

Mark Scheme 4734
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STATISTICS 3

1	(i)	$p_s \pm z\sigma_{est}$ 400. $p_s=186/400(0.465)$ $\sigma_{est}=\sqrt{\frac{0.465 \times 0.535}{400}}$ $z=1.96$ (0.416,0.514)	M1 A1 B1 A1 A1	5	Use formula, σ involving p_s and
	(ii)	Councillor statement implies $p=0.5$. CI does contain 0.5 but only just so councillor probably correct. assertive	B1	1	Any justifiable comment Not too
2	(i)	σ^2 unknown	B1	1	
	(ii)	$H_0: \mu=2000$ (or $\geq$), $H_1: \mu < 2000$ $\bar{x}=1958.2$, $s=115.57$ EITHER: Test statistic = $\frac{1958.2 - 2000}{115.57/2}$ = -0.7234 Critical value -1.638 Test statistic not in CR, accept H_0 Accept that specification is being met OR: Critical region: $\frac{\bar{x} - 2000}{115.57/2} < t$ $t=-1.638$ $\bar{x} < 1905.2$ As above	B1 B1B1 M1 A1 B1 A1 M1 M1 A1 M1A1	8	or 1958,115.6 art -0.723 Or equivalent Conclusion in context art 1900 or 1910 Conclusion in context
3	(i)	Use of $\int_{20}^a f(t)dt$ $\left[-\frac{2}{3} \cos \frac{\pi t}{60} \right]_{20}^a$ AG	M1 A1 A1	3	With limits and $f(t)$ substituted Properly obtained
	(ii)	$3 \times (i) + 2 \times (1-(i))$ Equate to 2.80 and attempt to solve $a=44.8$	M1 A1 M1 A1	4	Idea of expectation All correct From equation in a, 2 or 3 Accept 45 SR: $\frac{1}{3}(1-2\cos..)=0.8$ give max 3/4

4	(i)	Use Poisson distribution With $\mu=55$ $\sigma^2=55$ $(39.5-55)/\sqrt{55}$ -2.09 art 0.982	M1 B1 A1 A1 A1	Po(5.5) or Po(55) seen Standardising, with ,without or wrong cc	A1 6
	(ii)	$E(X-Y)=37$ $\text{Var}(X-Y)=55+18$ $=73$	B1✓ M1 A1✓	ft μ above 3 ft μ above	
	(iii)	EITHER: Expectation not equal to variance OR: $X-Y$ could be negative OR: Difference of two Poisson variables could have a negative expectation So $X-Y$ does not have a Poisson distn	A1 M1 2	Any one	
5	(i)	EITHER: Use $\frac{1}{8}(3-1)^2=a(3-2)$ OR: $a(4-2)=1$ $a=\frac{1}{2}$	A1 M1 2	Continuity of F	
	(ii)	$F(1.8)=\frac{1}{8}(0.8)^2$ $=0.08$ $C_X(8)=1.8$	M1 A1 2	Appropriate use of F	
	(iii)	$G(y)=P(Y \leq y)=P((X-1)^{1/2} \leq y)$ $=P(X \leq y^2+1)$ $=F(y^2+1)$ $G(y) = \begin{cases} \frac{1}{8}y^4 & (0 \leq y \leq \sqrt{2}), \\ \frac{1}{2}(y^2-1) & (\sqrt{2} < y \leq \sqrt{3}). \end{cases}$	M1 A1 A1 5		
		Ignore others, A1 for both ranges of y	B1 5		
	(iv)	Use $G(y)$ to find $C_Y(8)$ Obtain $\sqrt{0.8}$ Correct verification	M1 A1 B1 3		

6	(i)	$s^2 = (8 \times 0.7400 + 9 \times 0.8160) / 17$ $= 0.7802$ 0.780 AG	M1 A1	Formula for pooled estimate At least 4DP shown	2
	(ii)	Assumes braking distances have normal distributions Use $\bar{x}_A - \bar{y}_B \pm t\sigma$ $t = 2.567$ $\sigma = \sqrt{[0.7802(1/10 + 1/9)]}$ (0.40584) (1.518, 3.602)	B1 M1 A1 B1 A1	Must be t value Allow 0.780 art (1.52, 3.60)	5
	(iii)	$H_0: \mu_A - \mu_B = 2$, $H_1: \mu_A - \mu_B > 2$ Use of CV, 1.740 EITHER: Test statistic $= (2.56 - 2) / \sigma$ $= 1.38$ OR: Critical region $\bar{x}_A - \bar{x}_B > 2 + 1.74 \times 0.4054$ $= 2.7054$ Indication that test statistic is not in critical region and Insufficient evidence to accept claim and H_1	B1 B1 M1 A1 M1 A1 M1 A1	For both hypotheses Standardising, σ as above Rounding to 1.38 2.70 or 2.71 Not from different signs test statistic critical value. A1 dep on correct H_0	6
7	(i)	Use $\int_1^\infty x^\alpha x^{-\alpha-1} dx = \left(\int_1^\infty x^\alpha x^{-\alpha} dx \right)$ $\left[\frac{-x^{\alpha+1}}{\alpha+1} \right]_1^\infty$ $= \alpha / (1-\alpha)$ AG	M1 B1 A1	Correct limits not required Properly obtained	3
	(ii)	$\alpha / (1-\alpha) = 1.92$ giving 2.087 AG	B1		1
	(iii)	Integral of $2.087x^{-3.087}$ from 2 to 3 $[-x^{-2.087}]_2^3$ $\times 200$ Obtain AG	M1 A1 A1 A1	Evidence required	4
	(iv)	Combine last 3 cells $X^2 = 6.9^2/152.9 + 6.1^2/26.9$ $+ 4.9^2/9.1 + 4.1^2/11.18$ $= 5.847...$ Use CV 5.991 Accept that data supports Zipf's law SR: From 6 cells: B0M1A1 (for 9.34) then B1 for 9.488, B1	B1 M1 A1 A1 B1 B1	Accept one error All correct art 5.8 ft number of sells used.	6 Max 4/6