Mark Scheme 4725 June 2007

1	EITHER	M1		Use trig to find an expression for a (or b)
1	a=2	A1		Obtain correct answer
	a - 2	M1		Attempt to find other value
	_	A1		Obtain correct answer a.e.f.
	$b=2\sqrt{3}$,	M1		(Allow 3.46)
	OR	M1		State 2 equations for a and b
		A1 A1	4	State 2 equations for a und o
			·	Attempt to solve these equations
	$a = 2$ $b = 2\sqrt{3}$			Obtain correct answers a.e.f.
	$u = 2$ $v = 2\sqrt{3}$		4	SR ± scores A1 only
			-	
2	3 1 2 2	B1		Show result true for $n = 1$
	$(1^3 =)\frac{1}{4} \times 1^2 \times 2^2$			
		M1		Add next term to given sum formula
	$\frac{1}{2}$	M1(indep)		Attempt to factorise and simplify
	$\frac{1}{4}n^2(n+1)^2+(n+1)^3$	A1		Correct expression obtained convincingly
		A1	5	
	$\frac{1}{4}(n+1)^2(n+2)^2$			Specific statement of induction conclusion
	4			1
			5	
3	2	M1	3	Consider the sum of three separate terms
3	$3\Sigma r^2 - 3\Sigma r + \Sigma 1$	IVII		Consider the sum of three separate terms
				Correct formula stated
	$3\sum_{n}^{2} = \frac{1}{2}n(n+1)(2n+1)$	A1		Correct formula stated
	$3\Sigma r^2 = \frac{1}{2}n(n+1)(2n+1)$			
	$3\Sigma r = \frac{3}{2}n(n+1)$	A1		Correct formula stated
	2			
		A1		Correct term seen
	$\Sigma 1 = n$	M1		Attempt to simplify
	$\sum_{n=1}^{\infty} 1 = n$	A1	6	Obtain given answer correctly
			6	
4		B1		Transpose leading diagonal and negate other
	$\binom{1}{6} \frac{1}{2} \binom{5}{6} - 1$			diagonal or solve sim. eqns. to get 1 st column
	(i) $\frac{1}{2}$ $\begin{pmatrix} 5 & -1 \\ -3 & 1 \end{pmatrix}$	B1	2	Divide by the determinant or solve 2 nd pair to
	(3 1)			get 2 nd column
	(ii)	3.61		
		M1		Attempt to use B ⁻¹ A ⁻¹ or find B
	1 (2 0)	Michael	4	Attempt at matrix multiplication
	$\frac{1}{2}$ $\begin{pmatrix} 2 & 0 \\ 23 & -5 \end{pmatrix}$	M1(indep)	4	One element correct, a.e.f,
	(23 - 5)	A 1 ft	6	All elements correct, a.e.f.
		A1ft		NB ft consistent with their (i)
		A1ft		
		11110		

5	$(i) \frac{1}{r(r+1)}$	B1	1	Show correct process to obtain given result
	(iii) $1 - \frac{1}{n+1}$ (iii) $S_{\infty} = 1$ $\frac{1}{n+1}$	M1 M1 A1 B1ft M1 A1 c.a.o.	3 3 7	Express terms as differences using (i) Show that terms cancel Obtain correct answer, must be <i>n</i> not any other letter State correct value of sum to infinity Ft their (ii) Use sum to infinity – their (ii) Obtain correct answer a.e.f.
6	(i) (a) $\alpha + \beta + \gamma = 3, \alpha\beta + \beta\gamma + \gamma\alpha = 2$ (b)	B1 B1	2	State correct values
	$\alpha^{2} + \beta^{2} + \gamma^{2} = (\alpha + \beta + \gamma)^{2} - 2(\alpha\beta + \beta\gamma + \gamma\alpha)$ $= 9 - 4 = 5$ (ii) (a) $\frac{3}{u^{3}} - \frac{9}{u^{2}} + \frac{6}{u} + 2 = 0$ $2u^{3} + 6u^{2} - 9u + 3 = 0$ (b) $\frac{1}{\alpha} + \frac{1}{\beta} + \frac{1}{\gamma} = -3$	M1 A1 ft M1 A1 A1 A1 A1 A1	2 2 2 8	State or imply the result and use their values Obtain correct answer Use given substitution to obtain an equation Obtain correct answer Required expression is related to new cubic stated or implied -(their "b" / their "a")

	40		1	1 ~
7	(i)	M1		Show correct expansion process
		M1		Show evaluation of a 2 x 2
	a(a - 12) + 32	A1	3	determinant
	(ii)			Obtain correct answer a.e.f.
	$\det \mathbf{M} = 12$	M1	2	
	non-singular	A1ft		Substitute $a = 2$ in their determinant
	(iii) EITHER	B1		
		M1		Obtain correct answer and state a
	OR			consistent conclusion
	-	A1	3	
		M1		$\det \mathbf{M} = 0$ so non-unique solutions
		A1		1
		A1		Attempt to solve and obtain 2
				inconsistent equations
				Deduce that there are no solutions
				Substitute $a = 4$ and attempt to solve
				Obtain 2 correct inconsistent
				equations
			8	Deduce no solutions
8	(i) Circle, centre (3, 0),	B1B1		Sketch showing correct features
	y-axis a tangent at origin	B1		N.B. treat 2 diagrams asa MR
	Straight line,	B1		
	through $(1, 0)$ with +ve slope	B1		
	In 1 st quadrant only	B1		
	(ii) Inside circle, below line,	B2ft	6	Sketch showing correct region
	above <i>x</i> -axis		2	SR: B1ft for any 2 correct features
			8	
		1		1

9	$(\sqrt{2} 0)$	B1	1	Correct matrix
	(i) $\begin{pmatrix} \sqrt{2} & 0 \\ 0 & \sqrt{2} \end{pmatrix}$			
	(ii) Rotation (centre <i>O</i>), 45 ⁰ , clockwise	B1B1B1	3	Sensible alternatives OK, must be a
	(iii)			single transformation
		D1	1	Matrix multiplication or combination
		B1	1	of transformations
	(iv) $\begin{pmatrix} 0 \\ 0 \end{pmatrix}$ $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 1 \\ -1 \end{pmatrix}$ $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$	M1		
		A1	2	For at least two correct images For correct diagram
		B1		State correct value
	(v) $\det \mathbf{C} = 2$	B1	2	State correct relation a.e.f.
	area of square has been doubled	DI		
10		3.61	9	Au 1 1 1
10	(i)	M1		Attempt to equate real and imaginary parts of
	$x^2 - y^2 = 16$ and $xy = 15$			$(x + iy)^2$ and 16+30i
		A1A1		Obtain each result
		M1		Eliminate to obtain a quadratic in x^2 or y^2
	$\pm (5+3i)$	M1		Solve to obtain
				$x = (\pm) 5 \text{ or } y = (\pm) 3$
	(ii)	A1	6	Obtain correct answers as complex
	$z = 1 \pm \sqrt{16 + 30i}$			numbers
		M1*		Use quadratic formula or complete the square
	6 + 3i, -4 - 3i	A1		
		*M1dep	5	Simplify to this stage
		A1 A1ft		Use answers from (i)
			11	Obtain correct answers
<u> </u>			11	