

Mechanics 3

**ADVANCED GCE** 

MATHEMATICS

4730

Candidates answer on the Answer Booklet

OCR Supplied Materials:

- 8 page Answer Booklet
- List of Formulae (MF1)

Other Materials Required: None Monday 19 January 2009 Afternoon

Duration: 1 hour 30 minutes



## INSTRUCTIONS TO CANDIDATES

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by  $g \,\mathrm{m}\,\mathrm{s}^{-2}$ . Unless otherwise instructed, when a numerical value is needed, use g = 9.8.
- You are permitted to use a graphical calculator in this paper.

## INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- This document consists of 4 pages. Any blank pages are indicated.



A particle *P* of mass 0.5 kg is moving in a straight line with speed 6.3 m s<sup>-1</sup>. An impulse of magnitude 2.6 N s applied to *P* deflects its direction of motion through an angle  $\theta$ , and reduces its speed to 2.5 m s<sup>-1</sup> (see diagram). By considering an impulse-momentum triangle, or otherwise,

(i) show that 
$$\cos \theta = 0.6$$
, [4]

(ii) find the angle that the impulse makes with the original direction of motion of *P*. [4]



Two uniform rods AB and BC, of weights 70 N and 110 N respectively, are freely jointed at B. The rods are in equilibrium in a vertical plane with A and C at the same horizontal level and AC = 2 m. The rod AB is freely jointed to a fixed point at A and the rod BC is freely jointed to a fixed point at C. The horizontal distance between B and A is 4 m and B is 4 m below AC; angle BAC is obtuse (see Fig. 1). The force exerted on the rod AB at B, by the rod BC, has horizontal and vertical components as shown in Fig. 2.

- (i) By taking moments about A for the rod AB find the value of X Y. [2]
- (ii) By taking moments about C for the rod BC show that 2X 3Y + 165 = 0. [2]
- (iii) Find the magnitude of the force acting between *AB* and *BC* at *B*. [4]

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A and B are fixed points with B at a distance of 1.8 m vertically below A. One end of a light elastic string of natural length 0.6 m and modulus of elasticity 24 N is attached to A, and one end of an identical elastic string is attached to B. A particle P of weight 12 N is attached to the other ends of the strings (see diagram).

(i) Verify that *P* is in equilibrium when it is at a distance of 1.05 m vertically below *A*. [2]

P is released from rest at the point 1.2 m vertically below A and begins to move.

- (ii) Show that, when P is x m below its equilibrium position, the tensions in PA and PB are (18 + 40x) N and (6 40x) N respectively. [2]
- (iii) Show that P moves with simple harmonic motion of period 0.777 s, correct to 3 significant figures. [3]
- (iv) Find the speed with which *P* passes through the equilibrium position. [2]





One end of a light inextensible string of length 0.5 m is attached to a fixed point *O*. A particle *P* of mass 0.2 kg is attached to the other end of the string. With the string taut and horizontal, *P* is projected with a velocity of  $3 \text{ m s}^{-1}$  vertically downward. *P* begins to move in a vertical circle with centre *O*. While the string remains taut the angular displacement of *OP* is  $\theta$  radians from its initial position, and the speed of *P* is  $v \text{ m s}^{-1}$  (see diagram).

- (i) Show that  $v^2 = 9 + 9.8 \sin \theta$ . [3]
- (ii) Find, in terms of  $\theta$ , the radial and tangential components of the acceleration of *P*. [3]
- (iii) Show that the tension in the string is  $(3.6 + 5.88 \sin \theta)$  N and hence find the value of  $\theta$  at the instant when the string becomes slack, giving your answer correct to 1 decimal place. [4]



Two smooth uniform spheres A and B, of equal radius, have masses 3 kg and 4 kg respectively. They are moving on a horizontal surface, each with speed  $5 \text{ m s}^{-1}$ , when they collide. The directions of motion of A and B make angles  $\alpha$  and  $\beta$  respectively with the line of centres of the spheres, where  $\sin \alpha = \cos \beta = 0.6$  (see diagram). The coefficient of restitution between the spheres is 0.75. Find the angle that the velocity of A makes, immediately after impact, with the line of centres of the spheres. [10]

6 A stone of mass 0.125 kg falls freely under gravity, from rest, until it has travelled a distance of 10 m. The stone then continues to fall in a medium which exerts an upward resisting force of 0.025v N, where v m s<sup>-1</sup> is the speed of the stone *t* s after the instant that it enters the resisting medium.

(i) Show by integration that 
$$v = 49 - 35e^{-0.2t}$$
. [8]

- (ii) Find how far the stone travels during the first 3 seconds in the medium. [4]
- 7 A particle of mass 0.8 kg is attached to one end of a light elastic string of natural length 2 m and modulus of elasticity 20 N. The other end of the string is attached to a fixed point O. The particle is held at rest at O and then released. When the extension of the string is x m, the particle is moving with speed v m s<sup>-1</sup>.

(i) By considering energy show that 
$$v^2 = 39.2 + 19.6x - 12.5x^2$$
. [4]

- (ii) Hence find
  - (a) the maximum extension of the string, [2]
  - (b) the maximum speed of the particle, [4]
  - (c) the maximum magnitude of the acceleration of the particle. [5]



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