Mark Scheme 4733 January 2007

For over-specified answers (>6SF where inappropriate) deduct 1 mark, no more than once in paper.

| $\begin{gathered} \mathbf{1} \quad \frac{22-\mu}{5}=-\Phi^{-1}(0.242) \\ =-0.7 \\ \mu=\mathbf{2 5 . 5} \end{gathered}$ | M1  <br> A1  <br> B1  <br> A1 4 | Standardise with $\Phi^{-1}$, allow +, " 1 -" errors, cc, $\sqrt{5}$ or $5^{2}$ Correct equation including signs, no cc, can be wrong $\Phi^{-1}$ 0.7 correct to 3 SF , can be + Answer 25.5 correct to 3 SF |
| :---: | :---: | :---: |
| 2 (i) $900 \div 12=75$ | B1 1 | 75 only |
| (ii) (a) True, first choice is random <br> (b) False, chosen by pattern |   <br> B1 1 <br> B1 $\mathbf{1}$ | True stated with reason based on first choice False stated, with any non-invalidating reason |
| (iii) Not equally likely e.g. $P(1)=0$, or triangular | $\begin{array}{ll} \text { M1 } & \\ \text { A1 } & 2 \\ \hline \end{array}$ | "Not equally likely", or "Biased" stated Non-invalidating reason |
| 3 Let $R$ be the number of 1 s $\begin{aligned} & R \sim \mathrm{~B}(90,1 / 6) \\ & \approx \mathrm{N}(15,12.5) \\ & \frac{13.5-15}{\sqrt{12.5}} \\ & \mathbf{0 . 6 6 4 3} \end{aligned}$ | B1 <br> B1 <br> B1 <br> M1 <br> A1 <br> A1 <br> 6 | $B(90,1 / 6)$ stated or implied, e.g. $\operatorname{Po}(15)$ <br> Normal, $\mu=15$ stated or implied <br> 12.5 or $\sqrt{12.5}$ or $12.5^{2}$ seen <br> Standardise, $n p$ and $n p q$, allow errors in $\sqrt{ }$ or cc or both $\sqrt{ }$ and cc both right <br> Final answer, a.r.t. 0.664. [Po(15): 1/6] |
| $\begin{array}{\|lll} \hline 4 & \text { (i) } & \bar{w}=100.8 \div 14=7.2 \\ & & \frac{938.70}{14}-\bar{w}^{2}[=15.21] \\ & & \times 14 / 13 \\ & =\mathbf{1 6 . 3 8} \end{array}$ | B1  <br> M1  <br> M1  <br> A1 4 | 7.2 seen or implied Use $\Sigma w^{2}-$ their $\bar{w}^{2}$ <br> Multiply by $n /(n-1)$ <br> Answer, a.r.t. 16.4 |
| (ii) $\quad \begin{aligned} & \mathrm{N}(7.2,16.38 \div 70) \\ & \\ & {[=\mathrm{N}(7.2,0.234)]}\end{aligned}$ | $\begin{array}{ll} \text { B1 } \\ \text { B1 } \sqrt{ } \\ \text { B1 } \sqrt{ } & 3 \\ \hline \end{array}$ | Normal stated <br> Mean their $\bar{w} V$ <br> Variance [their (i) $\sqrt{ } \div 70$ ], allow arithmetic slip |
| 5 (i) $\lambda=1.2$ <br>   Tables or formula used <br>   $\mathbf{0 . 6 6 2 6}$ | B1  <br> M1  <br> A1 3 | Mean 1.2 stated or implied <br> Tables or formula [allow $\pm 1$ term, or " 1 -"] correctly used Answer in range [0.662, 0.663] $\text { [.3012, } 6990,6268 \text { or } 8795: \text { B1M1A0] }$ |
| (ii) $\quad \begin{aligned} & \mathrm{B}(20,0.6626 \sqrt{13} \\ & \\ & \\ & { }^{20} \mathrm{C}_{13} 0.66266^{13} \times 0.3374^{7} \\ & \mathbf{0 . 1 8 3}\end{aligned}$ | M1 <br> M1 <br> A1 3 | $\mathrm{B}(20, p), p$ from (i), stated or implied Correct formula for their $p$ <br> Answer, a.r.t. 0.183 |
| (iii) Let $S$ be the number of stars $\begin{aligned} & S \sim \operatorname{Po}(24) \\ & \approx \mathrm{N}(24,24) \\ & \frac{29.5-24}{\sqrt{24}}[=1.1227] \\ & \mathbf{0 . 8 6 9 2} \end{aligned}$ | B1 <br> B1 <br> B1 $\sqrt{ }$ <br> M1 <br> A1 <br> A1 <br> 6 | Po(24) stated or implied <br> Normal, mean 24 <br> Variance 24 or $24^{2}$ or $\sqrt{ } 24$, $\sqrt{ }$ if 24 wrong <br> Standardise with $\lambda, \lambda$, allow errors in cc or $\sqrt{ }$ or both $\sqrt{ } \lambda$ and cc both correct <br> Answer, in range [0.868, 0.8694] |


| $6$ | $\begin{align*} & {\left[a x+\frac{b x^{2}}{2}\right]_{0}^{2}=1}  \tag{i}\\ & 2 a+2 b=1 \end{align*}$ | M1 <br> B1 <br> A1 3 | Use total area $=1$ Correct indefinite integral, or convincing area method Given answer correctly obtained, " 1 " appearing before last line [if $+c$, must see it eliminated] |
| :---: | :---: | :---: | :---: |
| (ii) | $\begin{aligned} & {\left[\frac{a x^{2}}{2}+\frac{b x^{3}}{3}\right]_{0}^{2}=\frac{11}{9}} \\ & 2 a+\frac{8 b}{3}=\frac{11}{9} \end{aligned}$ <br> Solve simultaneously $a=\frac{1}{6}, \quad b=\frac{1}{3}$ | M1 <br> B1 <br> A1 <br> M1 <br> A1 <br> A1 6 | Use $\int_{x f}(x) \mathrm{d} x=11 / 9$, limits 0,2 <br> Correct indefinite integral <br> Correct equation obtained, a.e.f. <br> Obtain one unknown by correct simultaneous method $a$ correct, $1 / 6$ or a.r.t 0.167 <br> $b$ correct, $1 / 3$ or a.r.t. 0.333 |
|  | $\begin{aligned} & \text { e.g. } \mathrm{P}(<11 / 9)=0.453 \text {, or } \\ & {\left[a x+\frac{b x^{2}}{2}\right]_{0}^{m}=0.5, m=1.303 \text { or } \frac{\sqrt{13}-1}{2}} \end{aligned}$ <br> Hence median > mean | M1 <br> M1 <br> A1 <br> A1 $\sqrt{ } 4$ | Use $\mathrm{P}(x<11 / 9)$, or integrate to find median $m$ Substitute into $\int \mathrm{f}(x) \mathrm{d} x, \sqrt{ }$ on $a, b$, limits 0 and $11 / 9$ or $m$ <br> [if finding $m$, need to solve 3 -term quadratic] <br> Correct numerical answer for probability or $m$ <br> Correct conclusion, cwo <br> ["Negative skew", M2; median > mean, A2] |
| $7 \quad$ (i) <br> $\alpha$ : <br> $\beta$ : | $\begin{aligned} & \left.\hline \mathrm{H}_{0}: p=0.35 \quad \text { or } p \geq 0.35\right] \\ & \mathrm{H}_{1}: p<0.35 \\ & \mathrm{~B}(14,0.35) \\ & \mathrm{P}(\leq 2) \quad=0.0839>0.025 \\ & \mathrm{CR} \leq 1 \text {, probability } 0.0205 \\ & \text { Do not reject } \mathrm{H}_{0} \text {. Insufficient } \\ & \text { evidence that proportion that can } \\ & \text { receive Channel } \mathrm{C} \text { is less than } 35 \% \end{aligned}$ | B1 <br> B1 <br> M1 <br> A1 <br> B1 <br> M1 <br> A1 $\sqrt{ } 7$ | Each hypothesis correct, B1+B1, allow $p \geq .35$ if .35 used [Wrong or no symbol, B1, but $r$ or $x$ or $\bar{x}$ : B0] Correct distribution stated or implied, can be implied by $\mathrm{N}(4.9, \ldots)$, but not $\mathrm{Po}(4.9)$ <br> 0.0839 seen, or $\mathrm{P}(\leq 1)=0.0205$ if clearly using CR Compare binomial tail with 0.025 , or $R=2$ binomial CR Do not reject $\mathrm{H}_{0}, \sqrt{ }$ on their probability, not from N or Po or $\mathrm{P}(<2)$; Contextualised conclusion $\sqrt{ }$ |
| (ii) | $\begin{aligned} & \mathrm{B}(8,0.35): \mathrm{P}(0)=0.0319 \\ & \mathrm{~B}(9,0.35): \mathrm{P}(0)=0.0207 \end{aligned}$ <br> Hence largest value of $n$ is 8 | M1  <br> A1  <br> A1  <br> A1 4 | Attempt to find $\mathrm{P}(0)$ from $\mathrm{B}(n, 0.35)$ <br> One correct probability $\quad[\mathrm{P}(\leq 2)=.0236, n=18$ : M1A1] <br> Both probabilities correct <br> Answer 8 or $\leq 8$ only, needs minimum M1A1 |
| or | $\begin{aligned} & 0.65^{n}>0.025 ; n \ln 0.65>\ln 0.025 \\ & 8.56 ; \quad \text { largest value of } n=8 \end{aligned}$ | $\begin{aligned} & \text { M1M1 } \\ & \text { A1A1 } \end{aligned}$ | $p^{n}>0.025$, any relevant $p$; take $\ln$, or T\&I to get 1 SF In range [8.5, 8.6]; answer 8 or $\leq 8$ only |
| 8 (i) $\alpha$ : | $\frac{100.7-102}{5.6 / \sqrt{80}}=-2.076$ <br> Compare with -2.576 | M1 A1 <br> B1 3 | Standardise 100.7 with $\sqrt{ } 80$ or 80 a.r.t. -2.08 obtained, must be - , not from $\mu=100.7$ <br> -2.576 or -2.58 seen and compare $z$, allow both + |
| $\text { or } \beta \text { : }$ | $\begin{gathered} \Phi(-2.076)=0.0189 \\ \text { [or } \Phi(2.076)=0.981] \\ \text { and compare with } 0.005 \text { [or } 0.995 \text { ] } \end{gathered}$ | M1 <br> A1 <br> B1 (3) | Standardise 100.7 with $\sqrt{ } 80$ or 80 a.r.t. 0.019 , allow 0.981 only if compared with 0.995 Compare correct tail with 0.005 or 0.995 |
| $\text { or } \gamma \text { : }$ | $\begin{aligned} & 102-\frac{k \times 5.6}{\sqrt{80}} \\ & k=2.576, \text { compare } 100.7 \\ & 100.39 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { B1 } \\ & \text { A1 (3) } \end{aligned}$ | This formula, allow,+ 80 , wrong SD, any $k$ from $\Phi^{-1}$ <br> $k=2.576 / 2.58$, - sign, and compare 100.7 with CV CV a.r.t. 100.4 |
|  | Do not reject $\mathrm{H}_{0}$ Insufficient evidence that quantity of $\mathrm{SiO}_{2}$ is less than 102 | M1 <br> A1 2 | Reject/Do not reject, $\sqrt{ }$, needs normal, 80 or $\sqrt{80}, \Phi^{-1}$ or equivalent, correct comparison, not if clearly $\mu=100.7$ Correct contextualised conclusion |
| (ii) (a) | $\begin{align*} & \frac{c-102}{5.6 / \sqrt{n}}=-2.326 \\ & 102-c=\frac{13.0256}{\sqrt{n}} \tag{AG} \end{align*}$ | M1 <br> B1 <br> A1 3 | One equation for $c$ and $n$, equated to $\Phi^{-1}$, allow cc, wrong sign, $\sigma^{2} ; \quad 2.326$ or 2.33 <br> Correctly obtain given equation, needs in principle to have started from $c-102,-2.326$ |
| (b) | $\frac{c-100}{5.6 / \sqrt{n}}=1.645 \quad \text { or } \quad c-100=\frac{9.212}{\sqrt{n}}$ | $\begin{array}{ll} \mathrm{M} 1 & \\ \text { A1 } & 2 \end{array}$ | Second equation, as before Completely correct, aef |
| (c) | Solve simultaneous equations $\begin{aligned} & V_{n}=11.12 \\ & n_{\text {min }}=124 \\ & c=100.83 \end{aligned}$ | M1  <br> A1  <br> A1  <br> A1 4 | Correct method for simultaneous equations, find $c$ or $\sqrt{n}$ $\sqrt{n}$ correct to 3 SF $n_{\min }=124 \text { only }$ <br> Critical value correct, 100.8 or better |

