} dx = \left 3 - \frac{3}{-2} \right _{1} = 1 \frac{1}{2}$		$[x^4 \text{ is } not \text{ MR}]$
			M1	Integrate $x^2 f(x)$, correct limits
		$\int_{1}^{\infty} 3x^{-2} dx = \left 3\frac{x^{-1}}{1} \right - (1\frac{1}{2})^{2}$	A1	Either $\mu = 1\frac{1}{2}$ or $E(X^2) = 3$ stated or implied, allow $k, k/2$
			M1	Subtract their numerical μ^2 , allow letter if subs later
		Answer ³ / ₄	A1 5	Final answer $\frac{3}{4}$ or 0.75 only, cwo, e.g. not from $\mu = -1\frac{1}{2}$.
				[SR: Limits 0, 1: can get (i) B1, (ii) M1M1M1]
	(iii)	$\int_{-\infty}^{\infty} (a-1) x^{-a} dx = \left[-x^{-a+1} \right]_{-\infty}^{\infty} = 0.9$	M1*	Equate $\int f(x) dx$, one limit 2, to 0.9 or 0.1.
		$J_1 \sim J_2 \sim J_1$		[Normal: 0 ex 4]
		$1 - \frac{1}{2} = 0.9$ $2^{a-1} = 10$	dep*M1	Solve equation of this form to get 2^{a-1} = number
		2^{a-1} 2 ^{<i>a</i>-1}	M1 indept	Use logs or equivalent to solve 2^{a-1} = number
		<i>a</i> = 4.322	A1 4	Answer, a.r.t. 4.32. T&I: (M1M1) B2 or B0

Specimen Verbal Answers

constant average rate"B0 β Above + "but it is contagious"B1 γ Above + "but not independent as it is contagious"B2 δ "Not independent as it is contagious"B2 δ "Not constant average rate", or "not independent"B0 λ "Not constant average rate because contagious" [needs more]B1 ζ "Not constant average rate because contagious" [needs more]B1 ζ "Not constant average rate because more likely at certain times of year"B2 μ Probabilities changes because of different susceptibilitiesB0 ν Not constant average rate because of different susceptibilitiesB2 η Correct but with unjustified or wrong extra assertion [scattergun]B1 θ More than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant	1	α	"Cases of infection must occur randomly, independently, singly and at	
βAbove + "but it is contagious"B1γAbove + "but not independent as it is contagious"B2δ"Not independent as it is contagious"B2ε"Not constant average rate", or "not independent"B0λ"Not constant average rate because contagious" [needs more]B1ζ"Not constant average rate because more likely at certain times of year"B2μProbabilities changes because of different susceptibilitiesB0νNot constant average rate because of different susceptibilitiesB2ηCorrect but with unjustified or wrong extra assertion [scattergun]B1θMore than one correct assertion, all justifiedB2πValid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant			constant average rate"	B0
γ Above + "but not independent as it is contagious"B2 δ "Not independent as it is contagious"B2 ϵ "Not constant average rate", or "not independent"B0 λ "Not constant average rate because contagious" [needs more]B1 ζ "Not constant average rate because more likely at certain times of year"B2 μ Probabilities changes because of different susceptibilitiesB0 ν Not constant average rate because of different susceptibilitiesB2 η Correct but with unjustified or wrong extra assertion [scattergun]B1 θ More than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant		β	Above + "but it is contagious"	B1
δ"Not independent as it is contagious"B2ε"Not constant average rate", or "not independent"B0λ"Not constant average rate because contagious" [needs more]B1ζ"Not constant average rate because more likely at certain times of year"B2μProbabilities changes because of different susceptibilitiesB0vNot constant average rate because of different susceptibilitiesB2ηCorrect but with unjustified or wrong extra assertion [scattergun]B1θMore than one correct assertion, all justifiedB2πValid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant		γ	Above + "but not independent as it is contagious"	B2
ϵ "Not constant average rate", or "not independent"B0 λ "Not constant average rate because contagious" [needs more]B1 ζ "Not constant average rate because more likely at certain times of year"B2 μ Probabilities changes because of different susceptibilitiesB0 ν Not constant average rate because of different susceptibilitiesB2 η Correct but with unjustified or wrong extra assertion [scattergun]B1 θ More than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant		δ	"Not independent as it is contagious"	B2
λ "Not constant average rate because contagious" [needs more]B1 ζ "Not constant average rate because more likely at certain times of year"B2 μ Probabilities changes because of different susceptibilitiesB0 ν Not constant average rate because of different susceptibilitiesB2 η Correct but with unjustified or wrong extra assertion [scattergun]B1 θ More than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant		3	"Not constant average rate", or "not independent"	B0
$ \zeta \qquad \text{``Not constant average rate because more likely at certain times of year''} B2 \\ \mu \qquad Probabilities changes because of different susceptibilities \qquad B0 \\ \nu \qquad \text{Not constant average rate because of different susceptibilities} \qquad B2 \\ \eta \qquad \text{Correct but with unjustified or wrong extra assertion [scattergun]} \qquad B1 \\ \theta \qquad \text{More than one correct assertion, all justified} \qquad B2 \\ \pi \qquad \text{Valid reason (e.g. "contagious") but not referred to conditions} \qquad B1 \\ [Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant \\ \end{tabular} $		λ	"Not constant average rate because contagious" [needs more]	B1
μ Probabilities changes because of different susceptibilitiesB0 ν Not constant average rate because of different susceptibilitiesB2 η Correct but with unjustified or wrong extra assertion [scattergun]B1 θ More than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitatinglearnt phrases, such as "events must occur randomly, independently, singly and at constant		ζ	"Not constant average rate because more likely at certain times of year"	B2
vNot constant average rate because of different susceptibilitiesB2 η Correct but with unjustified or wrong extra assertion [scattergun]B1 θ More than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitatinglearnt phrases, such as "events must occur randomly, independently, singly and at constant		μ	Probabilities changes because of different susceptibilities	B0
ηCorrect but with unjustified or wrong extra assertion [scattergun]B1θMore than one correct assertion, all justifiedB2 π Valid reason (e.g. "contagious") but not referred to conditionsB1[Focus is on explaining why the required assumptions might not apply. No credit for regurgitatinglearnt phrases, such as "events must occur randomly, independently, singly and at constant		ν	Not constant average rate because of different susceptibilities	B2
$\begin{array}{ccc} \theta & \text{More than one correct assertion, all justified} & B2\\ \pi & \text{Valid reason (e.g. "contagious") but not referred to conditions} & B1\\ [Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant \\ \end{array}$		η	Correct but with unjustified or wrong extra assertion [scattergun]	B1
π Valid reason (e.g. "contagious") but not referred to conditions B1 [Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant		θ	More than one correct assertion, all justified	B2
[Focus is on explaining why the required assumptions might not apply. No credit for regurgitating learnt phrases, such as "events must occur randomly, independently, singly and at constant		π	Valid reason (e.g. "contagious") but not referred to conditions	B1
learnt phrases, such as "events must occur randomly, independently, singly and at constant	[Focu	s is on e	explaining why the required assumptions might not apply. No credit for regu	urgitating
	learnt	phrases	s, such as "events must occur randomly, independently, singly and at cons	tant

average rate, even if contextualised.]

2 Don't need either "yes" or "no".

α	"No it doesn't invalidate the calculation" [no reason]	B0
β	"Binomial requires not chosen twice" [false]	B0
γ	"Probability has to be constant but here the probabilities change"	B0
δ	Same but "probability of being chosen" [false, but allow B1]	B1
3	"Needs to be independently chosen but probabilities change" [confusion]	B0
ζ	"Needs to be independent but one choice affects another" [correct]	B2
η	"The sample is large so it makes little difference" [false]	B0
θ	"The population is large so it makes little difference" [true]	B2
λ	Both correct and wrong reasons (scattergun approach)	B1

[Focus is on modelling conditions for binomial: On every choice of a member of the sample, each member of the population is equally likely to be chosen; and each choice is independent of all other choices.

Recall that in fact even without replacement the probability that any one person is chosen is the same for each choice. Also, the binomial "independence" condition <u>does</u> require the possibility of the same person being chosen twice.]

1		<u>^ 468</u> 52	B1	52 stated
		$\mu = x = \frac{1}{9} = 52$	M1	Correct method for biased estimator
		24820	M1	Multiply by 9/8
		$\frac{21020}{9} - 52^2 = 53.78$		[if single formula, allow M0 M1 if wrong but divisor 8 seen
		9 50 -		anywhere]
		$\hat{\sigma}^2 = \frac{7}{8} \times 53.78 = 60.5$	A1 4	Answer 60.5 or exact equivalent
2		$53.28 - \mu$ 1.06	M1dep	Standardise with \sqrt{n} once & equate to z, allow sign, square/ \sqrt{n}
		$\frac{1}{5/\sqrt{n}} = 1.96$	_	errors
		u = 51.65	A1	twice, signs correct, zs may be wrong
		$\frac{\mu - 51.05}{5} = 1.3$	B1	Both correct z values seen
		$5/\sqrt{n}$	depM1	Solve to get \sqrt{n} or μ , needs first M1
		$\sqrt{n} = 10, \qquad n = 100$	A1	n = 100, not from wrong signs
		$\mu =$ 52.3	B1 6	a.r.t. 52.3, right arithmetic needed but \sqrt{n} can be omitted
3		B(200, 0.0228)	M1	B(200, 0.0228) stated or implied
		Po(4.56)	A1	Po(4.56) stated or implied, allow 4.6 here
		4.56^2	M1	Correct formula for $P(\le 2) \pm 1$ term, any λ (tables: M0)
		$e^{-4.56}(1+4.56+\frac{1000}{2})$	A1	Correct formula, 4.56 needed
		- 0 167	A1	Answer, a.r.t. 0.167 [0.16694]
		n large or n > 50: n small or nn < 5	B1 6	Both, can be merely asserted. If numbers, must be these
		<i>n</i> large of $n > 50$, <i>p</i> small of $np < 5$		SR interpolation: clear method M1, answer A2
				MR: typically B(200, 0.228) \approx N(45.6, 3.52); M1A1:
				standardise correctly. M1: state np , $nq > 5$, B1
4	(i)	Either 213.4-230	M1	Standardise z with $\sqrt{50}$, ignore sign or $\sqrt{0}$ or squaring errors
	~ /	Either $z = \frac{45}{\sqrt{50}}$		
		- 2608	A 1	<i>z</i> -value, a.r.t. –2.61, or <i>p</i> in range [0.0044, 0.005)
		-2.000	AI D1	Correctly compare $(-)2.576$, signs consistent,
		-2.008 < -2.370 07 0.0047 < 0.003	ы	or p explicitly with 0.005
	Or	CV is 220, 2.57 $c_{\rm V}$, $4^5 = 213.6$	M1	$230 - z\sigma/\sqrt{50}$, allow $\sqrt{100}$ or squaring errors, allow \pm but not
		$\sqrt{50} = 2.376 \times \frac{10}{\sqrt{50}} = 213.0$	B1	just +; $z = 2.576$
		213.4 < 213.6	A1	Explicitly compare 213.4 with 213.6
		Reject H ₀ , Significant evidence	M1	"Reject". FT, needs correct method and form of
		that population mean is not 230	A1 FT 5	comparison: interpreted acknowledge uncertainty
	(ii)	Yes population distribution is not	B2 2	Not "ves sample size is large" but ignore " <i>can</i> use it as "
	(11)	known to be normal	52 -	SR: Both right and wrong answers: B1
				α "Yes as it must be assumed normal". B1
5		H_{a} : $\lambda = 12$: H_{a} : $\lambda > 12$	B2	Both correct: B2 Allow // One error B1 but not r rate
•		H_{0} , $\mathcal{H} = 12$, H_{1} , $\mathcal{H} > 12$ Eithor: D(> 10) - 1 $D(< 18)$	M1	Po(12) stated or implied e.g. 0.9787
		$Luner \cdot f(\geq 19) - f(\leq 10)$	1011	10(12) stated of implied, e.g. 0.9787
		-1 - 0.9020 -0.0374	A1	0.0374 or 0.9626 if compared with 0.9
		- 0.0374 - 0.1	B1	Explicitly compare $P(> 19)$ with 0.1 or $P(< 18)$ with 0.9
		∇v_{1}	Δ1	> 18 and 0.062 stated
		0.000 $10 > 10$	R1	\geq 10 and 0.000 stated Explicit comparison of CV (right hand CP) with 10
		17∠10 Daiaat U. Significant avidance of	M1	"Dajast" ET pages correct mathed and comparison a 2 rect
		increase in mean number of	1111	from ≤ 10 or $= 10$, withhold if inconsistent
		applicants		IFOIN \geq 19 or = 19, Withhold II inconsistent
		applicants	AITI /	interpreted in context, acknowledge uncertainty

6	(i)	If one customer arrives, it does not	B1		Answer that shows correct understanding of "independent", in
		change the probability that another			context; not just equivalent to "singly"
		one does so; customers probably	B1	2	Plausible reason, in context, nothing wrong, nothing that
		arrive in groups of at least 2			suggests "constant average rate"
	(ii)	0.1730	M1		Correct use of tables or formula, e.g3007, or .4405 from Po(5)
			Al	2	if Po(7) stated; answer 0.173, 0.1730 or better
	(111)	Po(35)	Bl		$Po(5\times7)$ stated or implied
		N(35, 35)	MI		Normal, $\mu = \text{their } \lambda$
		$(40.5-35) = 1$ $\Phi(0.0207)$	AI M1		Both parameters correct, allow 35^2 , $\sqrt{35}$
		$1-\Phi\left \frac{1-\Phi}{\sqrt{25}}\right ^{-1}=\Phi(0.9297)$			Standardise 40 with λ , $\forall \lambda$, allow \forall , cc errors
				6	Both $\sqrt{\lambda}$ and cc correct
7	(i)	= 0.1763	D1	U	Answer, a.r.t. 0.176 [penalise 0.1765]
'	(1)		B1 B1		Concave decreasing curve above axis
			B1	3	Both correct including approx relationship, not extending
			DI	5	beyond [1_3] verticals and scale not needed
	(ii)		M1		Attempt $\int f_{x}(r) dr$ limits 1 3 at some stage and equate to 1
	(11)	$\int_{-\frac{a}{2}}^{3} \frac{a}{2} dx = 1, \left \frac{-a}{2} \right = 1; a = \frac{3}{2}$	B1		Correct indefinite integral
		$\int x^2 \qquad [x]_1$	A1	3	Correctly obtain $3/2$ or 1.5 or exact equivalent
	(iii)	$\int a^{3}a = \int a^{3}$	M1		Attempt $\int xf_x(x)dx$, limits 1, 3 at some stage
		$\int_{1} \frac{-dx}{x} - \left[a \ln x\right]_{1}$	B1 F	Т	Correct indefinite integral, FT on a
		$=\frac{3}{2}\ln 3$	A1 F	Т3	Answer, any exact equivalent or a.r.t 1.65, FT on a, or a ln 3
	(iv)	T is equally likely to take any value	R1		Must be "values taken by T" (or "of T") or clear equivalent
	(1)	between 1 and 3	DI	-	Any hint that they think T is an <i>event</i> gets B()
		between 1 and 5			α "Same chance of occurring anywhere between 1 and 3": 0
					β "For values of T between 1 and 3 T is equally likely". 0
					γ "Each value of T is equally likely to occur": 1
8	(i)	B(40, 0.225)	M1		B(40, 0.225) stated or implied
8	(i)	$B(40, 0.225) \approx N(9, 6.975)$	M1 M1		B(40, 0.225) stated or implied Normal, mean 9
8	(i)	B(40, 0.225) ≈ N(9, 6.975) 5.5-9 = -1.325	M1 M1 A1		B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975
8	(i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$	M1 M1 A1 M1		B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc
8	(i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074	M1 M1 A1 M1 A1		B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225)
8	(i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 wn = 9 > 5 or n large: and	M1 M1 A1 M1 A1 A1 A1	0	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908]
8	(i)	B(40, 0.225) $\approx N(9, 6.975)$ $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and na = 31 > 5 or n close to 0.5	M1 M1 A1 M1 A1 A1 B2	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> ,
8	(i) (i)	B(40, 0.225) $\approx N(9, 6.975)$ $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5	M1 M1 A1 M1 A1 A1 B2	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600
8	(i) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers	M1 M1 A1 M1 A1 A1 B2 B1 B1	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly")
8	(i) (ii)	B(40, 0.225) $\approx N(9, 6.975)$ $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 $np = 9 > 5 \text{ or } n \text{ large; and}$ $nq = 31 > 5 \text{ or } p \text{ close to } 0.5$ Number list sequentially and select using random numbers If # > 3600 ignore (etc)	M1 M1 A1 M1 A1 A1 B2 B1 B1 B1 B1	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600 or "ignore repeats"
8	(i) (ii)	B(40, 0.225) $\approx N(9, 6.975)$ $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc)	M1 M1 A1 M1 A1 A1 B2 B1 B1 B1	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1
8	(i) (ii)	B(40, 0.225) $\approx N(9, 6.975)$ $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7)	M1 M1 A1 M1 A1 A1 B2 B1 B1 B1 B1 M1	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered
8	(i) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13	M1 M1 A1 M1 A1 A1 B2 B1 B1 B1 B1 M1 A1	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities
8	(i) (ii) (i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 M1 A1 A1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen
8	(i) (ii) (i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$	M1 M1 A1 M1 A1 B2 B1 B1 B1 M1 A1 A1 A1 B2	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0
8	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 A1 A1 A1 A1 B2 B1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12,
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 M1 A1 A1 A1 B2 B1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV from correct tail and inequality with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 M1 A1 A1 A1 A1 B2 B1 M1 M1	8 3 3	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV
9	(i) (ii) (i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 M1 A1 A1 A1 B2 B1 M1	8	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12
9	(i) (ii) (i)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 M1 A1 B2 B1 M1 A1 F	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 M1 A1 A1 B2 B1 M1 A1 F	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob.0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 M1 A1 B2 B1 M1 A1 F	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum]
9	(i) (ii) (ii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, or "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum] [0.9932 or 0.0068 probably B2 maximum] D(14.0.8) extend prime in the second constant of the second constant constant contextualised, acknowledge uncertainty [N: Normal or Po: (i) M1, (ii) B2 maximum]
9	(i) (ii) (ii) (iii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7 B(14, 0.8) B(14, 0.8)	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and \sqrt{npq} , allow <i>npq</i> , no or wrong cc CC and \sqrt{npq} correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV <i>from correct tail and inequality</i> with 12, <i>or</i> P(\geq 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs \geq 13 or < 12; <i>p</i> method needs \geq 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum] B(14, 0.8) stated or implied, allow from B(14, 0.75)
8	(i) (ii) (ii) (iii)	B(40, 0.225) ≈ N(9, 6.975) $\frac{5.5-9}{\sqrt{6.975}} = -1.325$ 0.9074 np = 9 > 5 or n large; and nq = 31 > 5 or p close to 0.5 Number list sequentially and select using random numbers If # > 3600, ignore (etc) B(14, 0.7) CR is ≥ 13 with probability 0.0475 H ₀ : $p = 0.7$, H ₁ : $p > 0.7$ 12 < 13 Do not reject H ₀ . Insufficient evidence that proportion who show improvement is greater than 0.7 B(14, 0.8) P(≤ 12) from B(14, 0.8) 0.9021	M1 M1 A1 M1 A1 B2 B1 B1 B1 B1 B1 M1 A1 F M1 A1 F	8 3 3 T 5	B(40, 0.225) stated or implied Normal, mean 9 Variance 6.975 or SD 2.641 or 6.975 Standardise with <i>np</i> and √ <i>npq</i> , allow <i>npq</i> , no or wrong cc CC and √ <i>npq</i> correct, allow from N(3600, 0.225) Answer, in range [0.907, 0.908] Full conditions B2; partial, B1 (assertions OK). Allow <i>npq</i> , allow from e.g. <i>n</i> = 3600 Number list, don't need "sequentially" Mention random numbers (<i>not</i> "select numbers randomly") Deal with issue of # > 3600, <i>or</i> "ignore repeats" α "Randomly pick numbers from 0 to 3599": (B1) B0 B1 B(14, 0.7) stated or implied, e.g. N(9.8, 2.94), can be recovered CV 13, or > 12 or {13, 14}, allow = but no other inequalities Exactly correct CR, and supporting prob .0475 or .9525 seen Both, B2. Allow π . One error, B1, but <i>r</i> , <i>x</i> etc: B0 Compare CV from correct tail and inequality with 12, <i>or</i> P(≥ 12) = 0.1608 and > 0.05 <i>or</i> P(< 12) = 0.8392 and < 0.95 Correct method & conclusion, requires like-with-like; CV method needs ≥ 13 or < 12; <i>p</i> method needs ≥ 12 or < 12 Withhold if inconsistent Contextualised, acknowledge uncertainty [SR: Normal or Po: (i) M1, (ii) B2 maximum] B(14, 0.8) stated or implied, allow from B(14, 0.75) Attempt prob of acceptance region, e.g. 0.8990, $$ on (i) Answer 0.802 or o. <i>x</i> t 0.8021

1		Number all the houses sequentially, or use house numbers Select using random numbers Ignore numbers > 263	B1 B1 B1	3	Any mention of using house numbers, or houses, or other numbering. (List can be implied). <i>Not</i> random numbering unless correct subsequent method (e.g. sort them numerically) Mention random numbers. <i>Not</i> "select numbers randomly". Must be random method. NB: Using 263 × calculator Rand # is biased: B0. But "Ran#(263)" is unbiased. Deal with problem of > 263, <i>or</i> repeats.
					"Select 20 random numbers between 1 and 263": B1B0 [If this, need to mention repeats to get last B1]
_			2.64		<i>Example:</i> "put numbers/house names (etc) into hat and select": B1B0B0
2	α	$\mu = \frac{48+57}{52.5}$	MI		Use symmetry to find μ
		^μ 2	AI		Obtain $\mu = 52.5$
		$\Phi^{-1}(0.9332) = 1.5$	B1		1.5 seen, e.g. in $4.5 \div 1.5$
		$4.5 \div 1.5$ [$\sigma = 3$]	M1		4.5 ÷ their Φ^{-1} , or 1.645 ÷ their Φ^{-1} , must be +ve, allow cc
	β	$\frac{57-\mu}{\sigma} = 1.5, \frac{48-\mu}{\sigma} = -1.5$	M1 A1		$\frac{57-\mu}{\sigma} = z$, $\frac{48-\mu}{\sigma} = -z$ M1 for one, ignoring cc, σ^2 , sign or "1–" errors, RHS must be Φ^{-1} (<i>not</i> Φ
		Solve simultaneously: $y = 52.5$ [$\sigma = 3$]	B1		[e.g. 0.8246 or 0.5267] or 0.0668 or 0.9332); A1 for both completely correct except for value of z. $z = 1.5$ or -1.5 in at least one equation
		$\mu = 52.5$ [0 = 5]	AI		Solve without obvious errors, get μ = 52.5, OK from wrong z [NB: 52.5 from both signs wrong: A0]
		$u + \frac{4.5}{2} \times 1.645$	M1		$\mu + z\sigma$ [Their μ and σ , anything recognisable as z] [expect to see 52.5 + 3×1.645]
		1.5	B1		z = 1.645 seen
		= 57.4 (35)	A1	7	Answer in range [57.4, 57.45], cwo
3		$CV_{20} = \frac{5}{2226} \times 2326 = 17.0925$	M1		Attempt $20 - 5z/\sqrt{16}$, allow SD \leftrightarrow var errors, allow $20 \pm 5z/\sqrt{16}$, not $20 + 5z/\sqrt{16}$, allow cc
		$20 - \frac{1}{\sqrt{16}} \times 2.520$	B1		2.326 seen
			A1		CV a.r.t. 17.1 [NB: not 17.9075]
		P(X > 17.0925)	M1*		Standardise any attempt at a CV (from $\mu = 20$) with 15 and any SD that would have got first M1,
		$-(17.0925-15) - \Phi(1.674)$			allow cc
		$ -\Phi - \Phi - \Psi(1.0/4)$	Al		z = 1.674 seen or implied, e.g. by $p = 0.047$ or 0.953 or 0.9535, allow anything in range [1.67, 1.68]
			dep M1	_	Probability < 0.5 , or > 0.5 if their CV is < 15
		Answer U.U4/1	Al	7	Answer, a.r.t. 0.047 [including 0.0465 from CV 17.1]
					<i>Notes:</i> 16 missing: can get M0B1A0M1A0M1A0, or even last two A1's if 16 used then

4	(i)		M1 A1	2	Positive parabola, all above axis. [Don't worry about being pointed unless extreme.] Correct place, touches <i>x</i> -axis, not beyond the limits suggested by their axes, symmetric ends, not too straight
	(ii)	$\frac{3}{2}\int_{0}^{4}x^{2}(x-2)^{2}dx$	M1		Attempt $\int x^2 f(x) dx$, limits 0 and 4
		$16 \int_0^{16} \frac{1}{10} \int_0^{16} \frac{1}{10} \frac{1}{10$	M1		Method for integration, e.g. multiply out [indept] [Or use $\sigma^2 = \frac{3}{16} \int_{0}^{4} (x-2)^4 dx$]
		$= \frac{3}{16} \left[\frac{x^3}{5} - x^4 + 4\frac{x^3}{3} \right]_0 \qquad [= 6\frac{2}{5}]$	B1		Correct indefinite integral, limits not needed, e.g. parts: $\frac{3}{16} \left[\frac{x^2(x-2)^3}{3} - \frac{x(x-2)^4}{6} + \frac{(x-2)^5}{30} \right]$
		$\sigma^2 = 6\frac{2}{5} - 2^2$	B1		Subtract 2^2
		$=2\frac{2}{5}$	A1	5	Final answer 2.4, any equivalent exact form, cwo
	(iii)	No because <i>x</i> represents a value taken by the random variable [not an event that "occurs"]	B1	1	Show clear understanding that x is a value of X. Usual misunderstanding is "X is an event thatmay or may not occur, depending on x". However:SR:Allow B1 for answer clearly indicating that probabilities higher where curve
					higher, <i>or</i> clearly stating that all probabilities are effectively zero.
					E.g.: Agree as area under graph [or $I(x)$] increases, or minimum at 2 B1 "True only between 0 and 4": B0 unless explanation
					Mention of variance etc: 0. "Agree because the graph shows this": B0
5	(i)	$H_0: p = 0.4; H_1: p < 0.4$	B1B1		Both: B2. Allow π . One error, B1, but x or r: 0. SEE NOTES AT START AND END
		B(10, 0.4)	M1		B(10, 0.4) stated or implied, e.g. N(4, 2.4) [$P(=1)$ [=0.0404] or $P(\ge 1)$ [=0.9940] or $P(<1)$
			A 1		[=0.0060] or Poisson or normal, or RH tail for CR, gets no more marks in (i)]
	α	$P(\le 1) = 0.0464$			This probability or 0.9536 only
	ß	< 0.03 so reject Π_0			Explicit comparison with 0.05, or 0.9536 with 0.95
	Ч	Probability of this is 0.0464	A1 A1		This probability needs to be seen
		Reject H_0 .	M1		Correct method, \checkmark , comparison and first conclusion
		Significant evidence that % who	A1 √	7	Interpreted in context, "evidence that" or equiv needed, \checkmark on numbers
		book with travel agents reduced			-
	(ii)	Can't deduce cause-and-effect	B1	1	Equivalent comment, regardless of answer to (i). Ignore wrong answer if right answer seen "Other factors haven't been considered" B1
					"Sample is small", or "test may be wrong" B0

6	(i)	$H_0: \mu = 24.3; H_1: \mu \neq 24.3$	B1B1		Both: B2. 1 error, B1, but t, x etc: B0 SEE NOTES AT START AND END
		$\bar{t} = 26.28$	B1		26.28 seen or implied
		50[36602.17	M1		Correct formula for biased estimate $[= 41.405]$
		$\hat{\sigma}^2 = \frac{1}{49} \left[\frac{1}{50} - 26.28^2 \right]$	M1		Multiply by 50/49
					[Single formula: M2, or give M1 if wrong but 49 divisor seen]
		-42.23	A1		42.25 or 6.5 seen or implied
	α	$z = \frac{20.28 - 24.3}{\sqrt{12.25 + 22}} = 2.154$	M1		Standardise their \bar{t} with 24.3, $\sqrt{50}$, allow sign/ $\sqrt{/cc}$ errors, their variance
		√42.25/50 2.55 €	A1		2.15(4) or p in range [0.0153, 0.0158], not -2.154 unless 0.015(6) subsequently used, not 1-tail
		< 2.576	A1		Compare z with ± 2.576 , or $p > 0.005$, or $2p$ with 0.01, not from $\mu = 26.28$
	β	42.25	MI		
		$CV_{24.3+2.576\times\sqrt{\frac{12.25}{50}}}$			$24.3 + zs/V50$, allow cc, V errors, allow \pm but not – only. Not $26.28 - zs/V50$
		$\gamma = 50$			$z = 2.5/6$, not from $\mu = 26.28$ or 50 omitted, not from 1-tail
		= 20.07 and $20.28 < 20.07$			Correct CV, V on z, and compare sample mean
		Do not reject H_0 . Insufficient evidence of a		11	Conclusion, \checkmark , needs method, like-with-like, 50, not from $\mu = 26.28$, doesn't need correct z
		change in maximum daily temperature.	AIV.	11	Contextualised, recognise uncertainty, V on numbers
					NB: Clear evidence of $\mu = 26.28$: can't get last 4 marks. See exemplars y and δ
	(11)	<i>n</i> is large	B1	1	This answer <i>only</i> or " $n >$ number" where number ≥ 29 , <i>not</i> both this and "distribution unknown".
					But " <i>n</i> is large so we can approximate even though we don't know the distribution" is B1
					"Possible as $n = 50$ " B0.
7	(i)	Po(11)	M1		Po(11) stated or clearly implied
		$1 - P(\le r) = 0.854$ gives $r = 14$	M1		Find 1 – 0.146 in tables, e.g. answer 14 [RH tail, e.g. "7", or single value only: max M1M0A0]
		so <i>n</i> = 15	Al	3	$n = 15$ only, allow " ≥ 15 "
	(ii)	$Po(44) \approx N(44, 44)$	M1		Normal, mean attempted 2.2×20
		$\Phi(37.5-44) = \Phi(-0.980)$	A1		Both parameters 44, allow var = $\sqrt{44}$ or 44^2
		$\Psi\left(\frac{1}{\sqrt{44}}\right)$	M1		Standardise, their 44, allow cc, $\sqrt{\text{errors}}$, e.g. ans 0.283 or 0.2036 or 0.4411, not $\div 20$
			Al	_	$\sqrt{1}$ and cc both correct
		= 0.1635	Al	5	Answer in range [0.163, 0.164]
	(iii)	B(40, 0.146)	M1		B(40, 0.146) stated or implied, e.g. by Po(5.84)
		$\approx N(5.84, 4.98736)$	M1		Normal, attempt at mean = np [Poisson etc, or exact binomial (0.22132): no more marks]
		$-1 - \Phi(0.7433)$	A1		Both parameters correct [Poisson(5.84) \rightarrow N(5.84, 5.84): M0A0]
		$\left[1-\Psi\left(\frac{1}{\sqrt{4.98736}}\right)\right] = 1-\Psi(0.7433)$	M1		Standardise with their <i>np</i> and <i>npq</i> , allow cc, $\sqrt{\text{errors}}$, e.g. ans 0.3838 or 0.302 or 0.370
		(())))))))	A1		cc and $$ both correct
		= 0.2286	A1	6	Answer in range [0.228, 0.229]
					SC: $B(40, 0.854) \approx N(34.16, 4.98736)$: can get full marks, but if $R > 7$ used, max 3

8	(a) (i)	Several calls may all refer to the	B1 1	Any reason showing correct understanding of "independent", but not just "singly" or equivalent. Ignore
		same incident		extra condition(s) unless clearly wrong in which case B0. Not " <i>fires</i> " independent.
	<i></i>		D.I	"Fires might spread" B0
	(11)	Calls occur at constant average rate	BI	This condition only, allow "average" omitted, not "constant probability", not "random" unless clearly
				correct interpretation follows. No third condition unless fully justified by subsequent answer.
		E a No because incidents are	P 1 7	A nu commont (with either ves or ne) showing correct understanding, but
		less/more common at night		"Fires might not occur at constant average rate" is not enough (gets B1 B0)
		less more common at night		"Different rates at different times of year": B0
	(b) (i)	$(2.74^2)_{2.74}$	M1	Formula for any one correct Poisson probability for $r \ge 1$ $[1 - (0.06457 + 0.17692 + 0.24238)]$
		$1 - \left(1 + 2.74 + \frac{2.77}{2!}\right)e^{-2.74}$	M1	Correct overall formula, allow 1 error (e.g. 1 term extra or missing or no "1 –")
		= 0.516(1)	A1 3	Answer, a.r.t. 0.516 [Interpolation (0.51604) or no working: B0 or B3]
	(ii)	$(e^{-2} \times 1)(e^{-3} \times 3) + (e^{-2} \times 2)(e^{-3} \times 1)$	M1	Two correct terms multiplied, or all 4 bits seen, e.g. $.1353 \times .1494 + .2707 \times .4979 = 0.0202 + 0.0135$
			A1	Correct expression
		= 0.0337	A1 3	Answer, a.r.t. 0.0337
	(iii)	$(e^{-\lambda} \times 1)(e^{-\mu} \times \mu) + (e^{-\lambda} \times \lambda)(e^{-\mu} \times 1)$	M1	Correct algebraic expression [Ignore 1! throughout]
		$=e^{-\lambda}\!\! imes\!e^{-\mu}\left(\lambda+\mu ight)$	M1	Take out factor of $e^{-\lambda} \times e^{-\mu}$ or equivalent essential step
		$=e^{-(\lambda+\mu)}(\lambda+\mu)$	A1	Correctly obtain exact answer [allow $e^{-\lambda - \mu}(\lambda + \mu)$]
		= P(T = 1)	A1 4	4 All correct, and write down correct formula for $P(T = 1)$ [NB: <i>T</i> needed] Allow working towards middle
				SR: $\lambda = 2$, $\mu = 3$: Can get M1M1A1A0 if e^{-2} and e^{-3} retained. As soon as decimal approximations seen,
				no more marks.

Specific examples for question $S(t)$	Specific	examp	les for	question	5(i)
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~	$H_0: n = 0.4: H_1: n < 0.4$	B1B1		8	$H_{0}: n = 0.4: H_{1}: n < 0.4$	B1B1	
u	N(A = 2A)	M1		0	$\mathbf{R}(10, 0, 4)$	M1	
	N(4, 2.4)				B(10, 0.4)		
	$P(\le 1) = 0.0533$	A0			$P(\ge 1) = 0.9939$	A0	
	> 0.05				> 0.95	A0	
	So do not reject H ₀ . Insufficient evidence that % who	M0			So reject H ₀	M0	
	book with travel agents reduced		3		Insufficient evidence that % who book with travel agents	A0	3
					reduced		
β	$H_0: p = 0.4; H_1: p < 0.4$	B1B1		3	$H_0: p = 0.4; H_1: p \neq 0.4$ [two-tailed]	B1B0	
	B(10, 0.4)	M1			B(10, 0.4)	M1	
	" $P(=1) = 0.0464$ " [allow this]	A1			" $P(=1) = 0.0464$ "	A1	
	< 0.05	A1			> 0.025	A0	
	So reject H_0	M1			So do not reject H_0	M1	
	Insufficient evidence that % who book with travel	A0	6		Insufficient evidence that % who book with travel agents	A1	5
	agents reduced				reduced		
γ	$H_0: p = 0.4; H_1: p < 0.4$	B1B1		ζ	$H_0: p = 0.4; H_1: p < 0.4$	B1B1	
	B(10, 0.4)	M1		-	B(10, 0.4)	M1	
	P(=1) = 0.0404 [look out for this]	A0			P(=1) = 0.0464	A1	
	< 0.05 so reject H ₀	A0			[no explicit comparison]	A0	
	Significant evidence that % who book with travel	M0			So reject H ₀ . Significant evidence that % who book with	M1	
	agents reduced	A0	3		travel agents reduced	A1	6

Specific examples for question 6(i)

α	$ \begin{array}{l} \mathrm{H}_{0}: \ \bar{t} = 24.3; \ \mathrm{H}_{1}: \ \bar{t} \neq 24.3 \qquad [wrong symbol] \\ \bar{t} \ \text{not seen explicitly} \qquad [implied by] \\ \\ \hat{\sigma}^{2} = \left[\frac{36602.17}{50} - 26.28^{2} \right] = 41.405 \ [biased est] \\ \\ z = \frac{26.28 - 24.3}{\sqrt{41.405/50}} = 2.1758 \\ \\ < 2.576 \\ \\ \mathrm{Accept } \mathrm{H}_{0}, \ \mathrm{maximum \ temp \ unchanged} \\ \\ [over-assertive, \ otherwise \ A1] \end{array} $	B0B0 B1 M1 M0 A0 M1 A0 A1 M1A0	5	δ	$H_0 = 24.3; H_1 \neq 24.3 $ [missing symbol] $\bar{t} = 26.28$ $\hat{\sigma}^2 = = 42.25$ $z = \frac{24.3 - 26.28}{\sqrt{42.25/50}} = -2.154$ [loses 1] > -2.576 Insufficient evidence to reject H ₀ . No change in maximum daily temperature. [OK]	B1 only B1 M1M1 A1 M1 A0 A1 M1 A0 A1 M1 A0 A1 M1 A1 M1 A1 M1 A1 M1 A1 9
β	H ₀ : $\mu = 26.28$; H ₁ : $\mu \neq 26.28$ [WRONG] $\overline{t} = 24.3$ [explicitly] $\hat{\sigma}^2 = = 42.25$ $z = \frac{26.28 - 24.3}{\sqrt{42.25/50}} = 2.154$ [allow this – BOD] < 2.576 Accept H ₀ . Insufficient evidence of a change in maximum daily temperature.	B0B0 B0 M1M1 A1 M1 A1 A1 M1 A1	8	3	H ₀ : $\mu = 24.3$; H ₁ : $\mu > 24.3$ [one-tail] $\bar{t} = 26.28$ $\hat{\sigma}^2 = = 42.25$ $z = \frac{26.28 - 24.3}{\sqrt{42.25/50}} = 2.154$ < 2.326 Accept H ₀ . Insufficient evidence of a change in maximum daily temperature.	B1B0 B1 M1M1 A1 M1 A1 A0 M1 A1 9
γ	H ₀ : $\mu = 26.28$; H ₁ : $\mu \neq 26.28$ [WRONG] \bar{t} not seen separately [implied] $\hat{\sigma}^2 = = 42.25$ $z = \frac{24.3 - 26.28}{\sqrt{42.25/50}} = -2.154$ [DON'T allow this] > -2.576 Accept H ₀ . Insufficient evidence of a change in maximum daily temperature.	B0B0 B1 M1M1 A1 M1 A0 A0 M0 A0	5	η	$z = \frac{24.3 - 26.28}{\sqrt{42.25/50}} = -2.154 but \ then$ So $p = 0.0156 > 0.005 [OK \ here]$ Accept H ₀ . Insufficient evidence of a change in maximum daily temperature. $z = \frac{26.28 - 24.3}{\sqrt{42.25}} = 0.3046 \ [no \ \sqrt{50}]$ < 2.576 Accept H ₀ . Insufficient evidence of a change in maximum daily temperature.	M1 A1 A1 M1 A1 (11) M0 A0 A0 M0 A0 (6)

The following guidance notes are provided.

1 Standardisation using the normal distribution.

(a) In *stating* parameters of normal distributions, don't worry about the difference between σ and σ^2 , so allow N(9, 16) or N(9, 4²) or N(9, 4). When *calculating* $\frac{\overline{x} - \mu}{\sigma / \sqrt{n}}$, the following mistakes are accuracy mistakes

and not method mistakes so can generally score M1A0:

confusion of σ with σ^2 or $\sqrt{\sigma}$; *n* versus \sqrt{n} ; wrong or no continuity corrections.

(b) Use of $\frac{\mu - \overline{x}}{\sigma}$ instead of $\frac{\overline{x} - \mu}{\sigma}$ is not penalised if it leads to a correct probability, but if the candidate is

using a *z*-value in a hypothesis test, an answer of z = -2.15 when it ought to be 2.15 is an accuracy error and

loses the relevant A1. When finding μ or σ^2 from probabilities, some candidates are taught to use $\frac{\mu - \bar{x}}{\sigma}$

whenever $\mu > \overline{x}$; provided the signs are consistent this gains full marks.

- (c) Some candidates are taught to calculate, for example, P(X > 5) from N(9, 16) by calculating instead P(X < 13). This is a correct method, though it looks very strange the first time you see it.
- (d) When calculating normal approximations to binomial or Poisson, use of the wrong, or no, continuity correction generally loses the last two marks: A0 A0.
- 2 Conclusions to hypothesis tests. There are generally 2 marks for these.
- (a) In order to gain M1, candidates must not only say the correct "Reject/do not reject H₀" but have done the whole test in essence correctly apart from numerical errors. In other words, they must have compared their *p* value with a critical *p* value or other "like-with-like" (e.g. *not* say 0.0234 with 1.96), using the correct tail (e.g. *not* –2.61 with +2.576), and the working should in general have accuracy errors only. Thus miscalculation of *z*, comparison with 1.645 instead of 1.96, or using *n* instead of \sqrt{n} , or omission of a continuity correction when it is necessary, are all accuracy errors and the candidate can still gain the last M1 A1. Omission of \sqrt{n} where it is necessary is a method mistake and so gets M0. In hypothesis tests using discrete distributions, use of P(\leq 12) or P(> 12) or P(= 12) when it should be P(\geq 12) is a method mistake and usually loses all the final marks in a question.
- (b) The A1 mark is for interpreting the answer *in the context of the question*, and *without over-assertiveness*. Thus "The mean number of applicants has increased" is over-assertive and gets A0 (although we allow "There is sufficient evidence to reject H₀. The mean number of applicants has increased", A1), and "There is sufficient evidence that the mean has increased" is not contextualised, so that too is A0.
- (c) A wrong statement such as -2.61 > -2.576 generally gets B0 for comparison but can get the subsequent M1A1. Otherwise:
- (d) If there is a self-contradiction, award M1 only if "Reject/Accept H₀" is consistent with their comparison. Thus if, say, we had $z = 2.61 > z_{crit} = 2.576$: "Reject H₀, there is insufficient evidence that the mean number of ... has changed" is M1A0. but "Do not reject H₀, there is evidence that the mean number of ... has changed" is M0A0.
- (e) We don't usually worry about differences between "Reject H_0 " and "Accept H_1 " etc.

()uestio	on	Answer	Marks	Guidance
1			$\hat{\mu} = \bar{x} = 3.65$	B1	3.65 stated explicitly, not isw
			$S^2 = \frac{739.625}{50} - 3.65^2 [= 1.47]$	M1	Correct formula for biased estimate used, award if 1.47 seen
			$\hat{\sigma}^2 = \frac{50}{49}S^2$	M1	n/(n-1) factor used, or if wrong single formula, M1 if $n-1$
			= 1.5	A1 [4]	Answer 1.5 or exact equivalent only
2			Po(4.2)	M1	Po(<i>np</i>) stated or implied
			$e^{-4.2} \frac{4.2^5}{2} = 0.1633$	M1	Poisson formula or tables, allow for .1944, .1144, .16(0), .1663;
			5!	Al	Answer, a.r.t. 0.163
			<i>n</i> large, <i>p</i> small	BI	One condition Needs Poisson. If inequalities
			<i>or</i> $n > 50$, $np < 5$	BI	The other condition \int used, must be these, but allow $p < 0.1$ if and nothing extraneous $n > 50$ already stated
				[5]	
3			$\mu = 60$	B1	$\mu = 60$ stated or implied, can be written down
			$\frac{63.8 - \mu}{1000} = 0.000 = 1.282$	M1	Standardise 63.8 or 56.2 with σ , allow $\sqrt{\sigma}$ or cc errors, equate to
			σ σ σ σ	B1	Φ^{-1}
					1.282 (or 1.281 or 1.28) seen
			$\sigma = 2.96(4)$	A1	σ , in range [2.96, 2.97], can be implied by what follows, <i>not</i> σ ²
			$1 - \Phi\left(\frac{65 - 60}{2.964}\right) = 1 - \Phi\left(1.687\right)$	M1	Standardise 65 with their μ and σ , allow $$ or cc errors
			= 0.0458	A1	Final answer, a.r.t. 0.046, c.w.o.
				[6]	
4			N(2.5, 0.025)	M1	Normal (any – can be implied by standardisation)
			$\Phi(2.59-2.5) = \Phi(0.5692)$	A1	Mean 2.5
			$\left(\Psi \left(\frac{1}{\sqrt{0.025}} \right) \right) = \Psi \left(0.5072 \right)$	A1	Variance or SD $1.25 \div 50$ stated or used
				A1	Standardise 2.59 or 2.61, with $\sqrt{(1.25/50)}$
			= 0.7154	A1	Answer in range [0.715, 0.716] or [0.736, 0.737] from 0.632
				[5]	

5	(i)	(a)	${}^{6}C_{4} 0.6^{4} 0.4^{2} = 0.311[04] = 972/3125]$	M1 A1 [2]	This formula, allow $0.6 \leftrightarrow 0.4$, or tables used correctly Final answer, exact fraction or a.r.t. 0.311
5	(i)	(b)	$^{12}C_4 \times {}^8C_2 \div {}^{20}C_6 [=495 \times 28 \div 38760]$	M1	Product of two ${}^{n}C_{r}$ divided by ${}^{n}C_{r}$, or ${}^{6}C_{2}\left(\frac{12}{20} \times \frac{11}{19} \times \frac{10}{18} \times \frac{9}{17} \times \frac{8}{16} \times \frac{7}{15}\right)$
			= 0.3576 [= 231/646]	A1 [2]	Final answer, exact fraction or a.r.t. 0.358
5	(ii)		$B(60, 0.6) \approx N(36, 14.4)$	B1 B1	$N(36,)$ or $N(24,)$; 14.4 or $\sqrt{14.4}$, both from B(60, 0.6)
			$1 - \Phi\left(\frac{29.5 - 36}{\sqrt{14.4}}\right) = 1 - \Phi(-1.713)$	MI A1	Standardise with their <i>np</i> and \sqrt{npq} (or <i>npq</i>) Both their \sqrt{npq} and cc correct [30,5 if using 24]
			= 0.9567	A1	Answer in range [0.956, 0.957]
			No effect as population is large <i>or</i> yes but not by much	B1 [6]	Need all of one of these [not "sample"], or equiv, nothing wrong
6			$H_0: \lambda = 6.3 [or \mu]$	B2	Both: B2. One error e.g. " $H_0 = 6.3$ ", or " H_1 : $\lambda \neq 6.3$ ", B1,
			$H_1: \lambda < 6.3 [or \ \mu]$		but x , r etc: 0
			$P(\le 2) = e^{-6.3}(1 + 6.3 + 19.845)$	M1	Correct formula for at least 2 terms, can be implied by 0.0134
			0.0400	A1	Fully correct formula for ≤ 2 , can be implied by answer
			= 0.0498 < 0.05	A1 B1	Answer, a.r.t. 0.0498 SR tables: B2 if a.r.t. 0.0506, else 0 [then can get B1M1A1] Explicitly state < 0.05, <i>not</i> from H ₁ : $\lambda \neq 6.3$, or CR ≤ 2 and explicitly state 2 in CR, needs essentially correct distribution Not needed for final M1A1
			Therefore reject H_0 .	M1	Correct method, comparison and first conclusion
			Significant evidence that average number of pips has been reduced	A1√	Interpreted in context acknowledging uncertainty somewhere, $\sqrt{0}$ on n etc.
				[8]	$\begin{array}{c} p \ \text{etc} \\ \text{SR: } P(<2) \ [0.0134] \ \text{or Po}(=2) \ [0.0364]: \\ \text{but } allow \ \text{``Po}(=2) = 0.0498 \ \text{``etc} \\ \text{SR: } \text{Normal: } B2 \ \text{M1 A0 B0} \end{array}$

7	(i)	(a)	$\int_{1}^{4} \frac{1}{2\sqrt{x}} x dx = \left[\frac{1}{3} x^{\frac{3}{2}}\right]_{1}^{4} = 7/3 \text{ or } 2.333$	M1 B1 A1 [3]	Attempt to integrate $xf(x)$, correct limits Correct indefinite integral, a.e.f. Final answer 7/3 or equiv or a.r.t. 2.33					
7	(i)	(b)	$\int_{1}^{m} \frac{1}{2\sqrt{x}} dx = 0.5$ \sqrt{m-1} = 0.5 m = 2.25	M1 A1 A1 [3]	This or complementary integral, limits needed [not "- ∞ "], equated to 0.5, needn't attempt to evaluate This equation, any equivalent simplified form Answer 9/4 or exact equivalent only					
7	(ii)		$1.5 \int_{1}^{\infty} y^{-2.5} y^{2} dx = 1.5 \left[\frac{y^{0.5}}{0.5} \right]_{1}^{\infty}$ Upper limit gives infinite answer	M1 B1 A1 [3]	Attempt to integrate $y^2 f(y)$, limits 1 and ∞ , allow any letter Correct indefinite integral $[=3\sqrt{y}]$, ignore μ [= 3] Give correct reason, c.w.o. apart from constant, allow "= ∞ "					
8	(i)		Location of bacteria must be independent – the position of one does not affect that of another	f bacteria must be independent – the position of one fect that of another M1 "Found independently": M1. Allow "are independen						
			 Examples α Number of bacteria occurring in a particular volume is inder Number in one volume occurs randomly. β Bacteria are distributed independently from one another. The Position of each bacterium must be independent of the position of each bacterium must be independent of the position of each bacterium must be independent of the position of each bacterium must be independent of the position of each bacterium must be independent of the position of each bacterium must be independent of the position of each bacterium must be independent of the position of each bacteria by the surrounding bacteria must not be independent. The results of one cannot β Bacteria must occur independently, so the state of one bacteria for the probability of bacteria must be independent, they cannot af η Bacteria must occur independently, so if one occurs it can't 	[2] of bacteria occurring in a particular volume is independent of the number in another interval of the same volume. in one volume occurs randomly. are distributed independently from one another. This means that they cannot be in groups. of each bacterium must be independent of the position of other bacteria. Not well modelled by Poisson if they tended t hey must not be influenced by the surrounding bacteria or certain conditions (e,g, heat). need to be independent. The results of one cannot influence the result of another. must occur independently, so the state of one bacterium has no effect on any other bacteria. ity of bacteria must be independent, they cannot affect the probability of another bacterium occurring.						

8	(ii)	$1 - P(\le 4) = 1 - 0.8912$	M1	Allow M1 for 19580 [= 0.042] or wrong λ . 0.8912 etc: M0
		= 0.1088	A1	0.109 or 0.1088 or better
			[2]	
8	(iii)	Po(0.925)	M1	Po(0.925) stated or implied [37/40]
		$-0.925 0.925^2$ 0.1(0(64)	M1	Correct Po formula for $r = 2$, any λ , can be implied by:
		$e^{-0.109(64)}$ = 0.109(64)	A1	Answer 0.17(0) or 0.1696 or better
			[3]	
8	(iv)	Po(250)	B1	Po(250) stated or implied
		$\lambda > 15 \text{ or } \lambda \text{ large [or } \mu \text{]}$	B1	Either of these
		N(250, 250)	M1*	N, mean their $100 \times 2.5 \dots$
			A1√	variance (or SD) their mean
		(239.5 - 250)	Dep*M1	Standardise, allow wrong or no cc and/or no $\sqrt{10}$ or σ^2 , needs A1
		$\Phi = 1 - \Phi(0.664)$	A1√	Continuity correction and $\sqrt{\text{correct}}$
		- 0 2533	Δ1	Final answer a r t 0.253 c w o
		- 0.2355	[7]	1 mai answei a.i.t. 0.255, c.w.0.
0			[/]	
9	(1)	$H_0: \mu = 8; H_1: \mu \neq 8$	B 2	Both, B2. One error, B1, allow $x/r/t$ here, but not H
		where μ is the population mean amount of sleep obtained by	B1	Need "population" or equivalent, but allow "average amount of
		Year 11 pupils		sleep obtained by Year 11 pupils". Allow " μ is population mean".
			[3]	
9	(ii)	$\Phi(0.28) = \Phi(2.575)$	M1	Standardise, with \sqrt{n} or <i>n</i> , allow cc, \sqrt{r} errors
		$\Phi\left(\frac{1}{0.87/\sqrt{64}}\right)$	A1	<i>z</i> = 2.575 or 2.57 or 2.58, can be implied by, e.g., 0.005 or 0.995
		$2 \times (1 - above)$	M1	Correct handling of tails
		= 0.01 or 1%	A1	Answer 0.01 or 1% correct to 2 SF, c.w.o.
			[4]	
9	(iii)	Rejecting H_0 when $\mu = 8$	B1	Or equivalent, some mention of context, not "probability of"
			[1]	
9	(iv)	(8.28-7.9) $(7.72-7.9)$	M1	Find P(between 7.72 and 8.28 μ = 7.9), allow 1 – 2×P(1 tail)
		$\Psi\left(\frac{1}{0.87/\sqrt{64}}\right)^{-\Psi}\left(\frac{1}{0.87/\sqrt{64}}\right)$		(need attempt to find correct region, <i>not</i> isw – i.e., <i>not</i> ans 0.049)
1		$= \Phi(3.494) - \Phi(-1.655) $ [= 0.99976 - (1 - 0.951) or 1]	M1	Correct handling of tails, needn't attempt to evaluate, needs 64
		= 0.951	A1	Final answer, a.r.t. 0.951.
			[3]	SR: One tail only used: M1M0A0. 0.951 from no working: B2

Question		n	Answer	Marks	Guidance			
1			Number CDs (sequentially) Select using random numbers	B1 B1	List needn't be stated, but must mention CDs. <i>Not</i> "select numbers randomly". Hat, etc: B1B0	Assume sequential unless stated otherwise. If "number CDs randomly", B1 max unless		
				[2]	Systematic: 66 or 67 B1, random start B1	"sort by number". Stratified: apply scheme		
2	(i)		$\left(\frac{71.2 - 72.0}{\sigma / \sqrt{40}}\right) = -0.3853$	M1 A1 B1	Standardise with Φ^{-1} & $\sqrt{40}$, allow cc, $\sqrt{\text{errors eg }\sigma^2}$ Square roots and sign correct, no cc, no "1 –" error z in range (±) [0.385, 0.386] seen	RHS must be Φ^{-1} , i.e. <i>not</i> 0.7411 or 0.2589 or 0.6368 or 0.35. "1 –" error or ×40/39: M1A0 [0.674 may be from "1 – 0.35 = 0.75"]		
			$[\sigma = 13.13,]$ Var(V) = 172.4	A1 [4]	<i>Final</i> answer in range [172, 173], or 13.1 ² cwo	Needs variance, not SD NB: Look out for $-13.1 \rightarrow 172$, M1A0B1A0		
2	(ii)		Parent distribution not known <i>n</i> is large	B1 B1 [2]	Or clear equivalent. Not " <i>sample</i> not normal" Or clear equiv, e.g. sample size > 30. Extras: max 1 " <i>n</i> large, $n > n_0$ ": B1 if $n_0 \ge 30$.	Don't bother about order of these statements. If numerical must be 30. Ignore "continuous".		
3		α:	H ₀ : $p = \frac{1}{3}$ [or 0.33 or better] H ₁ : $p \neq \frac{1}{3}$ [or 0.33 or better] B(12, $\frac{1}{3}$) stated or implied P(\geq 7) = 1 - 0.9336 = 0.0664 > 0.025	B2 M1 A1 A1	Allow π , but $\mu = \frac{1}{3}$ etc B1. Any other letter, B0 One-tailed, or no symbol, B1 max B(12, $\frac{1}{3}$) stated or implied, allow for N(4,8/3), Po(4) Probability in range [0.066, 0.067] Explicit comparison with 0.025, or 2 <i>p</i> with 0.05	Not $\mu = 4$ (<i>if in doubt, consult</i>) <i>If N used, or P</i> (\leq 7) <i>or P</i> ($=$ 7), <i>no more marks</i> 1-tailed: A0 here regardless of value		
		β:	CR is \geq 8, 7 not in CR Probability is 0.0188 Do not reject H ₀ . Insufficient evidence that statement is false.	A1 A1 M1 A1√	Needs explicit comparison of 7 with CV Must be \geq 7, 0.019 or 0.0188 or better, allow 0.9812 Needs correct method, including like-with-like, correct tail, \geq 7 (or \leq 6). If CV, needs right tail A1 needs "evidence" or equivalent. "Statement" is enough context here	Need to be clear that CR is being used – look for comparison with 7. See also ζ . Allow from 1-tail. 0.9812 or 0.0188 or 0.0476: M0 unless " \geq 7" stated or clearly using β . on their <i>p</i> /CR. Withhold if answer refers only to <i>p</i> .		

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	Question		Answer	Marks	Guidar	nce
4	(i)		Crystals must occur	B1	Allow interpreted, or "randomly" but nothing else.	Ignore "singly" (meaningless in this context).
			independently of one another		Must be contextualised; no other answers included.	But allow "probability is independent"
				[1]		
4	(ii)		-323.2^5 - 0.114(0)	M1	Formula, or .0608 or .1781 or .1075 or .1203	
			$e^{52} - \frac{1}{5!} = 0.114(0)$		(tables)	
			5.	A1	Answer a.r.t. 0.114, implies both marks	
				[2]		
4	(iii)		Po(2.368)	M1	$Po(0.74 \times 3.2)$ stated or implied	Allow for 0.75×3.2 etc, e.g. Po(2.4)
			$1 - e^{-2.368} (1 + 2.368 + \frac{2.368^2}{2})$	M1	1 – correct Poisson terms, their λ , allow ± 1 term	Don't allow second M1 from λ in tables, e.g. if MR, treat as E-1.
			= 0.4219	A1	Answer, a.r.t. 0.422, implies all 3 marks	If no working: don't give M1A0
				[3]		
4	(iv)		$Po(32) \approx N(32, 32)$	M1	N(λ , λ) stated or implied, allow $\sqrt{\lambda}$ or λ^2 for var	Needs $\lambda \ge 15$
				A1	N(32, 32), allow $\sqrt{32}$ or 32^2 for var	
			(35.5-32)	M1	Standardise with λ and $\sqrt{\lambda}$ or λ , allow cc errors but	Can get (M0A0) M1A1 from $\lambda < 15$
			$1-\Phi\left(\frac{1-\sqrt{32}}{\sqrt{32}}\right)$	A1	not \sqrt{n} ; both cc and $\sqrt{\text{correct}}$	Typically, no cc \rightarrow 0.2203, or 32 \rightarrow 0.4565, 3/5 (but needs evidence, not just answer)
			$= 1 - \Phi(.619) = 0.2681$	A1	Final answer, a.r.t. 0.268	
				[5]		

C)uesti o	n	Answer	Marks	Guidance			
5			H ₀ : $\mu = 6.1$	B2	Both: B2. One error, B1, but \overline{x} , x, r etc: 0. 6.2: B0			
			$H_1: \mu \neq 6.1$					
			$\hat{\mu} = \overline{x} = 6.2$	B1	6.2 [31/5] seen somewhere (other than hypotheses)			
			$\hat{\sigma}^2 = \frac{80}{72} \left(\frac{3126}{22} - 6.2^2 \right) = 0.643$	M1	Correct formula for biased estimate [0.635 or 127/200]	If single formula used, M2 or, if wrong, allow M1 for divisor 79 anywhere		
			79(80)	M1	Divide by 79 somewhere			
		α:		A1	Variance estimate, a.r.t. 0.643, can be implied	[254/395 leading to 127/15800]		
			$z = \frac{6.2 - 6.1}{1.115}$	M1	Standardise their 6.2 with reasonable variance	80 needed, otherwise M0 and no more marks		
			$\frac{1}{\sqrt{0.643/80}}$		attempt, needs 80, allow cc	If clearly $\mu = 6.2$ used, no more marks		
			$[1 - \Phi(1.115) = 0.1325 > 0.05]$	A1	$z \in [1.11, 1.12] \text{ (not -) or } p \in [0.1323, 0.1333]$	A1 uses number used for comparison		
			1.115 < 1.645	A1	Compare z with 1.645 (allow -1.645 if $z < 0$)	Withhold if inequality incorrect or if 1-tailed		
					or <i>p</i> (< 0.5) with 0.05	Must be consistent signs/tails and like-with- like		
[$CV \in 1 + 1 \in 45 \times 0.643$	M1	$6.1 + z\sqrt{(\sigma^2/80)}$, allow \pm , $\sqrt{\text{errors}}$	Allow $6.2 - (\text{or } \pm)$ but no more marks		
		ß٠	C = 6.247 and 6.2 < 6.247	A1	CV, a.r.t. 6.25, needs $z = 1.645$, allow biased $\hat{\sigma}^2$	afterwards		
		р.		A1√	Compare 6.2 with CV from + sign, $\sqrt{\text{ on } z}$	If no 79 earlier but used here, recovers M1A1		
					(but not σ)	E.g. $1.96 \rightarrow 6.276 \text{ or } 1.282 \rightarrow 6.215 \text{ [gets]}$		
			Do not roject H	M1	Needs assentially correct method and comparison	First conclusion wrong: M0A0 even if second		
			Insufficient evidence that pH	1011	needs 80 but no need for correct variance	correct		
			value is not 6.1	A1√	Needs context and "evidence" or equivalent, ft on	"1.115 > 1.645 so do not reject H_0 " etc:		
					their $z/p/CV$	(A0)M1A1		
				[11]				
Not	es:		Biased estimate used : typically	gets	\overline{x} and μ interchanged: allow final M1A1 if <i>anywhere</i>	e right, but if always wrong (in hypotheses and z)		
			B2B1 M1M0A0 M1A0A1 M1A	A 1	M0A0. This would typically get B0B0B1 M1M1A1 M	M1A0A0 M0A0		
			[total 8]		[total 5]			

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6 (i) B(32, 0.4) $\approx N(12.8, 7.68)$ B1 $\approx N(12.8, 7.68)$ B(32, 0.4) stated or implied, e.g. by Po(12.8) N(their attempt at np, npq); N(12.8, 7.68) Poisson [0.09888], or exact [0.0462] Valid as 12.8 and 19.2 > 5 (17.5 - 12.8) B1 M1 B(32, 0.4) stated or implied, e.g. by Po(12.8) N(their attempt at np, npq); N(12.8, 7.68) Poisson [0.09888], or exact [0.0462] SC: B(12.8, 7.68/32): M1A0 Or "n large and p close to 0.5". Not npq or 7.68 > 5. (17.5 - 12.8) Allow np and nq both asserted > 5	59]:B1max
$\approx N(12.8, 7.68)$ Valid as 12.8 and 19.2 > 5 $\begin{pmatrix} M1A1 \\ B1 \\ (17.5-12.8) \end{pmatrix}$ M1A1 N(their attempt at <i>np</i> , <i>npq</i>); N(12.8, 7.68) \\ Or " <i>n</i> large and <i>p</i> close to 0.5". Not <i>npq</i> or 7.68 > 5. Allow <i>np</i> and <i>nq</i> both asserted > 5 (17.5-12.8) + M1 Standardise, their <i>np</i> , <i>npq</i> , allow wrong/no cc + 32: M0	
Valid as 12.8 and $19.2 > 5$ B1Or "n large and p close to 0.5". Not npq or 7.68 > 5.Allow np and nq both asserted > 5 $(17.5 - 12.8)$ M1Standardise, their np, npq, allow wrong/no cc $\div 32$: M0	
$(17.5-12.8)$ M1 Standardise, their <i>np</i> , <i>npq</i> , allow wrong/no cc $\div 32$: M0	
$1 - \Psi\left(\frac{1}{\sqrt{7.68}}\right)$ or no $\sqrt{1}$	
A1 17.5 and \sqrt{npq} correct	
$[= 1 - \Phi(1.696)]$ = 0.0449 A1 Answer, a.r.t. 0.045	
[7]	
6 (ii) $B(90, 0.01)$ B1 $B(90, 0.01)$ stated or implied. Exact [0.049003]: B1 max.	
$\approx Po(0.9) \qquad \qquad M1 \qquad Po(\text{their attempt at } np) \qquad \qquad Don't \text{ treat } p = 0.1 \text{ as MR. If } np > 5$	M0M0
M1 Correct formula or use of tables, e.g. 0.1646 or No working, wrong answer \Rightarrow M0A	0, but
$1 \qquad e \qquad \underline{3!} \qquad 0.0112 \qquad \qquad \text{right answer} \Rightarrow M1A1 \text{ provided cle}$	rly Po
A1 Final answer in range [0.049, 0.05) [i.e., not 0.05] SC: B(90, 0.1), N(9, 8.1), [0.015, 0.1] cwo B2)16]
[4]	
7(i)M1Positive parabola (only), through 0, nothing below $k < 0$: M0 even if $k > 0$ as well.	
x-axis	
Values of X A1 Clear truncation at ends Don't need any scales, vertical line	it a etc.
Can be vertical at A, needn't be hori	zontal at
$\square \square $	
than those B1 Withhold if concept misunderstood. Need to have E.g.: "More likely to <i>occur</i> for x clo	se to a ":
close to 0 probability of <i>values</i> (not of <i>occurring</i>); not just B0.	
shape. Allow for U-shape but nothing else Ignore extra comments like "expone	ntial"
$\begin{bmatrix} 7 \\ (11) \\ (1) \\ (1$	
$J_0 = a^3$ AI Correct limits and equate to I	
$ \int_{a}^{a} \frac{3}{x^{3}} dx = - \Rightarrow a = 6 $ M1 Attempt to integrate kx ³ , ignore limits Must attempt integration	
A1 Correct limits and equate to 4.5 Don't need k in terms of a here	
A1 One correct equation connecting k and a, can be $ka^3 = 3$ or $ka^4 = 18$, a.e. simplified for implied	rm
A1 Correctly obtain $a = 6$ only No marks explicitly for $k = 1/72$ or	
[6]	

(Question		Answer	Marks	Guidar	ince	
7	(ii)	(b)	$\int_{0}^{6} \frac{1}{72} x^{4} dx \qquad [=\frac{108}{5}]$ 21.6 - 4.5 ² = 1.35	M1 A1 A1 [3]	Attempt to integrate kx^4 , their <i>a</i> , <i>k</i> , can be algebraic Subtract 4.5 ² (given in question) 1.35 or exact equivalent only	Must attempt integration; limits 0, a Somewhere [=27/20]	
8	(i)		$30 + 1.645 \times \frac{8}{\sqrt{18}} = 33.102$ so CR is $\overline{X} > 33.1$	M1 A1 A1 A1√ [4]	$30 + z \times 8/\sqrt{18}$, allow $\sqrt{\text{errors, cc}}$ 1.645, requires + only 33.1 a.r.t. 33.10 ≥ their RH CV $$, allow ≤ their LH CV <i>as well</i> , allow >, allow no letter or X but no other letter	Allow \pm but not – only. No 18: 0 in this part. Don't allow "accept if \leq 33.1, reject if $>$ 33.1" Inequality required in final line	
	(ii)		Type I [error]	B1	Nothing else unless it's just an amplification. Allow "Type 1"		
	(iii)		B(20, 0.05): P(\geq 4) = 0.0159 so unlikely that μ = 30	M1 A1 A1√ [3]	B(20, 0.05) stated or implied. Not B(20, 1/5) Probability, a.r.t. 0.016 Justified conclusion, e.g. "I think $\mu = 30$ as not less than 0.01". FT on their <i>p</i> .	No reason: A0. Not over-assertive. But "I think $\mu = 30$ as probability is small" is A0.	
	(iv)		$\frac{33.1 - \mu}{8 / \sqrt{18}} = -0.253$	M1 A1 A1	Needs Φ^{-1} , their CV, SD right or same as in (i), allow cc Signs correct, can be implied by answer > their CV z in range (±)[0.25, 0.26]	Not 30. Allow omission of $\sqrt{18}$ only if omitted in (i). "1 –" errors: can get M1A0A1	
			$\mu = 33.58$	A1 [4]	Final answer $33.55 \le \mu \le 33.60$, 4 SF needed.	Typically 32.62 probably gets 2/4.	

Q	Question		Answer	Marks	Guidance			
1			<i>n</i> = 9	B1	Stated explicitly			
			CR is ≤ 2	M1A1	2 seen but not \leq : M1A0. Allow "P(\leq 2)"	CR must be stated explicitly for A1		
			0.0083	A1	Or more SF.	SR: ≤ 3 with 0.0424: (B1)M1A0		
					" <i>n</i> = 9, CR ≥ 3", 0.0083 seen: B1M1A0A1	SR: If 0, give B1 for at least 3 of		
						0.0083, 0.0113, 0.0026, 0.0197, 0.0034		
				[4]		seen		
2	(i)		$\hat{\mu} = \overline{x} = 38$	B1	38 stated separately			
			Σx^2 28 ² [-16.2]	M1	Use of $\sum x^2/n - \overline{x}^2$	Correct single formula: M2		
			$\frac{10}{10} - 58$ [= 10.2]	M1	Multiply by 10/9	If single formula, divisor of 9 seen		
			×10/9 to get 18	Al	18 or a.r.t. 18.0 only	anywhere gets second M1		
				[4]				
2	(ii)		(40-38) (0.4714) 0.2107	M1	Standardise with their μ and σ , allow cc,	$\sqrt{10}$ used: M0.		
			$\left[\Phi \left(\frac{1}{\sqrt{18}} \right) = \Phi \left(0.4/14 \right) = 0.3187 \right]$		$\sqrt{\text{errors}}$			
				A1	Answer, a.r.t. 0.319	Allow a.r.t. 0.311 [0.3106] from 16.2		
				[2]				
3	(i)		Allocate 4-digit number to each DVD;	B1	"DVD" & "4 digits/1 to 9000/sequentially"	<i>Not</i> allocate "random" numbers, unless		
					etc must be mentioned somewhere	subsequently sorted		
			Select using random numbers	B1	Mention random numbers	If "pick random numbers in range 1 to		
			Ignore random numbers outside range	B1	Unbiased method, mention of "outside	9000", must mention repeats		
				[2]	range" or "repeats"			
-	(••)							
3	(11)		$B(100, 0.24) \approx N(24, 18.24)$	MI	N(attempt at <i>np</i>)			
			$\Phi\left(\frac{19.5-24}{2}\right) = \Phi(-1.0537)$	Al	Both parameters correct	Allow 18.24/100 A1 but then MOA0		
			√18.24)		Standardise with their np and \sqrt{npq} or npq	Allow cc/v errors.		
			- 0 1/61		Both cc correct and $\forall npq$ used			
			- 0.1401		Answer, a.r.t. 0.146			
				[5]				

	Question		Answer	Marks	Guidance		
4	(i)		Values taken by X	B1	This answer only	Not "values taken by f"	
				[1]			
4	(ii)		$\int_{a}^{a} h du = 1 \implies h = 2$	M1	Use definite integral and equate to 1,	Or clear argument from triangle area	
			$\int_0^{\infty} kx dx - 1 \rightarrow k = \frac{1}{a^2}$	A1	Correctly obtain $2/a^2$		
				[2]			
4	(iii)		$\begin{bmatrix} a \\ a \end{bmatrix} = \begin{bmatrix} r^3 \end{bmatrix}^a = 2$	M1	Attempt to integrate $xf(x)$, limits 0 and a		
			$\int_{0}^{0} kx^{2} dx = \left k \frac{x}{2} \right = \frac{2}{3} a$	B1	Correct indefinite integral seen	either here or for $x^2 f(x)$	
				A1√	Correct mean <i>or</i> correct $E(X^2) = a^2/2$,	Can be in terms of <i>k</i>	
			$\int_{a}^{a} k x^{3} dx = \left[\int_{a} x^{4} \right]^{a} a^{2}$		$\sqrt{\mathrm{on}k}$		
			$\int_{0}^{\infty} k dx \qquad \left\lfloor \frac{k}{4} \right\rfloor_{0}^{\infty} = \frac{1}{2}$	M1*	Attempt to integrate $x^2 f(x)$, limits 0, <i>a</i>		
			a^2 ()?		2		
			$\frac{a}{2} - (\frac{2}{3}a)^2 = \frac{1}{18}a^2$	depM1	Subtract their μ^2		
			2	A1	Correct final answer, ae exact f, no k now	Or decimal, $0.056a^2$ or better	
				[6]			
5	(i)		$Po(4200) \approx N(4200, 4200)$	M1	Po(60 λ) stated or implied		
			$1 = \frac{1}{2} \left(4350.5 - 4200 \right)$	M1	$N(60\lambda, 60\lambda)$,	
			$1 - \Phi \left(\frac{1}{\sqrt{4200}} \right)$	M1	Standardise with their 60λ and $\sqrt{60\lambda}$ or 60λ	Allow wrong or no cc, or no $$	
			$1 - \frac{1}{2} = 0 - \frac{1}{2} = $	Al	4350.5 explicitly seen and $\sqrt{60\lambda}$ not wrong	$\sqrt{60\lambda}$ needn't be explicit	
			$= 1 - \Psi(2.322) = 0.010(1)$	Al	Answer, allow a.r.t. 0.010	Allow [0.0103, 0.0106] from no CC,	
						but <i>not</i> 0.0105 from wrong CC	
				[5]			
5	(ii)		B(30, 0.010(1))	M1	B(30, their (<i>i</i>)) stated or implied		
			$\approx Po(0.30(3))$	Al	Po(0.3) or 0.303 etc	[0.30→0.000266. 0.303→0.000276.	
			1 - 0.9997 = 0.0003	Al	Final answer a.r.t. 0.0003	0.309→0.000297]	
			$or: 1 - (q^{30} + 30q^{29}p + 435q^{28}p^2 + 4060q^{27}q^3)$		Exact binomial: $1 - (3,4 \text{ or } 5 \text{ terms}) (M1)M1$	Needs clear ${}^{n}C_{r}$ or right answer	
			= 1 - (.7397 + .2242 + .0328 + .0031)		Answer a.r.t. 0.0002: A1	No mention of dist: assume exact	
			= 1999777 = 0.0002226		Normal (0.3, 0.297) (M1)M1		
					Answer 0 (4 dp) ($z = 5.87$) A1		
				[3]			

Q	Question	Answer	Marks	Guidance	
6	(i)	$H_0: \mu = 28.0$	B2	One error, e.g. p , or μ_0 , μ_1 , or 2-tail: B1.	But \overline{x} etc: B0
		H ₁ : $\mu > 28.0$ α : $\frac{28.98 - 28}{12/\sqrt{30}} = 0.4473 \ [p = 0.3274]$ z < 1.645, or $p > 0.05OR: CC: 28.98 - \frac{1}{60} \rightarrow 0.4397, p = 0.33$	M1 A1 A1	Standardise with $\sqrt{30}$, allow $\sqrt{\text{errors}}$, cc Correct value of z or p: $z = \text{art } 0.447$ or p in range [0.327, 0.328] Compare z (incl 30) with 1.645, or p with 0.05, or with 0.95 if correct tail	CC is CORRECT here Not -0.447 but can be recovered if 0.327 used. Not $0.455/0.3246$ Needs μ and \overline{x} right way round
		$\beta: \qquad 28 + 1.645 \times 12/\sqrt{30} \\ = 31.6 \\ 28.98 < 31.6 \end{cases}$	M1 A1√ A1	$28 + z \times 12/\sqrt{30}$, allow $\sqrt{\text{errors}}$, cc Correct CV, $\sqrt{\text{on } z}$ (only) Explicitly compare 28.98	Ignore 28 –, do not allow 28.98 –
		γ : Totals used: $\frac{869.4 - 840}{12\sqrt{30}} = 0.4473$		Same scheme	NB: If totals used, allow ANY plausible CC or none
		Do not reject H_0 . Insufficient evidence of an increase in mean score	M1 A1	Consistent first conclusion Contextualised, "evidence" or exact equivalent somewhere	Needs correct method & comparison, 30 used, μ and \overline{x} right way round "Evidence" in either part of conclusion
		SD unchanged, or random sample/indept	B1 [8]	One of these seen, nothing irrelevant	
6	(ii)	Yes because population not stated to be normal	B2 [2]	Partial answer: B1 "Yes as parent distribution not normal" (i.e., "stated to be" omitted): B2 SR: "No as assumed normal" if in (i): B1	"Yes, because <i>n</i> large": B1 "Yes, as not normal and <i>n</i> large": B1 "Yes as not normal, but can be used as <i>n</i> large": B2
7	(i)	$\frac{\mu - 20}{\sigma / \sqrt{n}} = 1.0; \frac{35 - \mu}{\sigma / \sqrt{n}} = 2.0$ Solve to get $\sigma = 5\sqrt{n}$	M1 A1 B1 M1 A1 [5]	Standardise either 20 or 35, equate to Φ^{-1} Both equations completely correct Both correct <i>z</i> -values seen (to 3 SF at least) Correctly obtain $\sigma = k\sqrt{n}$ or $\sigma^2 = kn$ $\sigma = 5\sqrt{n}$ or $\sqrt{25n}$ only.	With \sqrt{n} or <i>n</i> and <i>z</i> , allow "1–", cc Including signs, but can have wrong <i>z</i> Independent of previous marks Allow $\sqrt{1}$ errors, ALLOW from not Φ^{-1} [only mark from 0.7998 & 0.8358]
7	(ii)	Binya is right $\mu = 25$ $1 - \Phi\left(\frac{32 - \mu}{5}\right) = 1 - \Phi(1.4)$ = 1 - 0.9192 = 0.0808	B1 B1 M1 A1 [4]	Binya stated $\mu = 25$ following no wrong working Standardise with their σ/\sqrt{n} and their numerical μ Answer, a.r.t. 0.081, CWO.	"Aidan" used: max B0B1M0 But allow if \sqrt{n} omitted or wrong NB: use of 1.282 probably implies "Aidan"

(Juestio	n Answer	Marks	Guidance		
8	(i)	Failures do not occur at regular or	B1	Not equivalent of "independent".	Both right and wrong: B0	
		predictable intervals		<i>Not</i> "equally likely at any moment"		
			[1]			
8	(ii)	Failures occur independently;	B1	"Failures" needed in one reason, else B0(B3)	<i>Not</i> "randomly", allow "singly" only if	
		Might not happen if a power cut	B1	Plausible reason	also "independent" in this part	
		and at constant average rate;	B1	Exact equivalents only	Not "equal probability", not "constant	
		Might not happen if manipulated to change	B1	Must be during one day and not week/year	rate", but allow second mark if OK.	
		more rapidly at peak times		Allow any answers that show correct	Extra wrong reason loses explanation	
				statistical understanding, however	mark	
			E 4 1	implausible		
0	(;;;)	27 28	[4] M1	At least one correct formula		
o	(111)	$e^{-\lambda} \frac{\lambda}{\pi} = e^{-\lambda} \frac{\lambda}{2} \Longrightarrow \lambda = 8$		Both sides correct		
		7! 8!	M1	Cancel exp and some λ		
			A1	Obtain $\lambda = 8$ only CWO		
		0.1396	B1√	Answer in range [0, 139, 0, 14] $\sqrt{100}$ on their λ	[before rounding]	
			[5]			
9	(i)	4.81% or 0.0481	B1	One of these only, or more SF	$N(18, 7.2) \rightarrow 0.0468$: B1	
	~ /		[1]			
9	(ii)	$P(\geq 14) = 0.7077$	M1	Allow M1 for answer 0.5722 or 0.8192	0.2923: 0	
			A1	0.708 or 0.7077 or more SF	$N(15, 7.5) \rightarrow 0.78$: M1A1;	
			[2]		0.8194 or 0.7674: M1A0	
9	(iii)	Only way that $p = 0.5$ for second test is if	M1	$0.2 \times 0.7077 \times 0.2923$ [= 0.04137]	Normal:	
		Type II error on first, where	M1	Consider 1 – 0.14154	$0.1416 \times 0.292 + 0.8584 \times 0.0468$ or	
		$0.2 \times 0.7077 = 0.14154$. Therefore	M2	$0.2 \times (ii) \times (1 - (ii)) + (1 - [0.2 \times (ii)]) \times (i)$	0.00175+0.03569+0.00273+0.04135	
		$0.14154 \times 0.2923 + 0.85846 \times 0.0481$		[= 0.04137 + 0.04127]	= 0.0815: full marks	
		= 0.0827	Al	Answer, a.r.t. 0.083		
				$0.8 \times 0.0481 \times 0.0481 [0.00185]$	Any two of these three M1	
				$+0.8 \times 0.9519 \times 0.0481$ [0.03663] MI	Third of these three M1	
				$+0.2 \times 0.2923 \times 0.0481$ [0.00281] MI	This one M1	
				$+0.2 \times 0.7077 \times 0.2923$ [0.04137] MI		
1				Add up 4 terms of 3 multiplications MI	SR: No 0.8 or 0.2 but 2 products: M1	
1			[5]	Answer 0.0827 A1	4 products: M2	

	Juestic	n	Answer	Marks	Guidance	
1	(i)		89, 90, 91, 91, 92	B2	All correct; B2; one error (e.g. all –1), B1	Allow 088, etc
				2		
	(ii)		Not all equally likely (91 more than 90 etc)	B1	Imply different likelihood/probability	Not "same pupil is selected twice"
			Multiply by 1000 and ignore if > 853	B1	Or equivalent method. Not "ignore repeats".	Number students, use random numbers
					Ignore extras.	and ignore outside range: B1
				2		
2			$Po(2 \times 10^{\circ})$	M1	N(their 40λ)	
			$\approx N(2 \times 10^6, 2 \times 10^6)$	A1	Both parameters correct, allow $\sqrt{1}$ here	
			$\Phi\left(\frac{1998999.5 - 2 \times 10^6}{1000000000000000000000000000000000000$	A1	Standardise, mean 40 λ , sd $\sqrt{40\lambda}$ (not 40 λ)	Correct cc must be seen for this A1
			$\sqrt{2 \times 10^6}$			
			= 0.2396	A1	Answer, a.r.t. 0.240	NB: no cc gives $\Phi(-0.7071)$, 0.23975,
					(no cc: M1A1A0A1)	wrong cc gives Φ(-0.70675), 0.23986
				4		
3	(i)		$\frac{\mu - 157.18}{\mu - 1.282} = 1.282 \cdot \frac{\mu - 164.76}{\mu - 164.76} = 0.5244$	M1	Standardise once with $\sqrt{80}$ or 80 and z, signs	Allow cc, but <i>not</i> 0.1, 0.7, 0.9, 0.3 or
			$\sigma/\sqrt{80}$ = 1.202, $\sigma/\sqrt{80}$ = 0.5244		may be wrong, allow "1–" errors	Φ (these) [= .5398, .758, .8159, .6179]
				A1	Both correct <i>including signs</i> , no cc	z may be wrong (provided it <i>is</i> z)
				B1	1.28(155) seen anywhere, correct to 3 SF	Ignore signs
				B1	[0.524, 0.525] seen anywhere	Ignore signs
			Solve simultaneously: $\mu = 170$	A1	μ , a.r.t. 170 to 3 SF (169.98)	CWO×2 but allow from inaccurate z if
			$\sigma = 89.44$	A1	σ , in range [89, 90], <i>not</i> isw	answer(s) within limits. Look out for
					<i>Don't</i> allow surds, e.g. $40\sqrt{5}$	-89.44: A0A0
				6		
	(ii)	(a)	In using normal tables	B1	Or equiv, e.g. "standardising", "dist of \overline{Y} "	Any reference to $\sigma/\sqrt{80:B0}$
		(b)	Parent distribution not known	B1	Allow "it is not normal", etc	No extras
		(c)	<i>n</i> large, nothing wrong seen	B1	If numerical, must be of the form " $n > n_0$ " or	<i>Not</i> " \geq 80".
			[must be in correct order, no repeats]		" $n \ge n_0$ " with $30 \le n_0 \le 60$	
				3		

C)uesti o	n	Answer		Marks	Guidance	
4			$H_0: \lambda = 3.2 \text{ (or } 0.32)$	[Allow μ]	B2	Both correct, B2. One error, e.g. wrong/	But x, \overline{x} , r, t etc: B0. E(X), words: B1
			$H_1: \lambda > 3.2 \text{ (or } 0.32)$	[Allow μ]		no/different symbols, or two-tail, B1	E.g. H_0 : $\lambda_0 = 3.2$, H_1 : $\lambda_1 > 3.2$: B1
			$R \sim \text{Po}(3.2)$		M1	Stated or implied, e.g. N(3.2, 3.2)	$P(= 6)$ or (≤ 6) or > 6 or normal:
			α : P($R \ge 6$) = 0.1054		A1	[0.105, 0.106] before rounding	no more marks, maximum B2M1.
			> 0.01		A1	Explicit comparison with 0.01	
			β : CR \geq 9		A1	$CR \ge 9$ stated; allow $CV = 9$ if comparison ft	
			and $6 < 9$, with probabilit	y 0.0057	A1	0.0057 or 0.9943 seen, and 6 compared	
			Do not reject H ₀ . Insufficient ev	idence of an	M1	Consistent first conclusion	needs correct method and like-with-
			increase in the number of floods		A1 ft	Conclusion, mentions "floods", "evidence"	like comparison, but 0.01 needn't be
						<i>Not</i> "evidence of no increase"	explicit
						$P(R \le 6) = 0.9554; P(R > 6) = 0.0446; P(R = 6)$	$ = 0.0608: \max B2 M1 $
					_	P(R < 6) = 0.8946 and compare 0.99 etc: can g	et full marks. Else A0A0M0A0
-				1	7		
5	(1)		llŤ		MI	Upwards parabola, not below x-axis	[scales/annotations not needed]
					AI	ignore pointed at <i>a</i>	Touching axes (not asymptotic)
					B1	Horizontal straight line, not beyond limits,	Don't need vertical lines
						y-intercept below curve (unless curve makes	
						this meaningless)	i.e., 3/3 only if wholly right
	(11)				3		
	(ii)		$\int_{0}^{a} \frac{3}{a^{3}} x(x-a)^{2} dx$		MI	Attempt this integral, correct limits seen	
			$\int_{a}^{a} \frac{3}{2} \left(\frac{3}{2} - \frac{2}{2} \right) dx$		M1	Method for $\int xf(x)$, e.g. multiply out or parts.	Multiplication: needs 3 terms
			$=\int_{0}^{1}\frac{1}{a^{3}}(x^{3}-2ax^{2}+a^{2}x)dx$			independent of first M1	I
					A1	Correct form for integration, e.g. multiplied	E g $\frac{3}{x}r(x-a)^3 - \left[\frac{3}{x}(x-a)^3\right] dr$
						out correctly, or correct first stage of parts	a^{3} a^{3} 3 a^{3} 3 a^{3} 3
			$= \left[\frac{3}{a^{3}} \left(\frac{x^{4}}{4} - \frac{2ax^{3}}{3} + \frac{a^{2}x^{2}}{2}\right)\right]_{0}^{a}$		B1	Correct indefinite integral	E.g. $\frac{3}{a^3} x \frac{(x-a)^3}{3} - \frac{3}{a^3} \frac{(x-a)^4}{12}$
			$=\frac{a}{4}$		A1 5	$\frac{a}{4}$ or exact equivalent (e.g. 0.25 <i>a</i>) only	Limits not seen anywhere: can get M0M1A0B1A0

Q	Question		Answer	Marks	s Guidance		
5	(iii)		S is concentrated more towards 0	M1	Reason that shows understanding of PDF	<i>Not</i> , e.g., " <i>T</i> is constant"	
			Therefore T has bigger variance	A1	Correct conclusion		
				2			
6			$H_0: \mu = 38.4$ [Allow E(X) both times]	B2	Both correct: B2. One error e.g. no or	But \overline{x} , x, t etc B0.	
			$H_1: \mu \neq 38.4$		different symbols, one-tail etc, B1	E.g. H_0 : $\mu_0 = 38.4$, H_1 : $\mu_1 \neq 38.4$: B1	
			$\hat{\mu} = \bar{x} = 36.68$	B1	36.68 seen anywhere	$H_0: \mu = 36.68, H_1: \mu \neq 36.68: B0B0B1$	
						See below and exemplars	
			$\hat{\sigma}^2 = \frac{50}{49} \left(\frac{70027.37}{50} - 36.68^2 \right) = 56.25$	M1	Use biased variance formula [55.125]	Single formula: M2 or M0. If M0, a	
				M1	Multiply by 50/49	divisor of 49 seen anywhere gets M1	
				A1	56.25	Allow rounded if clearly correct	
			$\alpha: \qquad z = \frac{36.68 - 38.4}{2} = -1.62$	M1	Standardise using $\sqrt{50}$ or 50	If 50 missing, no more marks	
			$\sqrt{56.25}/50$	A1	<i>z</i> , a.r.t. -1.62 or $p = 0.0525$	<i>p</i> in range [0.052, 0.053]	
			> - 2.576 [or 0.0525 > .005]	A1ft	Compare $-z$ with -2.576 or $+z$ with 2.576	Ft on z. Or p explicitly with 0.005	
			β CV is 28.4 2.570 $56.25 = 35.6677$	M1	CV 38.4 – $z\sigma/\sqrt{50}$, ignore 38.4 + anything	36.68 + <i>z</i> σ/√50: M1A0A0, M0A0	
			$p = 2.576 \sqrt{\frac{50}{50}} = 55.0077$	A1	A.r.t 35.7		
			36.68 > 35.6677	A1ft	CV ft and correct comparison	Ft on wrong z or on $$ only	
			Do not reject H_0 .	M1	Correct first conclusion, needs correct	Like-with-like, needs μ and \overline{x} right	
					method & comparison if seen	way round, needs 50	
			Insufficient evidence of a change in crop	A1ft	Contextualised, "evidence" somewhere	Ft on wrong TS and/or CV	
			yield		<i>Not</i> "evidence of no change"		
				Biased v	rariance [55.125; -1.638 or 0.0508] can get B2B	1 M1M0A0 M1A0A1M1A1 (max 8)	
				σ^2 used	[-1.529 or 0.0632, or -0.12162 or 0.4144]: B2B	1 M1M1A1 M1A0A1M1A1 (max 10)	
				No √50	[-0.2293 or 0.4092]: B2B	1 M1M1A1M0 (max 6)	
				H_0/H_1 in	terms of 36.68: can get last 4 marks only if (36.	68 – 38.4) seen, and not (38.4 – 36.68)	
				11			

(Question	Answer	Marks	Guidance	
7		$H_0: p = 0.35$	B2	One error (e.g. μ , no symbol, 2-tailed) B1,	H ₀ : $\mu = 42$, H ₁ : $\mu > 42$: B1 only
		$H_1: p > 0.35$		but \overline{x} , t etc: B0. Allow π	
		B(120, 0.35)	M1	B(120, 0.35) stated or implied	
		\approx N(42, 27.3)	M1	N(<i>np</i> , <i>npq</i>), their attempt at 120×0.35	$120 \times 0.35 \times 0.65$ <i>Not</i> N(<i>np</i> , <i>nq</i>).
		α : $z = \frac{49.5 - 42}{2}$	A1ft	Standardise, with their np and \sqrt{npq} , right cc	√50 or √120: M1M1A0A0A1M0A0
		$\sim \sqrt{27.3}$		Allow both 49.5 and 50.5 and both in CR	
		= 1.435	A1	z in range [1.43, 1.44] before rounding	Or <i>p</i> in range [0.075, 0.0764]
		> 1.282 [or 0.0757 < 0.1]	A1ft	Comparison with 1.282, ft on z/p or $\sqrt{120}$	Or <i>p</i> explicit comparison with 0.1
		β: $CV = 42.5 + 1.282 \times \sqrt{27.3}$ [= 49.198]	A1ft	CV 42.5 + $z \times \sqrt{27.3}$, ignore LH, ft on np , npq	No cc: 48.618, can get A0A1A0
		z = 1.282 and compare 50	A1	z = 1.282 used in RH CV and compare 50	
		$CR \ge 50 \text{ or} \ge 49.2$	A1ft	CV correct ft on z, but don't worry about \geq	Must round up. 49 from 49.2: A1A1A0
		Reject H ₀ .	M1	Consistent first conclusion, needs correct	Can give M1A1 even if comparison
				method and comparison	not explicit. Allow from exact binomial
		Significant evidence that proportion who	A1ft	Contextualised, needs "who know	Ft on TS & CV
		know regulations has increased		regulations" or "pupils", and "evidence"	Or exact equivalent somewhere
		np > 5 [= 42] from normal attempted	M1	From $p = 0.35$ or 5/12, don't need 42	or n large or p close to 0.5 asserted
		nq = 78 > 5 and no others apart from <i>n</i> large	A1	Need 78, or 70 from 5/12, not npq	and the other qualitative reason
					asserted
		SC: If B0, B(120, 5/12):		Wrong or no cc [1.627, 0.0519 or 1.5311, 0.06	29]: loses (α) first two A1A1 only
		N(50, 29.17) M1M1		Exact B(120, 0.35): $P(\ge 50) = 0.076824$, CR \ge	50. B2M1, M0A0A0A0, M1A1M0A0
		np > 5, nq = 70 > 5: M1A1 Max 4		NB: If S3 difference of proport	ions test used, consult PE
		SC: P(≥ 42): B2 M1M1A0A0A1M0A0			
_			11		
8	(i)	B(14, 0.25): Critical region ≥ 7	M1	Use B(14, 0.25) and find r for an upper tail	e.g. CV 5 or 6 or 7, or .1117, .0383,
			A 1	All marks need upper tail	.0103, 0.0003, 0.9017, .9097
			AI	$CR \ge 7$ or $AR \le 6$ stated or clearly implied	Not just $CV = I''$
		B(14, 0.4): $P(\le 6)$	MI	Find P(in AR when $p = 0.4$) [indept of M1]	Not $P(\geq r)$, e.g. final answer 0.3075
		= 0.6925	Al	Answer 0.692 or 0.693 or a.r.t. 0.6925 or	NB: expect CV 8 or 9 and answer
			4	[0.0924 only, not 1sw [0.092452]	0.9825 or 0.9417: MUMU

(Juestic	n	Answer M		Guidance		
	(ii)	(a) De	creases	B1	One correct answer & one correct reason <i>or</i> two correct answers	Allow from numerical calculation	
		(b) De	creases; increased prob (Type I) \Leftrightarrow	B1	Two correct answers and one correct reason,	Allow equivalent or similar reason	
			decreased prob (Type II)		e.g. "CR becomes larger", etc	Allow from numerical calculation	
				2			
9	(i)	Constant <i>plus</i> "brea	<i>average</i> rate; <i>or</i> [*] same statement akdowns independent"	B1	State "average" or equiv, "random" or "uniform".	No extras apart from independence (ignore "singly")	
		Otherwise regular in	e it means that they occur at exactly atervals	B1	Correct explanation	Can't get from [*]	
				2			
	(ii)	No becau hours, etc	se breakdowns more likely in rush	B1	Any plausible reason for either "yes" or "no" that shows understanding of what the <i>statistical</i> concept means	Not "equally likely". <i>Not</i> reason for (in)dependence, unless [*], which needs <i>both</i> conditions if affirmed	
				1			
	(iii)	13		B1			
		0.0739		B1	0.074 or a.r.t. 0.0739. Marks independent		
				2			
	(iv)	$e^{-\lambda} \frac{\lambda^2}{2!} =$	0.0072	M1*	Correct formula = their 0.0072 seen		
		$\lambda = \sqrt{(0.0)}$	$144e^{\lambda}$)	M1dep	Rearrange $e^{-\lambda}$ and square root, to get $\lambda = f(\lambda)$	Allow even if left with e^{λ} or $e^{-\lambda}$ or exact equivalent	
			$= 0.12e^{\lambda/2}$	A1	Correctly obtain AG, with $k = 0.5$	_	
		$8.5 \rightarrow 8.4$	$4126; \qquad 8.6 \rightarrow 8.8440$	A1	Two correct evaluations to 4 dp at least	4 dp explicitly required	
		Therefore	e solution between 8.5 and 8.6	A1 5	All completely correct and deduction stated	CWO, except allow if only 3 SF	

Q	uestion	Answer/Indicative content	Marks	Guidance
1		N(35, 10.5)	M1	Normal, mean 35
			A1	Both parameters correct, allow $\sqrt{10.5}$ or 10.5^2
		(40.5-35) = 1 (1.607)	M1	Standardise, their <i>np</i> , <i>npq</i> , allow no $\sqrt{10.5^2}$, allow wrong or no cc
		$1 - \Phi\left(\frac{1}{\sqrt{10.5}}\right) = 1 - \Phi(1.697)$	A1	Both 40.5 and \sqrt{npq} [Ans 0.0448 or 0.9552 can imply first 4 marks]
		= 1 - 0.9552 = 0.0448	A1	Answer, a.r.t. 0.045. [Exact binomial (0.040232): 0/5]
			[5]	
2	(i)		M1	Consider any two conditions, out of <i>np</i> , <i>nq</i> (allow <i>npq</i>), size of <i>n</i> , size of <i>p</i>
		np = 147 > 5 so not Poisson	A1	147 stated, or "p not small", no wrong conditions for Poisson seen
		nq = 3 < 5 so not normal	A1	3 [not just 2.94] stated, or "p not close to $\frac{1}{2}$ ", no wrong conditions for normal seen
				(apart from <i>npq</i>)
				If spurious extra reasons seen ("not independent" etc), max 2/3
			[3]	
2	(ii)	<i>A</i> ~ B(150, 0.98) so 150 – <i>A</i> ~ B(150, 0.02)	M1	Clearly consider complement, with $p = 0.02$
		$\approx Po(3)$	A1	Po(3) stated or implied
		P(A < 146) = P(150 - A > 4) = 1 - 0.8153	M1	1 – Po(3) probability, e.g. 0.3528 or 0.0839
		= 0.1847	A1	0.185 or better [Exact binomial (0.1830): 0/4. N(3, 2.94): M1A0M0A0]
			[4]	
3	(i)	$\mu - 40 - 0.9544$	M1	Standardise with μ and σ and equate to Φ^{-1} , allow σ^2 but not \sqrt{n} , allow 1–, cc, wrong
		$\sigma = 0.0544$		signs. P(): M0 here. But can recover both marks from part (ii).
			B1	[0.954, 0.955] seen
			[2]	
3	(ii)	$60 - \mu = 0.674(5)$	M1	Standardise as in (i) but do not give if "1 –" or wrong signs in <i>either</i> equation
		$\frac{\sigma}{\sigma}$	B1	[0.674, 0.675] seen. (Other errors lead to loss of A marks.)
		Solve to get $\sigma = 12.3$ [12.278]	A1	<i>σ</i> , a.r.t. 12.3, cwo
		$\mu = 51.7(18)$	A1	μ , a.r.t. 51.7, cwo [NB: <i>CARE</i> ! either or both can be obtained from wrong equns.]
			[4]	{note for scoris zoning – (i) to be visible in marking (ii)}
3	(iii)	Based on a sample/small sample, etc	B1	Any similar comment, e.g. "frequencies not probabilities" (but not <i>just</i> " <i>n</i> is small")
				and no wrong comments. Not "because data is grouped". No scattergun.
			[1]	

4	(i)	Snakes must occur independently of one another	B1	Contextualised ("snakes" must be mentioned); not <i>just</i> "singly" but allow both
				independent and singly. Allow explanation, e.g. "Occurrence of one snake doesn't
				affect occurrences of others". Allow "snakes must occur randomly". Otherwise, more
				than one condition, "e.g. "randomly, independently, singly and at constant rate": 0.
			[1]	
4	(ii)	$1 - P(\leq 5)$	M1	Give M1 for 0.3712, 0.1107 or 0.2307. Answer 0.7851 is M0.
		= 1 - 0.7851 = 0.2149	A1 [2]	Answer, a.r.t. 0.215
4	(iii)	Po(3.08)	M1	Po(3.08) stated or implied. [Just $\lambda = 3.08$ is M0 unless Poisson later.]
		$200(3.08^2 - 3.08^3)$	M1	Correct formula for Po $(r > 0)$ used at least once, can be implied
		$e^{-3.08}\left(\frac{0.02}{2!} + \frac{0.02}{3!}\right) = [= 0.2180 + 0.2238]$	A1ft	Completely correct formula for their λ (not 4), can be implied
		= 0.4418	A1	Final answer, a.r.t. 0.442
			[4]	No working: last 3 marks either 0 or 3, no "nearly right".
5	(i)	$\int \mathbf{r}^{1} \pi$ $\begin{bmatrix} 1 \end{bmatrix}^{1} 1 \begin{pmatrix} 1 \end{bmatrix}$	M1	Attempt to integrate $f(x)$, limits (0, 1) somewhere, evidence e.g. "from calculator"
		$\left \int_{0}^{\frac{1}{2}} \sin(\pi x) dx = \left -\frac{1}{2} \cos(\pi x) \right = \frac{1}{2} - \left -\frac{1}{2} \right = 1$	B1	Correctly integrate $\sin(\pi x)$ to $-\frac{1}{2}\cos(\pi x)$
			A1	Fully correct, need to see $-\frac{1}{2}\cos(\pi x)$ and final 1, no wrong working seen
		and function non-negative for all x in range	B1	Non-negative asserted explicitly, allow positive or equivalent. Not just graph drawn.
			[4]	(Most will not get this mark!)
5	(ii)		M1	Correct shape, through 0, allow below axis outside range. Allow partial curve if clearly
				part of sine curve.
			A1	Fully correct including no extension beyond [0, 1]. Don't worry about grads at ends.
				Ignore labelling of axes
		$\mathrm{E}(X) = \frac{1}{2}$	B1	$\frac{1}{2}$ or 0.5, needs to be simplified, no working needed, <i>no</i> ft
			[3]	
5	(iii)	$\int_{-1}^{1} -\sin(\pi t) dt = 0.75 \cdot \left[\int_{-1}^{1} \cos(\pi t) dt = 0.75 \right]$	M1	Equate integral to correct probability, correct limits somewhere
		$\int_{q} \frac{1}{2} \pi \sin(\pi x) dx = 0.75, \left\{ \left[-\frac{1}{2} \cos(\pi x) \right]_{q} = 0.75 \right\}$		allow complementary probability (= 0.25) only if limits $(0, q)$
		$\cos(\pi q) = 0.5$	A1	$\cos(\pi q) = 0.5$ or exact equivalent
		Solve to get $q = \frac{1}{3}$	A1	$q = \frac{1}{3}$ or a.r.t. 0.333.
			[3]	SR: Numerical (no working needed): 0.333 B3, 0.33 B2
5	(iv)	$\int_{-1}^{1} \pi r^{2} \sin(-r) dr (1)^{2}$	M1	Integral part correct, allow limits omitted, ignore dx
		$\int_{0}^{\infty} \frac{1}{2} x^{2} \sin(\pi x) dx - (\frac{1}{2})$	A1ft	Subtract their $[E(X)]^2$, allow μ in form of integral, correct limits needed, not just " μ^2 "
			[2]	{note for scoris zoning – (ii) needs to be visible here}
5	(v)	Values of x in range close to $E(X)$ are more	B1	Need to see "values of x" or equivalent, and probably not "occur"
		likely than those further away		Not "the probability of x is greater when x is close to $E(X)$ " etc. Not "PDF greater"
			[1]	

6	(i)	Sample is random	B1	Indicate random sample. Allow "unbiased sample" or "randomly selected" or "all
				equally likely". Allow "representative" provided it's clearly "of company" (not city)
			[1]	Not just "independent". Withhold if extra wrong bits.
6	(ii)	List population, number sequentially	B1	List can be implied; must imply employees or people. "Sequential" can be assumed.
		Select using random numbers	B1	Not "select numbers randomly", Don't need "ignore outside range" etc.
				Number randomly and select randomly, B1, but "assign random nos & arrange", B2
				SC: Put names into hat/lottery machine and take them out: <u>B2</u>
			[2]	SC: Systematic: B1 for list, can get second B1 if starting-point random
6	(iii)	$H_0: p = 0.4; H_1: p < 0.4$	B2	Both correct, B2. Allow π . One error, e.g, μ or no symbol, B1, but \overline{x} , z etc: B0.
		B(12, 0.4)	M1	B(12, 0.4) stated or implied. Can be implied by N(4.8, 2.88) but no further marks.
				0.1673, 0.0398, 0.1513, 0.0421: M1A0(A1M1A1)
	α:	$P(\le 2) = 0.0834$	A1	$P(\le 2) = 0.0834$, or $P(> 2) = 0.9166$.
		> 0.05	A1	Compare numerical $P(\le 2)$ with 0.05, or $P(>2)$ with 0.95
	β:	CR is ≤ 1	A1	CR is ≤ 1 stated.
	,	0.0196 seen and compare 2 with ≤ 1	A1	Explicitly compare 2 with CR, probability 0.0196 must be seen
		Do not reject H_0 .	M1	Correct first conclusion, needs $P(\le 2 p = 0.4)$ or fully consistent equivalent
		Insufficient evidence that proportion of	A1ft	In context (mention "employees", "city" etc), acknowledge uncertainty ("evidence")
		employees from group Z is less.		<i>Not</i> "there is evidence that the proportion of employees is 0.4"
				FT on wrong <i>p</i> -value or wrong critical value if previous mark gained
			[7]	SC: Normal: B2 M1 max
				SC: $P(=2)$ or $P(\ge 2)$ or $P(<2)$: B2 M1 max
				SC: two-tailed: can get B1B0 M1A1A0 M1A1 (don't give second A1 for 0.05)
6	(iv)	Yes as H_0 is rejected	M1	Realise this changes conclusion (FT!), or "more likely to reject H ₀ ", "larger CR"
			A1 [2]	More supportive [just "more supportive" without evidence is M0A0]
7	(i)	$\hat{\mu} = \overline{x} = 81$	B1	81 only, can be implied
		329800 012 [- 25]	M1	Correct formula for biased estimate, their "81", can be implied
		$\times \frac{50}{50};$ = 35.71	M1	Multiply by 50/49. SC: single formula: M2, or M1 if wrong but divisor 49 anywhere
		49		[can be recovered if correctly done in part (ii)]
			A1	A.r.t. $35.7 - \underline{\operatorname{can't}}$ be recovered from part (ii). Can be implied
		$1 = \Phi(90-81)$ 1 $\Phi(1.50c) = 1 = 0.0220$	M1	Standardise with their μ and σ , allow σ^2 , cc but not $\sqrt{50}$
		$1 - \Psi\left(\frac{1}{\sqrt{35.71}}\right) = 1 - \Psi(1.500) = 1 - 0.9339$		
		= 6.61% or 0.0661	A1	Answer, a.r.t. 6.6% or 0.066
			[6]	

7	(ii)	$H_0: \mu = 80$	B2	Correct, B2. One error, e.g. wrong or no symbol, >, B1, but x or \overline{x} or t etc, or 81, B0.
		$H_1: \mu \neq 80$		NB: If both hypotheses involve 81, <i>can't</i> get final M1
	α:	$z = \frac{81 - 80}{1183} = 1.183$ [or $n = 0.1183$]	M1	Standardise, with $\sqrt{50}$, allow $$, sign or cc errors, allow from biased variance
		$\frac{1}{\sqrt{35.71/50}} = 1.105 [07p = 0.1105]$	A1	<i>z</i> , a.r.t. 1.18, or <i>p</i> , a.r.t. 0.118. <u>Allow –1.18</u> .
		< 1.645	B1	Their $z < 1.645$ or $p > 0.05$, not if one-tail. <u>Allow $-1.18 > -1.645$. Not just 1.645 seen</u> .
	β:	CV $80 + 1.645\sqrt{\frac{35.71}{50}} = 81.39$	M1	$80 + zs/\sqrt{50}$, allow $\sqrt{0}$ or cc errors, ignore – (no marks for – alone);
			B1	z = 1.645 used in this expression (not just seen), <i>not</i> from one-tail
		81 < 81.39	A1	Compare CV with 81, allow 81.08 from one-tailed ($z = 1.282$) (but not on their σ)
				SC: $81 - 1.645\sqrt{\frac{35.71}{50}}$: If H ₀ : $\mu = 80$: (B2) M1B1A0M0A0.
				If H_0 : $\mu = 81$: (B0) M1B1A1 (79.61) M0A0
		Do not reject H_0 .	M1	Correct first conclusion, needs $\sqrt{50}$, correct comparison type, μ and \overline{x} not consistently
				wrong way round (thus H ₀ : $\mu = 81$ can get B0 M1A1A1 M0A0, max 3/7)
				In method β , it needs to be clear that comparison involves \overline{x} .
		Insufficient evidence that the mean time is not	A1ft	Contextualised (mention "time"), acknowledge uncertainty ("evidence that")
		80 minutes.		<i>Not</i> "significant evidence that mean time is 80"
				FT on wrong z-value or wrong critical value if previous mark gained
			[7]	SC: One-tailed: can get B1B0 M1A1B0 M1A1, max 5/7
				No $\sqrt{50}$: can get B2 M0 B1 M0, max $3/7$
7	(iii)	(a) Yes (single observation only)	B1	No reason needed, but withhold if wrong reason seen. Allow "yes, no dist" given"
		(b) No, CLT applies to large sample	B1	"No" and refer to central limit theorem or "large sample"
	(1)		[2]	{note for scoris $zoning - (a)$ and (b) to be in single $zone$ }
8	(1)	$P(W=0 \mid \lambda = 3.6)$	MI	Use this conditional probability. Not 0.9727, not just 2.5% etc
		= 0.0273 or 2.73%	Al	Answer a.r.t. 0.0273 or 2.73%. ISW if appropriate (e.g. "0.0273, .: 2.5%")
			[2]	
8	(11)	$1 - e^{-\lambda_0} = 0.8$	MI	Use $P(W > 0 \lambda = \lambda_0)$, formula needed but allow if wrong
		$e^{-\lambda_0} = 0.2$	A1	This exact equation, or $e^{\lambda_0} = 5$, or exact equivalent RHS
		$\lambda_0 = -\ln(0.2)$	M1	Solve using ln or otherwise [independent of first M1, e.g. $-\ln(0.8) = 0.223$ is M1 here]
		= 1.609	A1	Final answer, exact or a.r.t. 1.61, cwo
				SC: No working: 1.60 (tables etc): B0. 1.61 (T&I): SC B4.
			[4]	