

**Mark Scheme 4730**  
**June 2006**

1	(i)	M1		For using $I = \Delta(mv)$ in the direction of the original motion (or equivalent from use of relevant vector diagram).
	$20\cos\theta = 0.4 \times 25$ Direction at angle $120^\circ$ to original motion	A1 A1	3	Accept $\theta = 60^\circ$ with $\theta$ correctly identified.
	(ii)	M1		For using $I = \Delta(mv)$ perp. to direction of the original motion (or equivalent from use of relevant vector diagram).
	$20\sin 60^\circ = 0.4v$ Speed is $43.3 \text{ ms}^{-1}$	A1ft A1	3	
2		M1		For applying Newton's 2 <sup>nd</sup> Law.
		M1		For using $a = v(dv/dx)$ .
	$2v(dv/dx) = -(2v + 3v^2)$	A1		
		M1		For separating variables and attempting to integrate.
	$2/3 \ln(2 + 3v) = -x \quad (+C)$ [ $2/3 \ln 14 = C$ ]	A1ft		ft absence of minus sign,
	[ $2/3 \ln 2 = -x + 2/3 \ln 14$ ]	M1		For using $v(0) = 4$ .
	Comes to rest after travelling 1.30m	M1		For attempting to solve $v(x) = 0$ for $x$ .
		A1	8	AG

<b>3</b>	<b>(i)</b>		M1	For taking moments about C for the whole structure.	
		$1.4R = 0.35 \times 360 + 1.05 \times 200$	A1		
		Magnitude is 240N	A1	AG	
			M1	For taking moments about A for the rod AB.	
		$0.7 \times 240 = 0.35 \times 200 + 1.05T$	A1		
		Tension is 93.3N	A1		6
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	<b>OR</b>				
	<b>(i)</b>		M1	For taking moments about A for AB and AC.	
		$0.7R_B = 70 + 1.05T$ and	A1		
		$0.7R_C = 126 + 1.05T$			
			M1	For eliminating T or for adding the equations, and then using $R_B + R_C = 560$ .	
		$0.7(560 - R_B) - 0.7R_B = 126 - 70$ or	A1	For a correct equation in $R_B$ only or T only	
		$0.7 \times 560 = 70 + 126 + 2.1T$			
		Magnitude is 240N	A1	AG	
		Tension is 93.3N	A1		6
	<b>(ii)</b>	Horizontal component is 93.3 N to the left	B1ft		
		$Y = 240 - 200$	M1	For resolving forces vertically.	
		Vertical component is 40 N downwards	A1		3

4	(i)	M1	For using Newton's 2 <sup>nd</sup> Law	
		A1	perp. to string with $a = L \ddot{\theta}$ .	
		B1		
	(ii)	M1	For using $T = 2\pi/\omega$ and $k = \omega^2$ or $T = 2\pi\sqrt{L/g}$ for simple pendulum.	
		A1	5	AG
	(i)	M1	For using $\dot{\theta}^2 = \omega^2(\theta_0^2 - \theta^2)$ or the principle of conservation of energy	
	(ii)	A1		
	(iii)	A1	3	(0.1599... from energy method)
	OR	(in the case for which (iii) is attempted before (ii))		
	(ii)	M1	For using $\dot{\theta} = d(A\cos nt)/dt$	
	(iii)	A1ft		
	(i)	A1	3	
	(ii)	M1	For using $\theta = A\cos nt$ or $A\sin(\pi/2 - nt)$ or for using $\theta = A\sin nt$ and $T = t_{0.1} - t_{0.06}$	
	(iii)	A1ft	ft angular displacement of 0.04 instead of 0.06	
	(i)	A1	3	

5		M1		$\Sigma mv$ conserved in <b>i</b> direction.
	$2 \times 12 \cos 60^\circ - 3 \times 8 = 2a + 3b$	A1		
		M1		For using NEL
	For LHS of equation below	A1		
	$0.5(12 \cos 60^\circ + 8) = b - a$	A1		Complete equation with signs of <b>a</b> and <b>b</b> consistent with previous equation.
		M1		For eliminating <b>a</b> or <b>b</b> .
	Speed of <b>B</b> is $0.4 \text{ ms}^{-1}$ in <b>i</b> direction	A1		
	<b>a</b> = -6.6	A1		
6	Component of <b>A</b> 's velocity in <b>j</b> direction is	B1		May be shown on diagram or implied in subsequent work.
	$12 \sin 60^\circ$			
	Speed of <b>A</b> is $12.3 \text{ ms}^{-1}$	B1ft		
		M1		For using $\theta = \tan^{-1}(\text{jcomp}/\pm \text{i comp})$
	Direction is at $122.4^\circ$ to the <b>i</b> direction	A1ft	1	Accept $\theta = 57.6^\circ$ with
			2	$\theta$ correctly identified.
	(i) $T = 1470x/30$	B1		
	$[49x = 70 \times 9.8]$	M1		For using $T = mg$
	$x = 14$	A1		
	Distance fallen is 44m	A1ft	4	
	(ii) PE loss = $70g(30 + 14)$	B1ft		
	EE gain = $1470 \times 14^2 / (2 \times 30)$	B1ft		
	$[\frac{1}{2} 70v^2 = 30184 - 4802]$	M1		For a linear equation with terms representing KE, PE and EE changes.
	Speed is $26.9 \text{ ms}^{-1}$	A1	4	AG
	OR			
	(ii) $[0.5 v^2 = 14g - 68.6 + 30g]$	M1		For using Newton's 2 <sup>nd</sup> law ( $v dv/dx = g - 0.7x$ ), integrating ( $0.5 v^2 = gx - 0.35x^2 + k$ ), using $v(0)^2 = 60g \rightarrow k = 30g$ , and substituting $x = 14$ .
	For $14g + 30g$	B1ft		
	For $\mp 68.6$	B1ft		
	Speed is $26.9 \text{ ms}^{-1}$	A1	4	Accept in unsimplified form. AG
	(iii) PE loss = $70g(30 + x)$	B1ft		
	EE gain = $1470x^2 / (2 \times 30)$	B1ft		
	$[x^2 - 28x - 840 = 0]$	M1		For using PE loss = KE gain to obtain a 3 term quadratic equation.
	Extension is 46.2m	A1	4	
	OR			
	(iii)	M1		For identifying SHM with $n^2 =$
				$1470/(70 \times 30)$
		M1		For using $v_{\max} = An$
	$A = 26.9/\sqrt{0.7}$	A1		
	Extension is 46.2m	A1	4	

7	(i)	$\frac{1}{2} 0.3v^2 + \frac{1}{2} 0.4v^2$	B1		
		$\pm 0.3g(0.6\sin \theta)$	B1		
		$\pm 0.4g(0.6 \theta)$	B1		
		$[0.35v^2 = 2.352 \theta - 1.764\sin \theta]$	M1		For using the principle of conservation of energy.
		$v^2 = 6.72 \theta - 5.04\sin \theta$	A1	5	AG
	(ii)		M1		For applying Newton's 2 <sup>nd</sup> Law radially to P and using $a = v^2/r$
		$0.3(v^2/0.6) = 0.3g\sin \theta - R$	A1		
		$[\frac{1}{2} (6.72 \theta - 5.04\sin \theta) =$	M1		For substituting for $v^2$ .
		$0.3g\sin \theta - R]$			
		Magnitude is $(5.46\sin \theta - 3.36 \theta)N$	A1		AG
		$[5.46\cos \theta - 3.36 = 0]$	M1		For using $dR/d \theta = 0$
		Value of $\theta$ is 0.908	A1	6	
	(iii)	$[T - 0.3g\cos \theta = 0.3a]$	M1		For applying Newton's 2 <sup>nd</sup> Law tangentially to P
		$[0.4g - T = 0.4a]$	M1		For applying Newton's 2 <sup>nd</sup> Law to Q
					[If $0.4g - 0.3g\cos \theta = 0.3a$ is seen, assume this derives from
					$T - 0.3g\cos \theta = 0.3a$ ..... M1 and $T = 0.4g$ ..... M0]
		Component is $5.6 - 4.2\cos \theta$	A1	3	
OR					
(iii)	$0.4g - 0.3g\cos \theta = (0.3 + 0.4)a$	B2			
	Component is $5.6 - 4.2\cos \theta$	B1	3		
OR					
(iii)	$[2v(dv/d \theta) = 6.72 - 5.04\cos \theta]$	M1		For differentiating $v^2$ (from (i)) w.r.t. $\theta$	
	$2 (0.6a) = 6.72 - 5.04\cos \theta$	M1		For using $v(dv/d \theta) = ar$	
	Component is $5.6 - 4.2\cos \theta$	A1	3		