OCR
RECOGNISING ACHIEVEMENT

GCE

Mathematics

Advanced GCE

Unit **4725:** Further Pure Mathematics 1

Mark Scheme for June 2011

Oxford Cambridge and RSA Examinations

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of pupils of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, OCR Nationals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by Examiners. It does not indicate the details of the discussions which took place at an Examiners' meeting before marking commenced.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the Report on the Examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

Any enquiries about publications should be addressed to:

OCR Publications
PO Box 5050
Annesley
NOTTINGHAM
NG15 0DL

Telephone: 0870 770 6622
Facsimile: 01223 552610
E-mail: publications@ocr.org.uk

1	**(i)** $\begin{pmatrix} 4 & 4a \\ 12 & 0 \end{pmatrix}$	B1		3**B** seen or implied
		B1		2 elements correct
		B1	**3**	Other 2 elements correct, a.e.f., including brackets
	(ii) $\begin{pmatrix} 4+4a & 3a \\ 4 & 1 \end{pmatrix}$	M1		Sensible attempt at matrix multiplication for **AB** or **BA**
		A1	**2**	Obtain correct answer
		5		
2		B1		Establish result true for $n = 1$ or 2
		M1*		Add next term to given sum formula
		DM1		Combine with correct denominator
		A1		Obtain correct expression convincingly
		A1	**5**	Specific statement of induction conclusion, provided 1st 4 marks earned
		5		
3	$k^2 - 16$	B1		Obtain correct det
		M1		Equate their det to 0
	$k = \pm 4$	A1	**3**	Obtain correct answers
		3		
4	$3 \times \frac{1}{6} \times 2n(2n+1)(4n+1) - \frac{1}{2} \times 2n$	M1		Express as sum of two series
		A1 A1		Each term correct a.e.f.
		M1		Attempt to factorise
	$2n^2(4n+3)$	A2	**6**	Completely correct answer, (A1 if one factor not found)
		6		
5	**(i)** $\lvert a \rvert = 2$	B1		Correct modulus
	$\arg a = 60°, \frac{\pi}{3}$, 1.05	B1	**2**	Correct argument
	(ii)	B1		Circle
		B1		Centre $(1, \sqrt{3})$
		B1		Through origin, centre $(\pm 1, \pm\sqrt{3})$ and another y intercept
		B1		Vertical line
		B1*		Through *a* or their centre, with +ve gradient
		DB1		Correct half line
			6	
		8		

6		M1		Show correct expansion process for 3×3 or multiplication of **C** and adj**C**
		M1		Correct evaluation of any 2×2
	det **C** = $\Delta = 5a-5$	A1		Obtain correct answer
		M1		Show correct process for adjoint entries
	$\frac{1}{\Delta}\begin{pmatrix} 5 & -4 & 1 \\ -5 & 4a & -a \\ 5 & -3a-1 & 2a-1 \end{pmatrix}$	A1		Obtain at least 4 correct entries in adjoint
		A1		Obtain completely correct adjoint
		B1		Divide their adjoint by their determinant
			7	
		7		
7	**(i)**	B1	**1**	Obtain **given** answer correctly
	(ii)	M1		Express at least 1st two and last two terms using (i)
		A1		1st two terms correct
		A1		Last two terms correct
		M1		Show that correct terms cancel
	$\frac{3}{2}-\frac{1}{n}-\frac{1}{(n+1)}$	A1	**5**	Obtain correct answer, a.e.f. in terms of *n*
	(iii)	B1ft		Sum to infinity stated or implied or start at 1000 as in (ii)
		M1		S_∞ – their (ii) with *n* = 999 or 1000 or show correct cancelling
	$\frac{1999}{999000}$	A1	**3**	Obtain correct answer, a.e.f.
				(condone 0.002)
		9		
8	**(i)**	B1		(0, 3) seen
		B1		(3, 0) seen
		B1	**3**	Square with A ' B' and C' positioned correctly
	(ii) $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ **or** $\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$	B1*		Reflection in $y = x$ or $y = -x$
		DB1		Correct matrix, dep on stating reflection
	$\begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$ **or** $\begin{pmatrix} -3 & 0 \\ 0 & -3 \end{pmatrix}$	B1*		Enlargement scale factor 3 or s.f. -3
		DB1	**4**	Correct matrix, dep on stating enlargement **S.C. B2 for a pair of transformations consistent with their diagram.**
		7		

9 (i)	16 + 30i	B1	**1**	State correct value
(ii)		M1		Use a = – (sum of roots)
	a = –32	A1		Obtain correct answer
		M1		Use b = product of roots
	b = 1156	A1	**4**	Obtain correct answer
		M1		Substitute, expand and equate imag. parts
		A1		Obtain **a** = -32
		M1		Equate real parts
		A1		Obtain b = 1156
(iii)		M1		Attempt to equate real and imaginary parts of $(p+iq)^2$ & 16 – 30i or root from (ii)
	$p^2 - q^2 = 16$ and $pq = -15$	A1		Obtain both results cao
		M1		Obtain quadratic in p^2 or q^2
		M1		Solve to obtain $p = (\pm)5$ or $q = (\pm)3$
		A1		Obtain 2 correct answers as complex nos
		M1		Attempt at all 4 roots
	$\pm$ (5 ± 3i)	A1	**7**	State other two roots as complex nos
		12		

10 (i)

$\frac{1}{u^{\frac{3}{2}}} + \frac{3}{u} + 2 = 0$	B1		Use substitution correctly
EITHER	M1		Rearrange
	M1		Square
$\frac{9}{u^2} + \frac{12}{u} + 4 = \frac{1}{u^3}$	A1		Obtain correct equation
$4u^3 + 12u^2 + 9u - 1 = 0$	A1	**5**	Obtain **given** answer
OR			
e. g. $(2u^{3/2} + 3u^{1/2} + 1)(2u^{3/2} + 3u^{1/2} - 1) = 0$	M2		Multiply their equation in u by appropriate related expression
	A2		Obtain **given** answer
(ii)	B1		Stated or imply that $u = \frac{1}{x^2}$
	M1		Use $-\frac{b}{a}$
– 3	A1		Obtain correct answer
	M1		Use $\frac{c}{a}$
$\frac{9}{4}$	A1	**5**	Obtain correct answer
	10		

OCR (Oxford Cambridge and RSA Examinations)
1 Hills Road
Cambridge
CB1 2EU

OCR Customer Contact Centre

14 – 19 Qualifications (General)
Telephone: 01223 553998
Facsimile: 01223 552627
Email: general.qualifications@ocr.org.uk

www.ocr.org.uk

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored

Oxford Cambridge and RSA Examinations
is a Company Limited by Guarantee
Registered in England
Registered Office; 1 Hills Road, Cambridge, CB1 2EU
Registered Company Number: 3484466
OCR is an exempt Charity

OCR (Oxford Cambridge and RSA Examinations)
Head office
Telephone: 01223 552552
Facsimile: 01223 552553