

<b>1</b>	<p>For included angle marked <math>\alpha</math> or for <math>0.8(10.5 - 8.5\cos\alpha) = 4\cos\beta</math>  For opposite side marked 4/0.8 (or 4) or for <math>-0.8 \times 8.5\sin\alpha = 4\sin\beta</math></p> <p><math>8.4^2 + 6.8^2 - 2 \times 8.4 \times 6.8 \cos\alpha = 4^2</math>  <math>\alpha = 28.1^\circ</math></p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1ft</p> <p>A1</p> <p>[6]</p>	<p>For triangle with two of its sides marked 0.8 x 10.5 and 0.8 x 8.5 (or 10.5 and 8.5) or for using <math>I = \Delta mv</math> in one direction.</p> <p>Allow B1 for omission of 0.8</p> <p>Allow B1 for omission of 0.8</p> <p>For using the cosine rule or for eliminating <math>\beta</math></p> <p>ft 0.8 mis-used or not used</p>
<b>2(i)</b>	<p>[100a = 2aV<sub>B</sub>]  Vertical component at B is 50 N  Vertical component at C is 150 N</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>	<p>For taking moments about A for AB</p>
<b>(ii)</b>	<p><math>100(0.5a) + (\sqrt{3}a)F = 150a</math> or  <math>100a + 100(1.5a) = 150a + (\sqrt{3}a)F</math>  Frictional force is 57.7 N  Direction is to the right</p>	<p>M1</p> <p>A1ft</p> <p>A1</p> <p>B1</p> <p>[4]</p>	<p>For taking moments about B for BC (3 terms needed) or about A for the whole (4 terms needed)</p>
<b>3(i)</b>	<p><math>u = 4</math>  <math>v = 2</math></p>	<p>B1</p> <p>B1</p> <p>[2]</p>	
<b>(ii)</b>	<p><math>mu = ma + mb</math> (or <math>u = b - a</math>)  <math>u = b - a</math> (or <math>mu = ma + mb</math>)  <math>a = 0</math> and <math>b = 4\text{ms}^{-1}</math>  Speed of A is <math>2\text{ms}^{-1}</math> and direction at <math>90^\circ</math> to the wall  Speed of B is <math>4\text{ms}^{-1}</math> and direction parallel to the wall</p>	<p>M1</p> <p>A1</p> <p>B1</p> <p>A1ft</p> <p>A1ft</p> <p>A1ft</p> <p>[6]</p>	<p>For using the principle of conservation of momentum or for using NEL with <math>e = 1</math></p> <p>ft incorrect u</p> <p>ft incorrect v</p> <p>ft incorrect u</p>
<b>4(i)</b>	<p>[0.25 dv/dt = 3/50 - <math>t^2/2400</math>]   <math>v = 12t/50 - t^3/1800</math>  [v(12) = 1.92]  [0.25 dv/dt = <math>t^2/2400 - 3/50 \rightarrow</math>  <math>v = t^3/1800 - 12t/50 + C_2</math>]  [1.92 = 0.96 - 2.88 + <math>C_2</math>]  <math>v = t^3/1800 - 12t/50 + 3.84</math>  <math>v(24) = 5.76 = 3 \times v(12)</math></p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[8]</p>	<p>For using Newton's second law (1<sup>st</sup> or 2<sup>nd</sup> stage)  For attempting to integrate (1<sup>st</sup> stage) and using <math>v(0) = 0</math> (may be implied by the absence of + <math>C_1</math>)</p> <p>For evaluating v when force is zero</p> <p>For using Newton's second law (2<sup>nd</sup> stage) and integrating</p> <p>For using <math>v(12) = 1.92</math></p> <p>AG</p>

(ii)	Sketch has $v(0) = 0$ and slope decreasing (convex upwards) for $0 < t < 12$ Sketch has slope increasing (concave upwards) for $12 < t < 24$ Sketch has $v(t)$ continuous, single valued and increasing (except possibly at $t = 12$ ) with $v(24)$ seen to be $> 2v(12)$	B1 B1 B1 [3]	
5(i)	For using amplitude as a coefficient of a relevant trigonometric function. For using the value of $\omega$ as a coefficient of $t$ in a relevant trigonometric function. $x_1 = 3\cos t$ and $x_2 = 4\cos 1.5t$	B1 B1 B1 [3]	
(ii)	Part distance is 20m  [20 – (-3.62)] Distance travelled by $P_2$ is 23.6 m	M1 A1  M1 A1 [4]	For using distance travelled by $P_2$ for $0 < t < 5\pi/3$ is $5A_2$  For subtracting displacement of $P_2$ when $t = 5.99$ from part distance.
(iii)	$\dot{x}_1 = -3\sin t$ ; $\dot{x}_2 = -6\sin 1.5t$  $v_1 = 0.867$ , $v_2 = -2.55$ ; opposite directions	M1 A1  M1 A1 [4]	For differentiating $x_1$ and $x_2$  For evaluating when $t = 5.99$ (must use radians)
	Alternative for (iii):  $v_1^2 = 3^2 - 2.87^2$ , $v_2^2 = 2.25[4^2 - (-3.62)^2]$ [ $\pi < 5.99 < 2\pi \rightarrow v_1 > 0$ , $4\pi/3 < 5.99 < 2\pi \rightarrow v_2 < 0$ ] $v_1 = 0.867$ , $v_2 = -2.55$ ; opposite directions	M1 A1  M1 A1	For using $v^2 = n^2(a^2 - x^2)$ (must use radians to find values of $x$ )  For using the idea that $v$ starts –ve and changes sign at intervals of $T/2$ s
6(i)	PE loss at lowest allowable point = 25W  EE gain = $32000x^2/(2 \times 20)$  [25W = 20000] Value of $W$ is 800	B1  M1 A1  M1 A1 [5]	For using $EE = \lambda x^2/(2L)$ ; may be scored in (i) or in (ii)  For equating PE loss and EE gain and attempting to solve for $W$
(ii)	[800 = 32000x/20]  $\frac{1}{2}(800/9.8)v^2$ = $800 \times 20.5 - 32000x0.5^2/(2 \times 20)$ Maximum speed is $19.9\text{ms}^{-1}$	M1  M1  A1 A1 [4]	For using $W = \lambda x/L$ at max speed For using the principle of conservation of energy (3 terms required)
(iii)	$(800)\ddot{x}/g = 800 - 32000 \times 5/20$ Max. deceleration is $88.2\text{ms}^{-2}$	M1 A1 A1 [3]	For applying Newton's second law to jumper at lowest point (3 terms needed)

7(i)	$[\frac{1}{2}mv^2 - \frac{1}{2}m6^2 = mg(0.7)]$ Speed of P before collision is $7.05\text{ms}^{-1}$ Coefficient of restitution is 0.695	M1 A1 B1ft [3]	For using the principle of conservation of energy for P (3 terms needed) ft $4.9 \div$ speed of P before collision
(ii)	$[\frac{1}{2}mv^2 = \frac{1}{2}m4.9^2 - mg0.7(1 - \cos\theta)]$ $v^2 = 3.43(3 + 4\cos\theta)$  $T - mg\cos\theta = mv^2/0.7$ $[T - m9.8\cos\theta = m3.43(3 + 4\cos\theta)/0.7]$ Tension is $14.7m(1 + 2\cos\theta)$ N	M1 A1  M1 A1  M1 A1 [6]	For using the principle of conservation of energy for Q Accept any correct form For using Newton's second law radially with $a_r = v^2/r$  For substituting for $v^2$ AG
(iii)	$T = 0 \Rightarrow \theta = 120^\circ$  Radial acceleration is $(\pm)4.9\text{ms}^{-1}$ <b>or</b> transverse acceleration is $(\pm)8.49\text{ms}^{-1}$ Radial acceleration is $(\pm)4.9\text{ms}^{-1}$ <b>and</b> transverse acceleration is $(\pm)8.49\text{ms}^{-1}$	B1  M1  A1  B1 [4]	For using $a_r = -g\cos\theta$ {or $3.43(3 + 4\cos\theta)/0.7$ } or $a_t = -g\sin\theta$
			SR for candidates with a sin/cos mix in the work for M1 A1 B1 immediately above. (max. 1/3) Radial acceleration is $(\pm)8.49\text{ms}^{-1}$ <b>and</b> transverse acceleration is $(\pm)4.9\text{ms}^{-1}$ B1
(iv)	$[V^2 = 3.43\{3 + 4(-0.5)\} \times 0.5^2 \text{ or } V^2 = (-g\cos 120^\circ \times 0.7) \times \cos^2 60^\circ]$ $V^2 = 0.8575$ $[mgH = \frac{1}{2}m(4.9^2 - 0.8575) \text{ or } mg(H - 1.05) = \frac{1}{2}m(3.43 - 0.8575)]$ Greatest height is 1.18 m	M1 A1  M1 A1 [4]	For using $V = v(120^\circ) \times \cos 60^\circ$ AG For using the principle of conservation of energy