

**ADVANCED GCE
MATHEMATICS**

Mechanics 3

4730

Candidates answer on the answer booklet.

OCR supplied materials:

- 8 page answer booklet
(sent with general stationery)
- List of Formulae (MF1)

Other materials required:

- Scientific or graphical calculator

**Monday 24 January 2011
Morning**

Duration: 1 hour 30 minutes



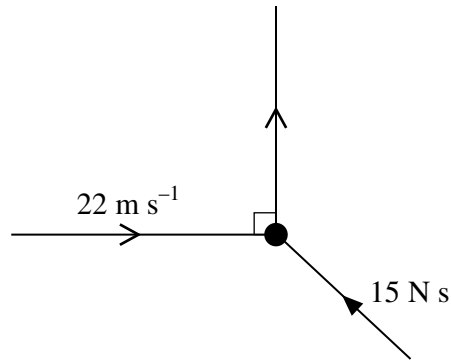
INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the spaces provided on the answer booklet. Please write clearly and in capital letters.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Answer **all** the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- The acceleration due to gravity is denoted by $g \text{ m s}^{-2}$. Unless otherwise instructed, when a numerical value is needed, use $g = 9.8$.
- You are permitted to use a scientific or graphical calculator in this paper.

INFORMATION FOR CANDIDATES

- The number of marks is given in brackets [] at the end of each question or part question.
- **You are reminded of the need for clear presentation in your answers.**
- The total number of marks for this paper is **72**.
- This document consists of **4** pages. Any blank pages are indicated.

1



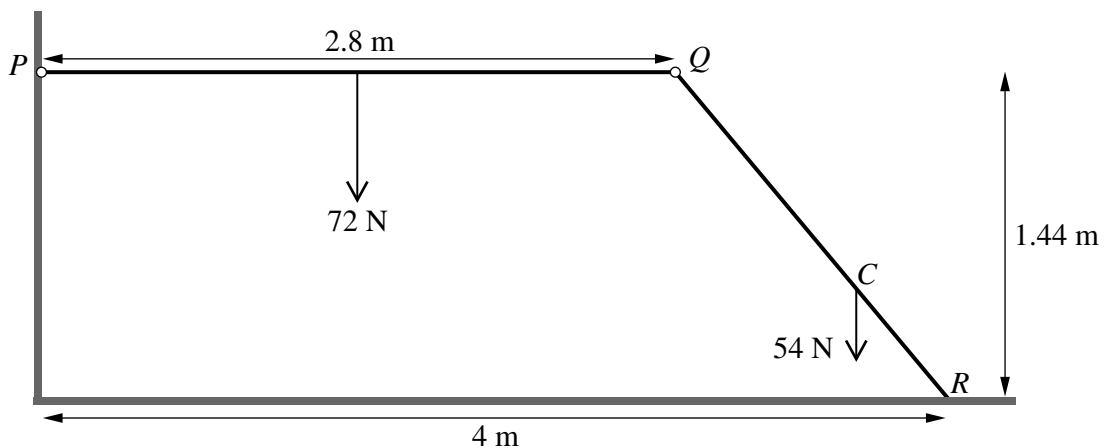
A ball of mass 0.5 kg is moving with speed 22 m s^{-1} in a straight line when it is struck by a bat. The impulse exerted by the bat has magnitude 15 N s and the ball is deflected through an angle of 90° (see diagram). Find

- (i) the direction of the impulse, [3]
- (ii) the speed of the ball immediately after it is struck. [3]

- 2 A particle of mass 0.4 kg is attached to a fixed point O by a light inextensible string of length 0.5 m . The particle is projected horizontally with speed 6 m s^{-1} from the point 0.5 m vertically below O . The particle moves in a complete circle. Find the tension in the string when

- (i) the string is horizontal,
- (ii) the particle is vertically above O . [6]

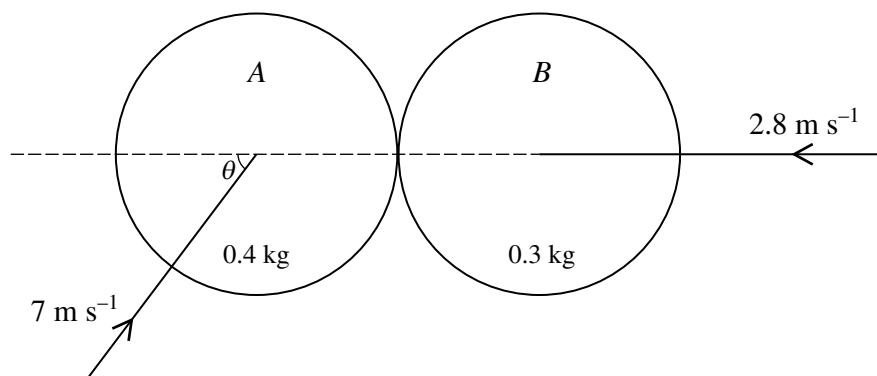
3



A uniform rod PQ has weight 72 N . A non-uniform rod QR has weight 54 N and its centre of mass is at C , where $QC = 2CR$. The rods are freely jointed to each other at Q . The rod PQ is freely jointed to a fixed point of a vertical wall at P and the rod QR rests on horizontal ground at R . The rod PQ is 2.8 m long and is horizontal. The point R is 1.44 m below the level of PQ and 4 m from the wall (see diagram).

- (i) Find the vertical component of the force exerted by the wall on PQ . [2]
- (ii) Hence show that the normal component of the force exerted by the ground on QR is 90 N . [2]
- (iii) Given that the friction at R is limiting, find the coefficient of friction between the rod QR and the ground. [5]

4



Two uniform smooth spheres A and B of equal radius are moving on a horizontal surface when they collide. A has mass 0.4 kg and B has mass 0.3 kg . Immediately before the collision A is moving with speed 7 m s^{-1} at an acute angle θ to the line of centres, where $\cos \theta = 0.6$, and B is moving with speed 2.8 m s^{-1} along the line of centres (see diagram). The coefficient of restitution between the spheres is 0.7 . Find

- (i) the speed of B immediately after the collision, [6]
- (ii) the angle turned through by the direction of motion of A as a result of the collision. [5]

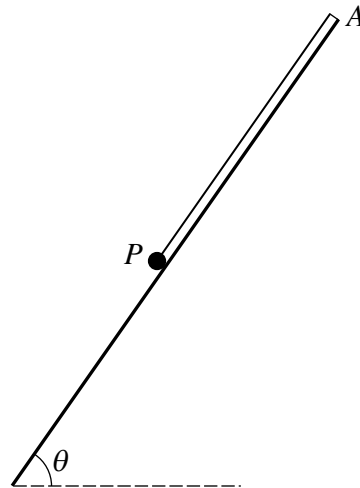
- 5 A particle P of mass 0.05 kg is suspended from a fixed point O by a light elastic string of natural length 0.5 m and modulus of elasticity 2.45 N .

- (i) Show that the equilibrium position of P is 0.6 m below O . [3]

P is held at rest at a point 0.675 m vertically below O and then released. At time $t\text{ s}$ after P is released, its downward displacement from the equilibrium position is $x\text{ m}$.

- (ii) Show that $\frac{d^2x}{dt^2} = -98x$. [3]
- (iii) Find the value of x and the magnitude and direction of the velocity of P when $t = 0.2$. [7]

[Questions 6 and 7 are printed overleaf.]



A particle P , of mass 3.5 kg , is in equilibrium suspended from the top A of a smooth slope inclined at an angle θ to the horizontal, where $\sin \theta = \frac{40}{49}$, by an elastic rope of natural length 4 m and modulus of elasticity 112 N (see diagram). Another particle Q , of mass 0.5 kg , is released from rest at A and slides freely downwards until it reaches P and becomes attached to it.

- (i) Find the value of V^2 , where $V \text{ m s}^{-1}$ is the speed of Q immediately before it becomes attached to P , and show that the speed of the combined particles, immediately after Q becomes attached to P , is $\frac{1}{2}\sqrt{5} \text{ m s}^{-1}$. [6]

The combined particles slide downwards for a distance of $X \text{ m}$, before coming instantaneously to rest at B .

- (ii) Show that $28X^2 - 8X - 5 = 0$. [6]

- 7 A particle P of mass 0.2 kg is released from rest at a point O and falls vertically. Air resistance of magnitude $\frac{v^2}{2000} \text{ N}$ acts upwards on P , where $v \text{ m s}^{-1}$ is the velocity of P when it has fallen a distance of $x \text{ m}$.

- (i) Show that $\left(\frac{400v}{3920 - v^2} \right) \frac{dv}{dx} = 1$. [2]

- (ii) Find v^2 in terms of x and hence show that $v^2 < 3920$ for all values of x . [7]

- (iii) Find the work done against the air resistance while P is falling, from O , to the point where its downward acceleration is 5.8 m s^{-2} . [6]

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